

TULIP Algorithm Trilateration

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minRTT = propagation delay + extra delay (due to extra circular routes , congestion and router delays)

delta(T) measured= delta(t) + delta(t0)

(Pseudo-distance)

PD = delta(T) measured . alpha

(Actual distance)

D = delta(T) . alpha

PD = (delta(T) + delta(T0)). alpha

PD = D + delta(T0) .c(1)

D = actual distance from the landmark.

C = speed of light

alpha = X(c) i.e. Speed of digital info in fiber optic cable

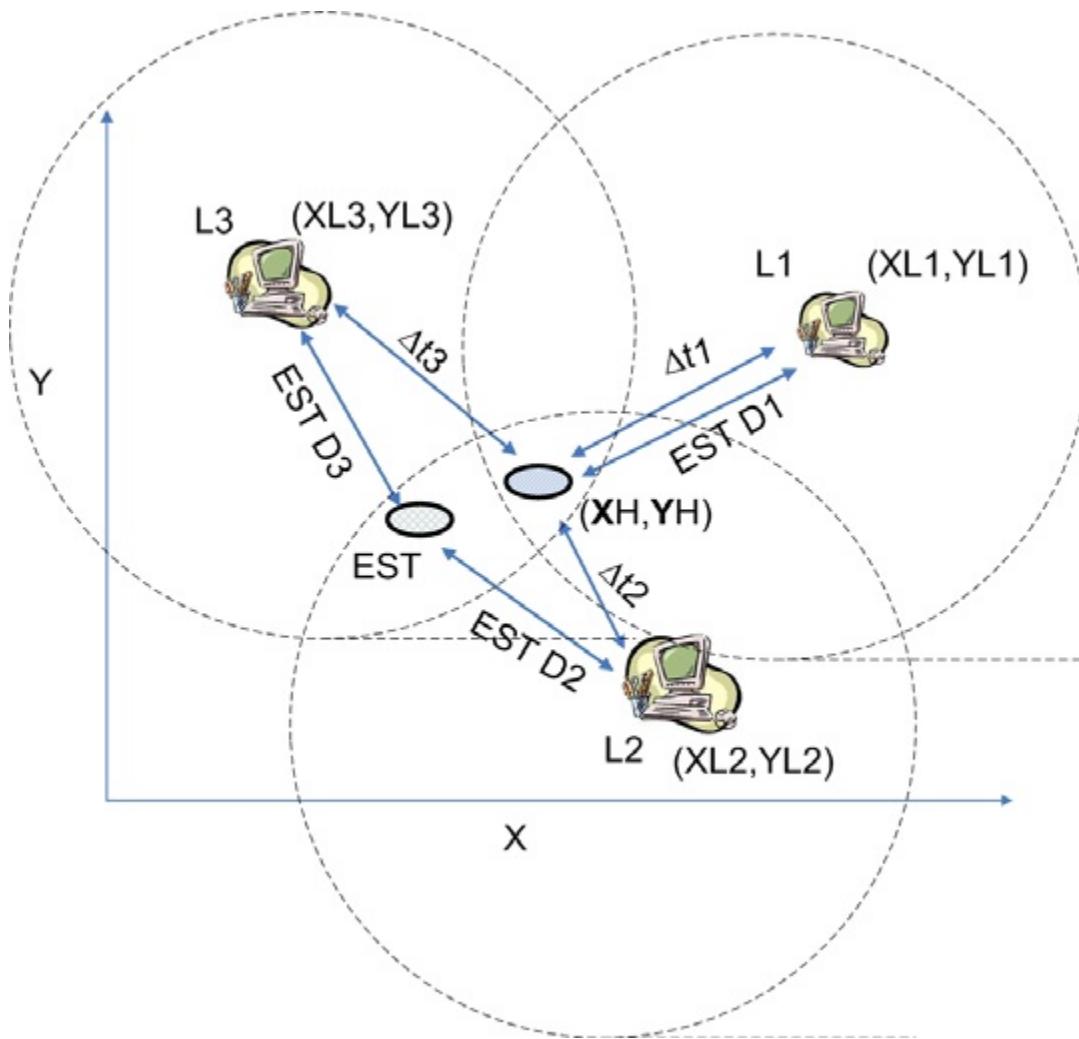
X = factor of c with which digital info travels in fiber optic cable.

delta(T) = actual propagation delay along the greater circle router/path.

delta(T0) = the extra delay causing overestimation.

PD = pseudo distance

Graphically,



H: host

L1: Landmark 1

L2: Landmark 2

L3: Landmark 3

Using distance formula:

$$D_1 = \sqrt{(XL_1 - X_h)^2 + (YL_1 - Y_h)^2} \quad \dots \dots \dots (2)$$

FROM (1) & (2)

$$PD_1 = (\sqrt{(XL_1 - X_h)^2 + (YL_1 - Y_h)^2}) + \delta(t_0) \cdot \alpha \quad \dots \dots \dots (A)$$

Similarly for other 2 landmarks:

$$PD_2 = (\sqrt{(XL_2 - X_h)^2 + (YL_2 - Y_h)^2}) + \delta(t_0) \cdot \alpha \quad \dots \dots \dots (B)$$

$$PD_3 = (\sqrt{(XL_3 - X_h)^2 + (YL_3 - Y_h)^2}) + \delta(t_0) \cdot \alpha \quad \dots \dots \dots (C)$$

We need to linearize (A), (B) & (C) to solve them

Using Taylor Series:

$$f(x_0) \cdot (x - x_0) \quad f'(x_0) \cdot (x - x_0)$$

$$f(x) = f(x_0) + \frac{f'(x_0)}{1!} + \frac{f''(x_0)}{2!}$$

Considering the simplified part first

$$f(x) = f(x_0) + f(x_0)(x - x_0)$$

$$\text{put } (x - x_0) = \delta(x)$$

$$f(x) = f(x_0) + f'(x_0) \delta(x) \dots \dots \dots (3)$$

Hence to compute the original value of X an arbitrary value x_0 is required, this is done by simple trilateration

We know that:

$$Hx = X \text{ est} + \delta(x)$$

$$Hy = Y \text{ est} + \delta(y)$$

Also

From (3) and (4)

d(EstDi) . delta (x) d(EstDi) . delta(y)

$$PDi = Est\ Di + \frac{dX}{dY}$$

After carrying out partial differentiation

$$(X_{est} - X_{li}) \quad (Y_{est} - Y_{li})$$

$$ODI = Est\ Di + \frac{\text{delta (x)}}{dX} + \frac{\text{delta (y)}}{dY} + c.\ \text{delta}(To)$$

Now we need to solve (x , y , delta(to))

$$\begin{bmatrix} PD_1 - E_{st}D_1 \\ PD_2 - E_{st}D_2 \\ PD_3 - E_{st}D_3 \end{bmatrix} = \begin{bmatrix} \frac{(X_{Est} - X_{l1})}{E_{st}D_1} & \frac{(Y_{Est} - Y_{l1})}{E_{st}D_1} \\ \frac{(X_{Est} - X_{l2})}{E_{st}D_2} & \frac{(Y_{Est} - Y_{l2})}{E_{st}D_2} \\ \frac{(X_{Est} - X_{l3})}{E_{st}D_3} & \frac{(Y_{Est} - Y_{l3})}{E_{st}D_3} \end{bmatrix} c \times \begin{bmatrix} \Delta X \\ \Delta Y \\ \Delta t \end{bmatrix}$$

Solution from (4) is put in eq(D) to get new estimations.

Hx,Hy becomes the new estimated position

Reference

<http://www.ece.cmu.edu/research/publications/2003/CMU-ECE-2003-038.pdf>