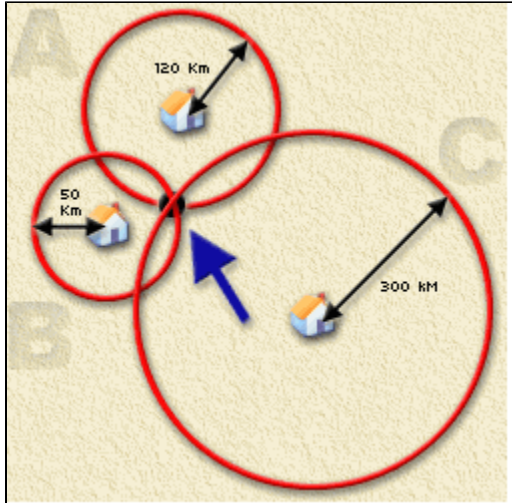


TULIP Algorithm Alternative Trilateration Method

As the name suggests, the [trilateration technique](#) uses three RTT values to estimate the coordinates of target node. In the trilateration technique, when several landmarks ping the specified target, the three landmarks with smallest RTT values (probably nearest located landmarks) are selected. The algorithm then tries to estimate the location on the basis of overlapping region of the drawn circles around these selected landmarks. Figure 1 depicts this technique. In the trilateration technique, the center of the overlapping region is considered as the location of the target node.

Figure 1



There are many ways to implement the trilateration technique, discussed in the paper [Time Of Arrival \(TOA\)- based trilateration method](#). These include:

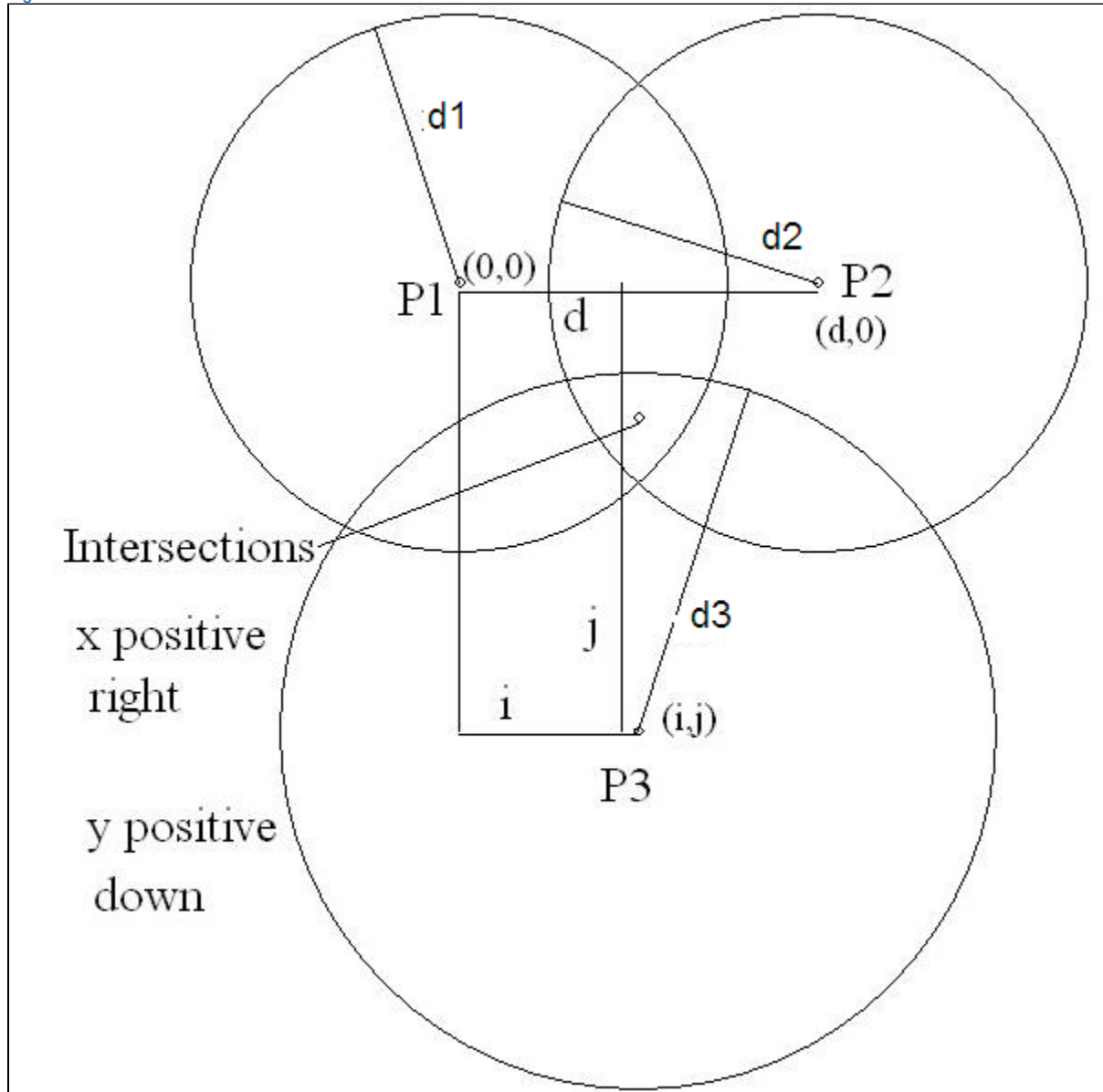
- Linear Least Square Method
- Nonlinear Least Square Method
- Circles intersection with Clustering
- Trilateration in 2D and 3D

Previously we were implementing Linear Least Square Method to implement trilateration. With this method 50% of targets showed distance error above 1000 km. We went through a paper on [Time Of Arrival \(TOA\)- based trilateration method](#) which discusses the different positioning algorithms. In that paper it is mentioned that Linear Least Square Method is not very accurate and it just provides initial position which can be used in other positioning algorithms (i. e. Nonlinear Least Squares and Independent Time GPS Least Squares) as initialization value for further iterations.

We went through [trilateration method as described on wikipedia](#) and found that method to be easy and straight forward. But the algorithm mentioned was solving trilateration in 3D plane. We implemented it in 2D plane.

This method is based on solving equations of circle. Figure 2 below shows three circles drawn from each of three landmarks to the target. d_1 , d_2 , d_3 are the radii of circles.

Figure 2



P1=1st Landmark position in x,y coordinates

P2=2nd Landmark position in x,y coordinates

P3=3rd Landmark position in x,y coordinates

d1= distance from 1st Landmark to target (Calculated using distance=(MinRTT/2)*alpha)

d2=distance from 2nd Landmark to target (Calculated using distance=(MinRTT/2)*alpha)

d3=distance from 3rd Landmark to target (Calculated using distance=(MinRTT/2)*alpha)

i1=P1.x,

i2=P2.x,

i3=P3.x

j1=P1.y,

j2=P2.y,

j3=P3.y

x=target x coordinate

The histograms of the 2 frequency distributions is shown below. The details are found in the [spreadsheet](#).

Frequency histograms of New and old Trilateration methods

