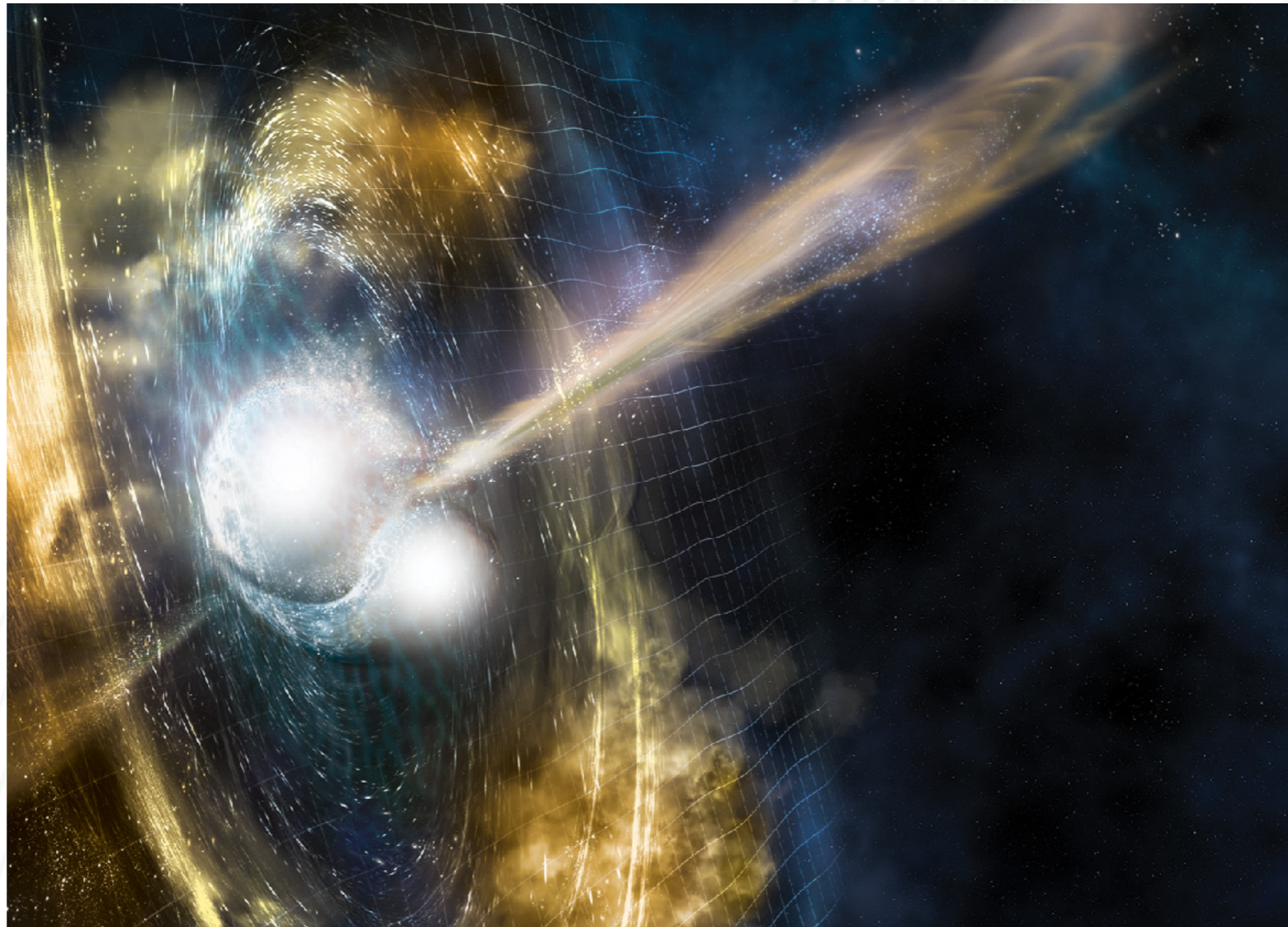




Neutron Stars and Gravitational Waves - Part 2



Cecilia Chirenti

Fermi Summer School - Lewes DE - June 2 2022



Neutron star binaries and gravitational waves

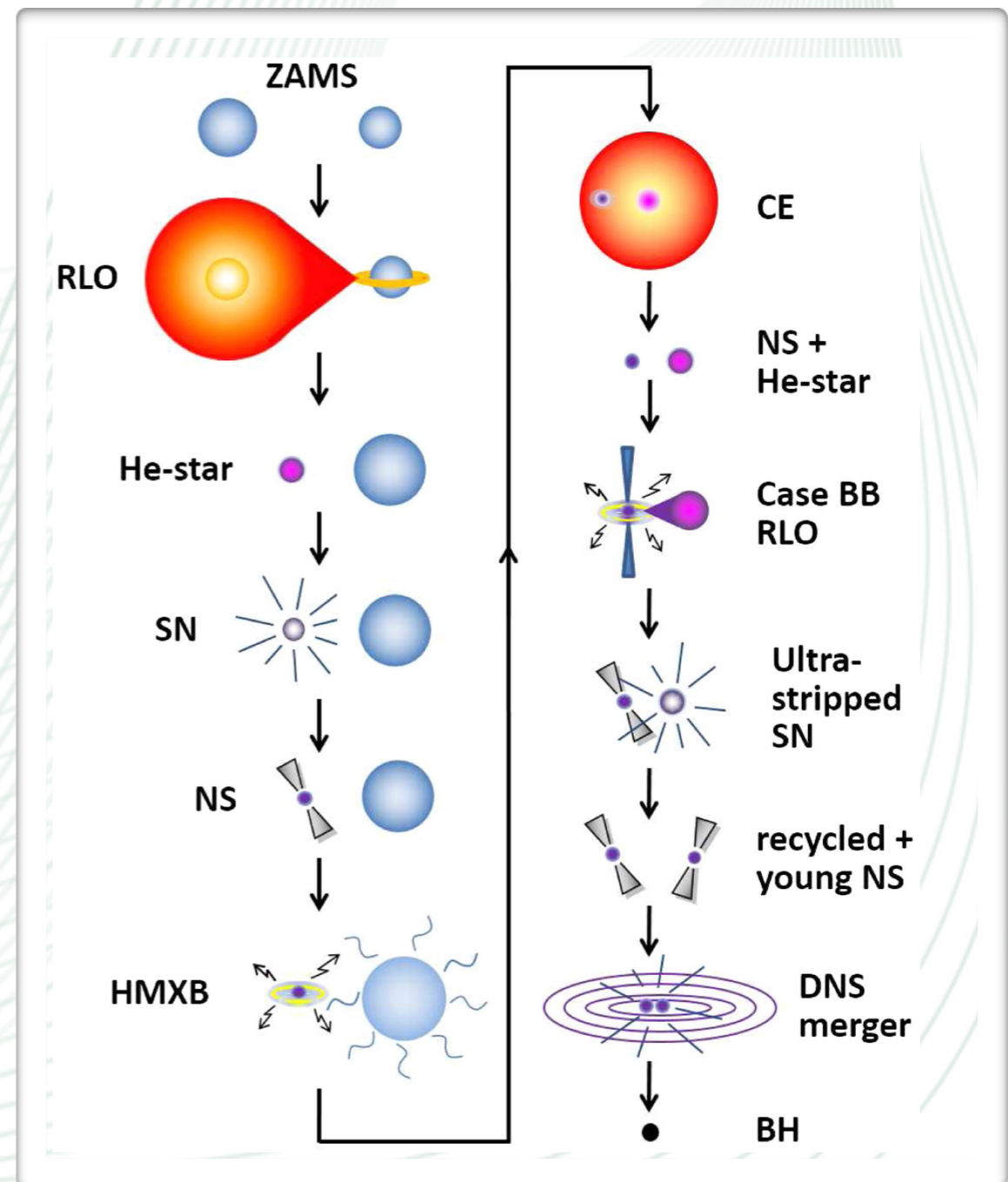
How do neutron stars form binary systems*?

*that collide in a time less than the age of the universe?

Note: we already know 10 such systems in our galaxy!

Question:

What could go wrong in this scenario?



[Tauris et al., 2017]

Rates of binary NS mergers

* before O_I ???

* after O_I

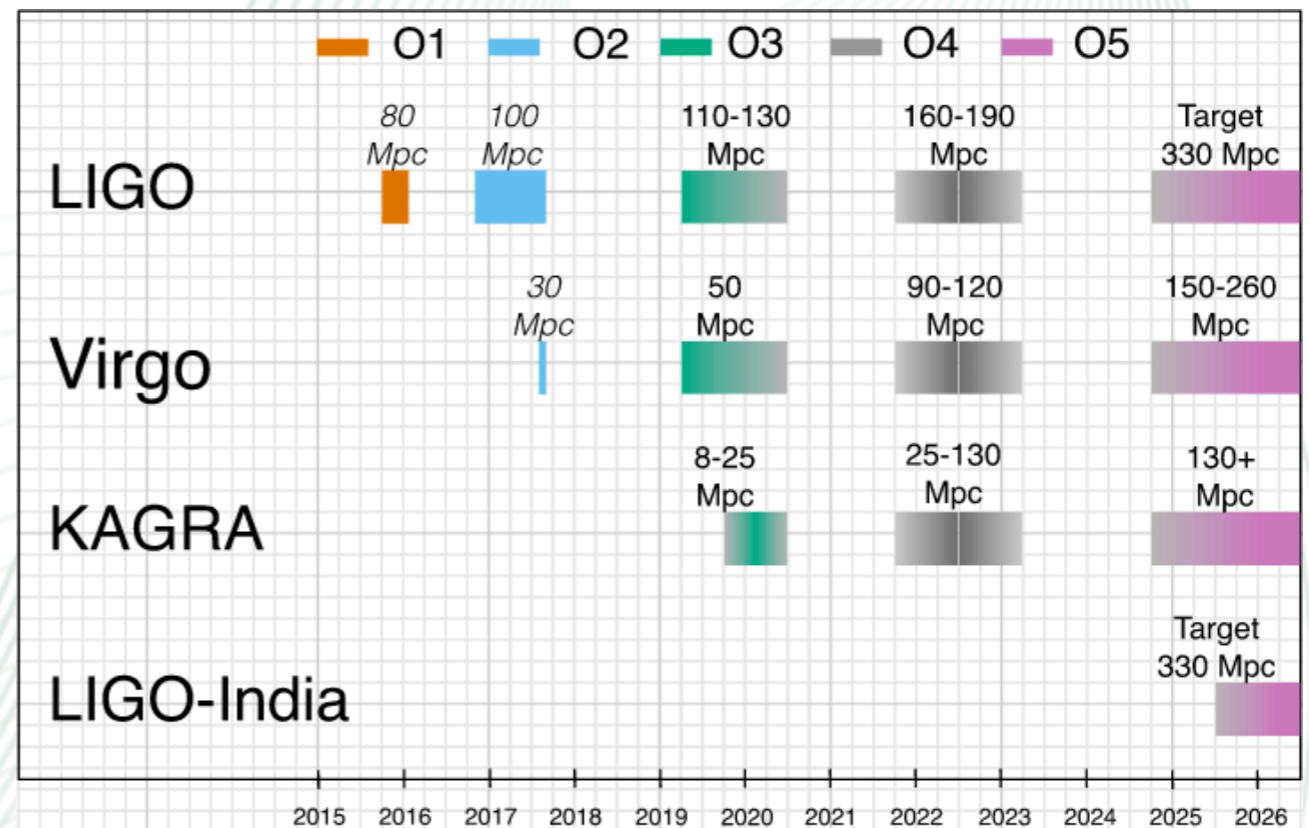
$$110 - 3840 \text{ Gpc}^{-3} \text{ yr}^{-1}$$

* after O₂

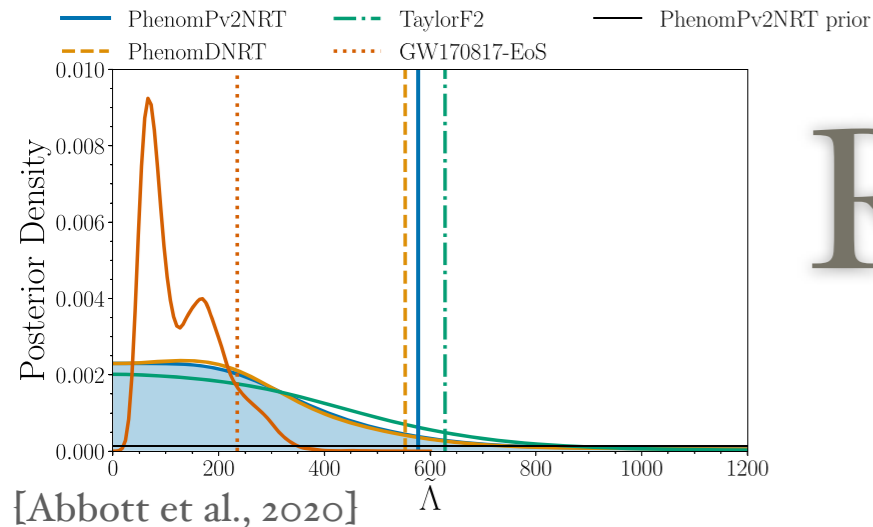
$$80 - 180 \text{ Gpc}^{-3} \text{ yr}^{-1}$$

* after O₃:

$$13 - 1900 \text{ Gpc}^{-3} \text{ yr}^{-1}$$



trend?



Recap: 2 events so far

- * GW170817

- * masses

$$m_1 = 1.36 - 2.26 M_{\odot}$$

$$m_2 = 0.86 - 1.36 M_{\odot}$$

- * distance 40 Mpc

- * observed by H, L, V
with EM counterpart

- * GW190425

- * masses

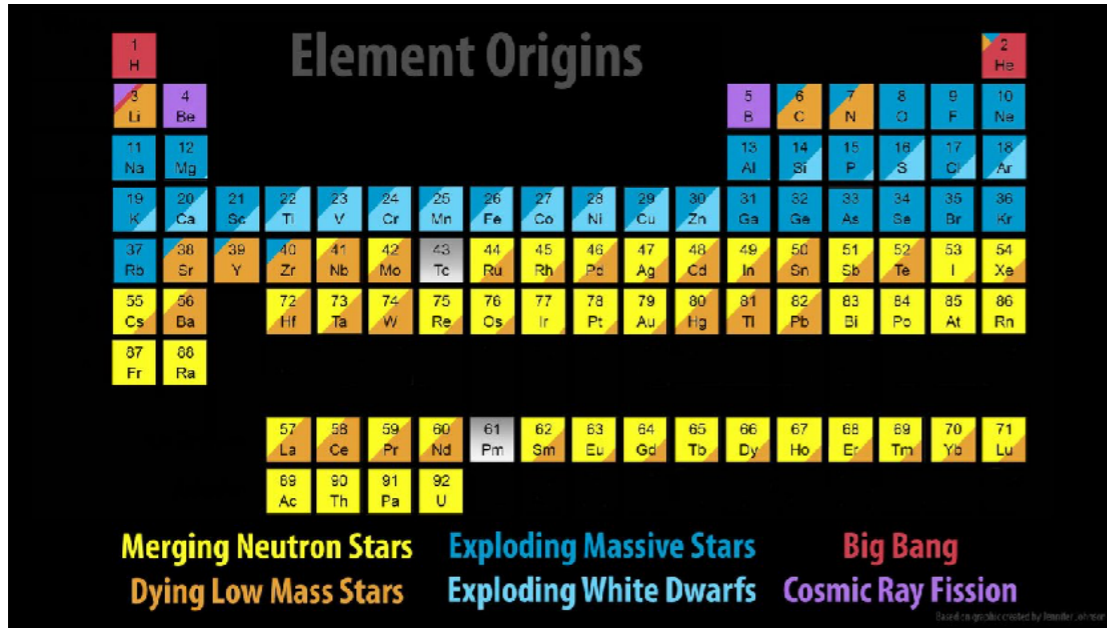
$$m_1 = 1.61 - 2.52 M_{\odot}$$

$$m_2 = 1.12 - 1.61 M_{\odot}$$

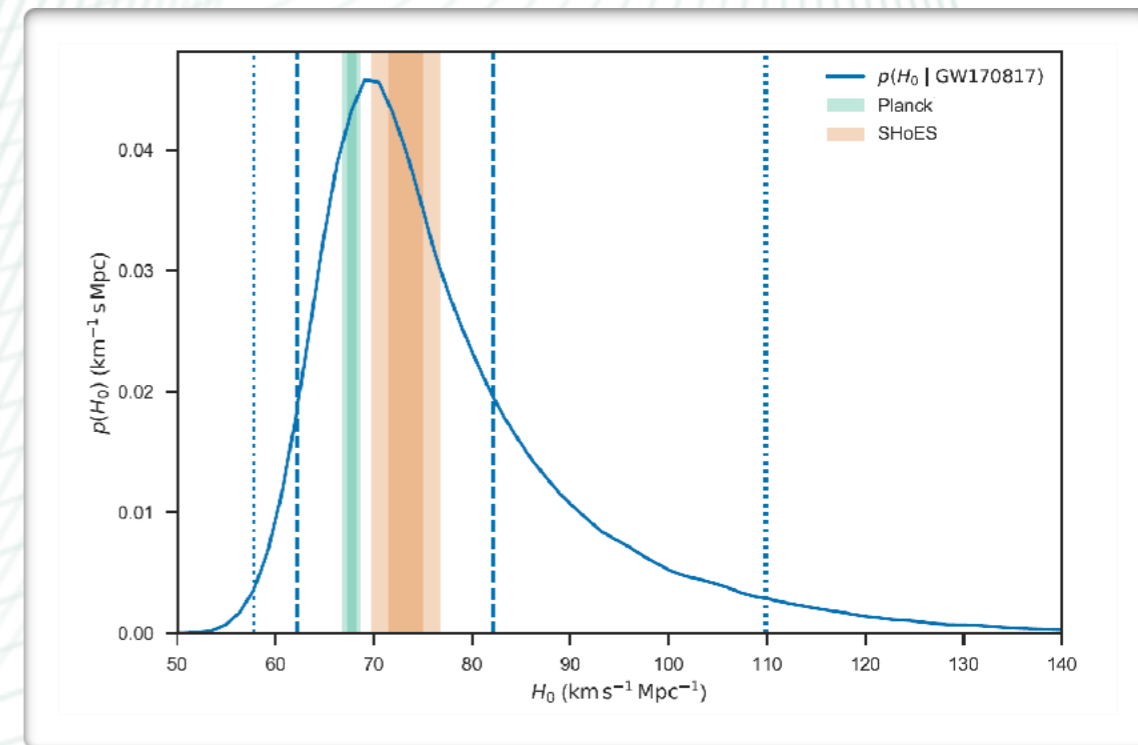
- * distance 88 - 230 Mpc

- * observed by L, V
without EM counterpart

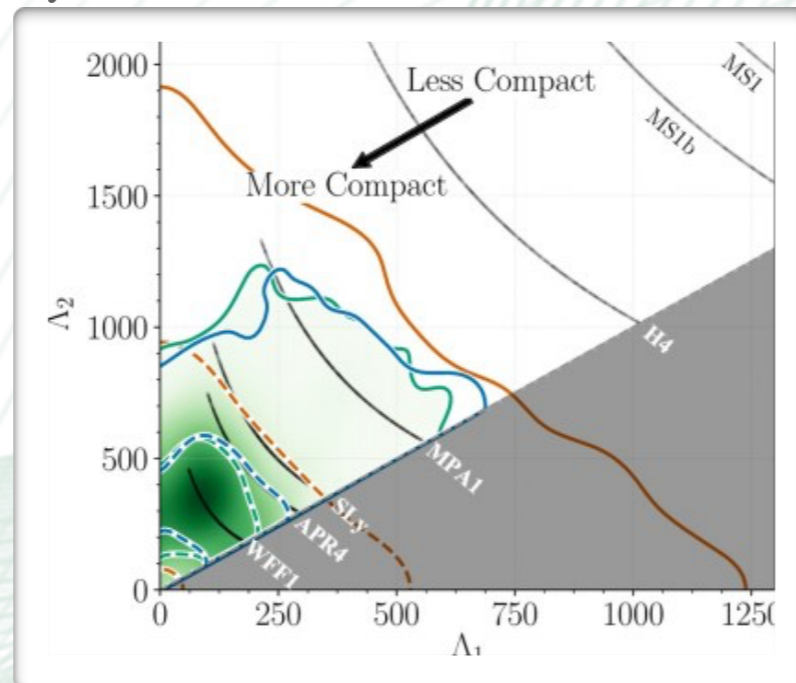
What can we learn from binary neutron star mergers



Determination of the Hubble constant



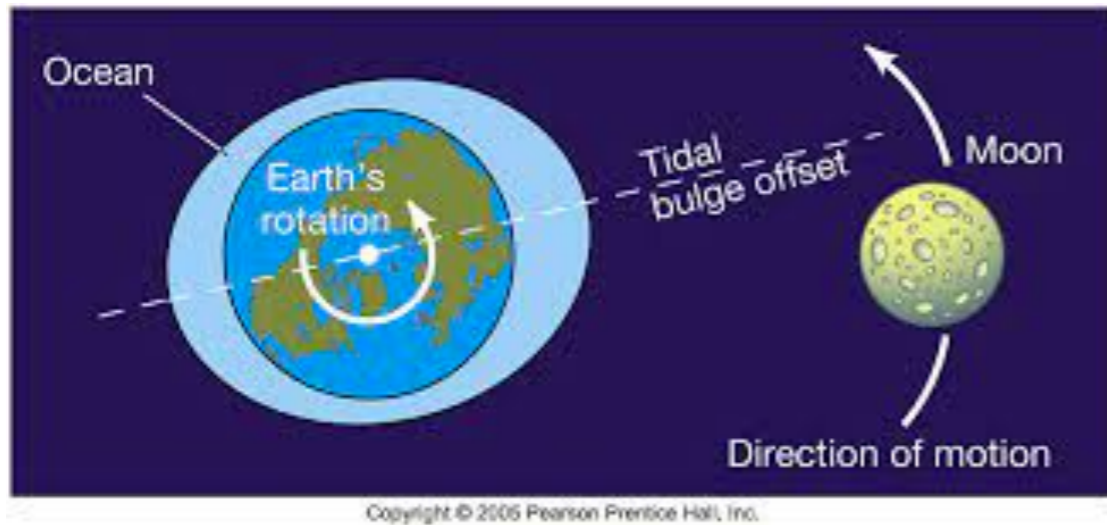
Formation of heavy elements



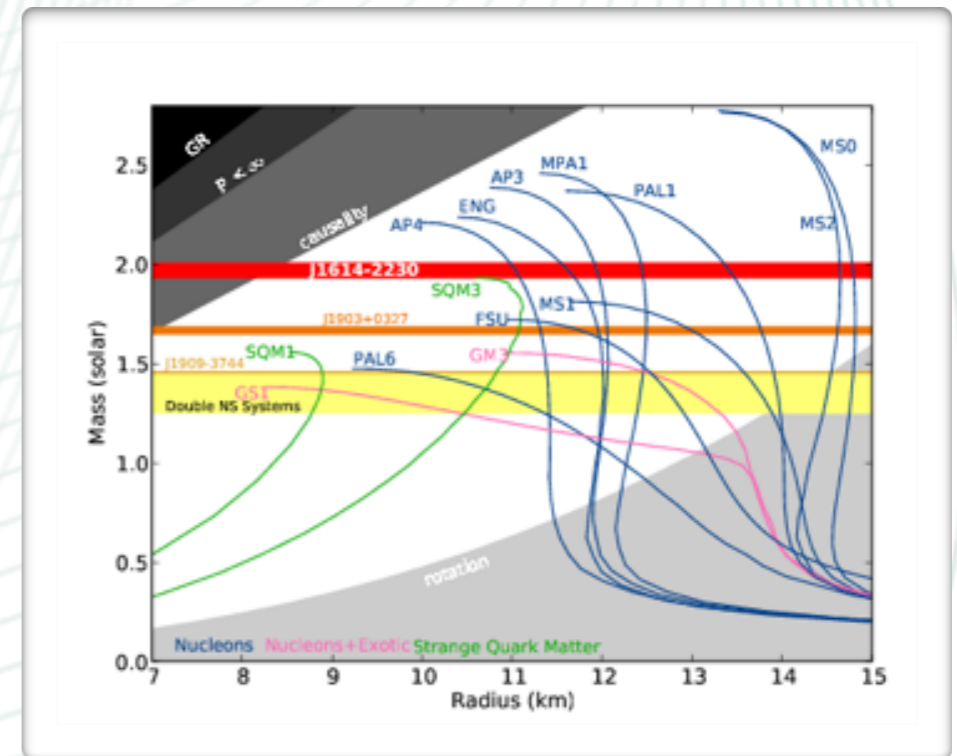
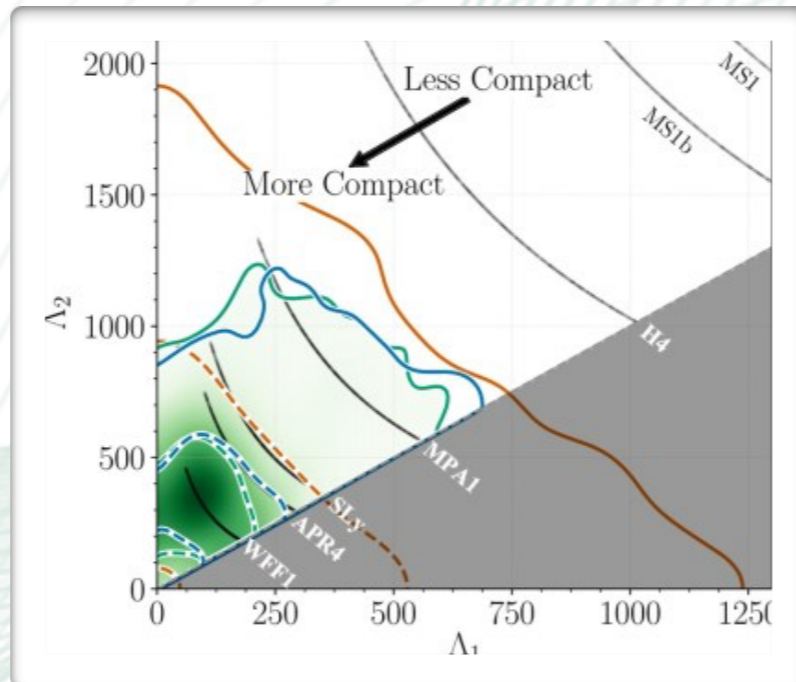
Neutron star equation of state

Neutron star equation of state

tidal forces



Tidal deformability causes the neutron stars to merge sooner



Less compact stars have larger radii and are easier to deform

Determining the Hubble constant

measured
unknown

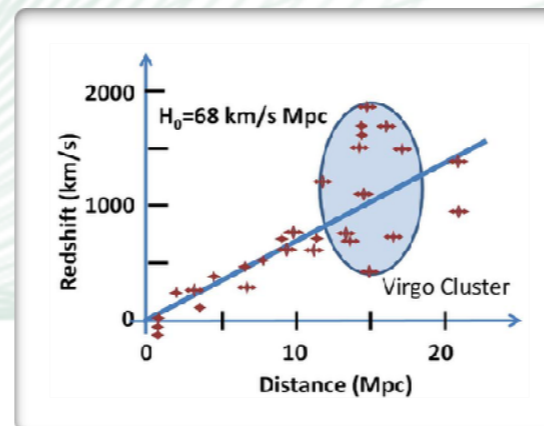
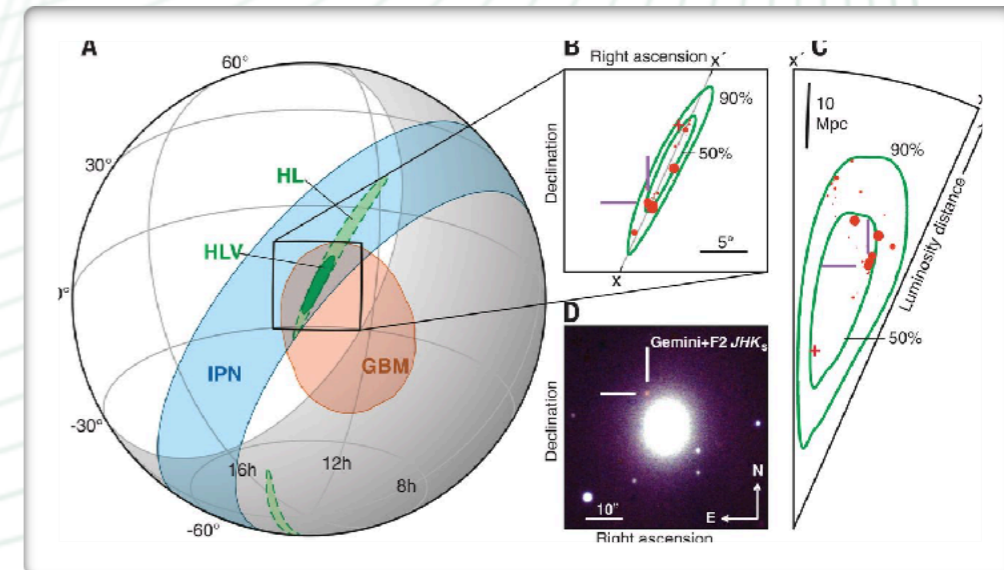
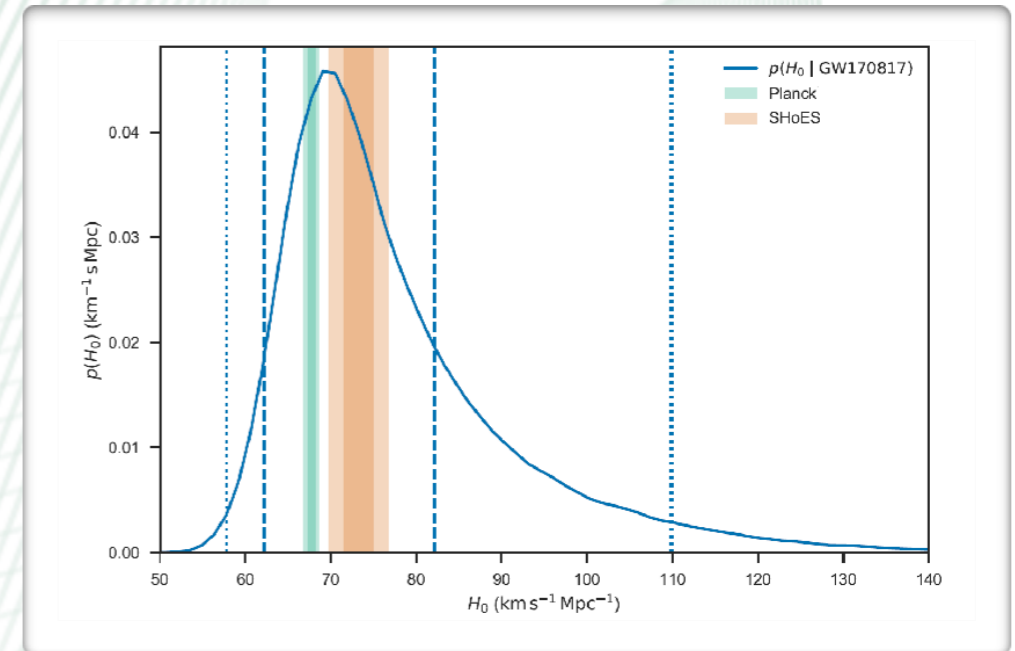
* Chirp mass $\mathcal{M} = \frac{(m_1 m_2)^{3/5}}{(m_1 + m_2)^{1/5}}$

* Amplitude $A \propto \frac{\mathcal{M}^{5/3}}{D_L} F(\cos(i))$
 inclination angle

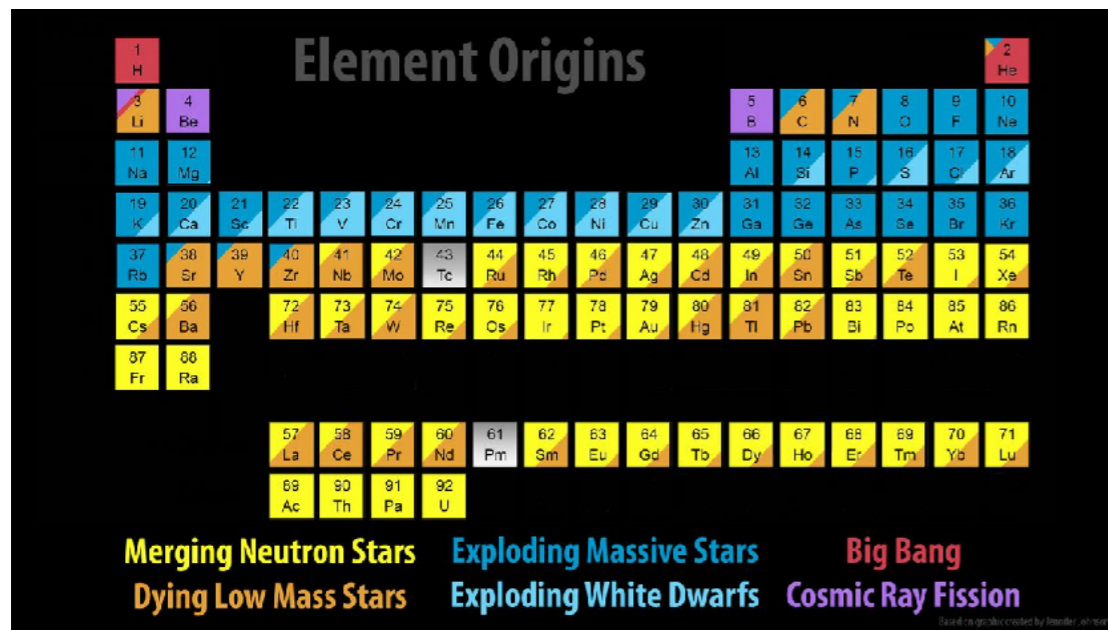
* Frequency $f \propto \mathcal{M}^{5/3} f^{11/3}$

* Luminosity distance D_L + sky localization allow us to obtain the redshift z

Hubble's law: $z \approx \frac{H_0 D_L}{c}$



Formation of heavy elements



GW170817 produced 200* times the mass of the Earth in gold!

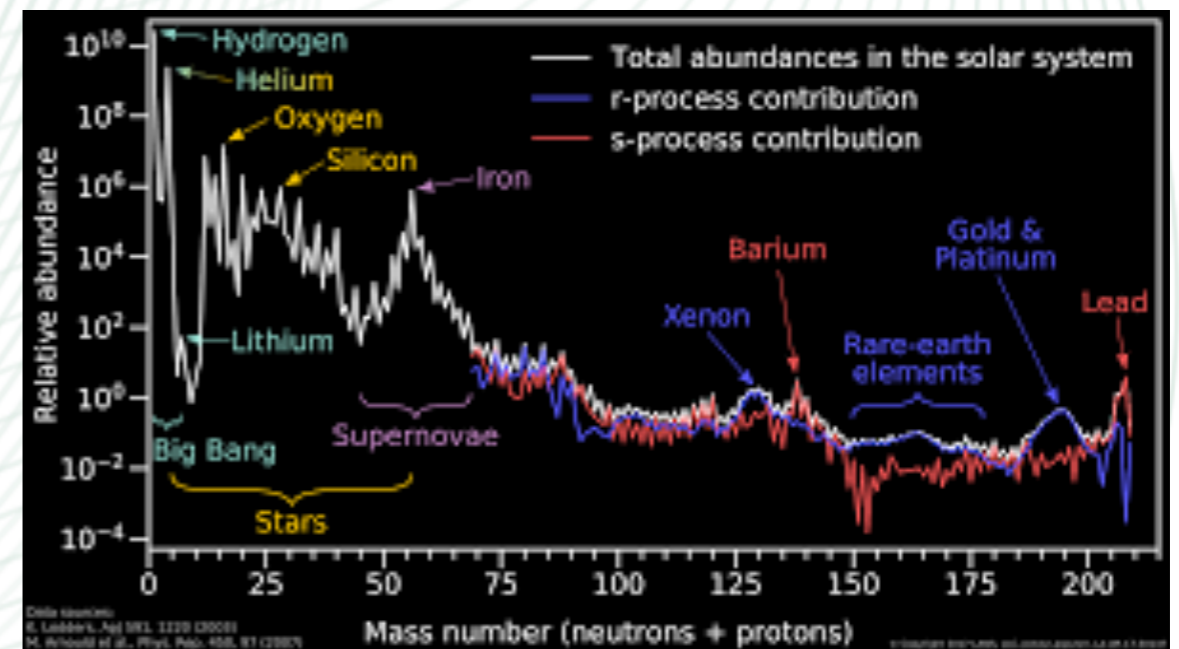
Where do the r-process elements come from?

Supernovae

Neutron star mergers

More frequent
Less mass

Less frequent
More mass



* according to models

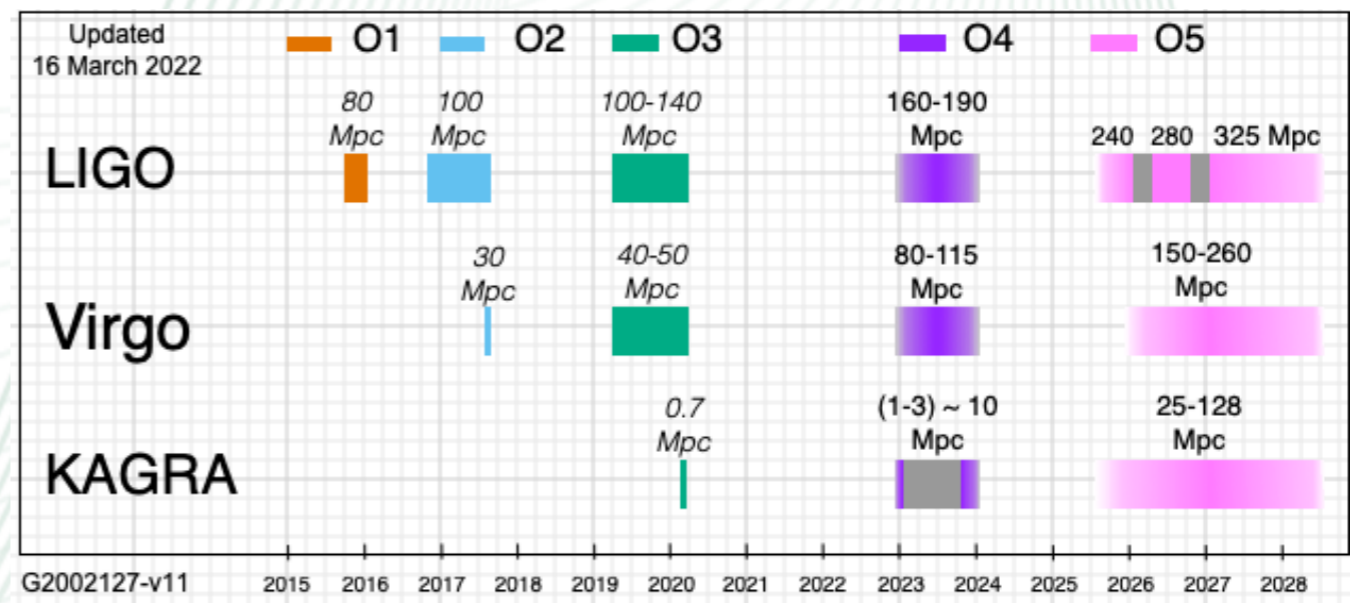
Future Timeline for Gravitational Wave Detectors

* LIGO: O₄ (planned start in mid-December 2022) and beyond

* 3G ground detectors: estimated operation in mid-2030's

* Space detector LISA: estimated launch 2037

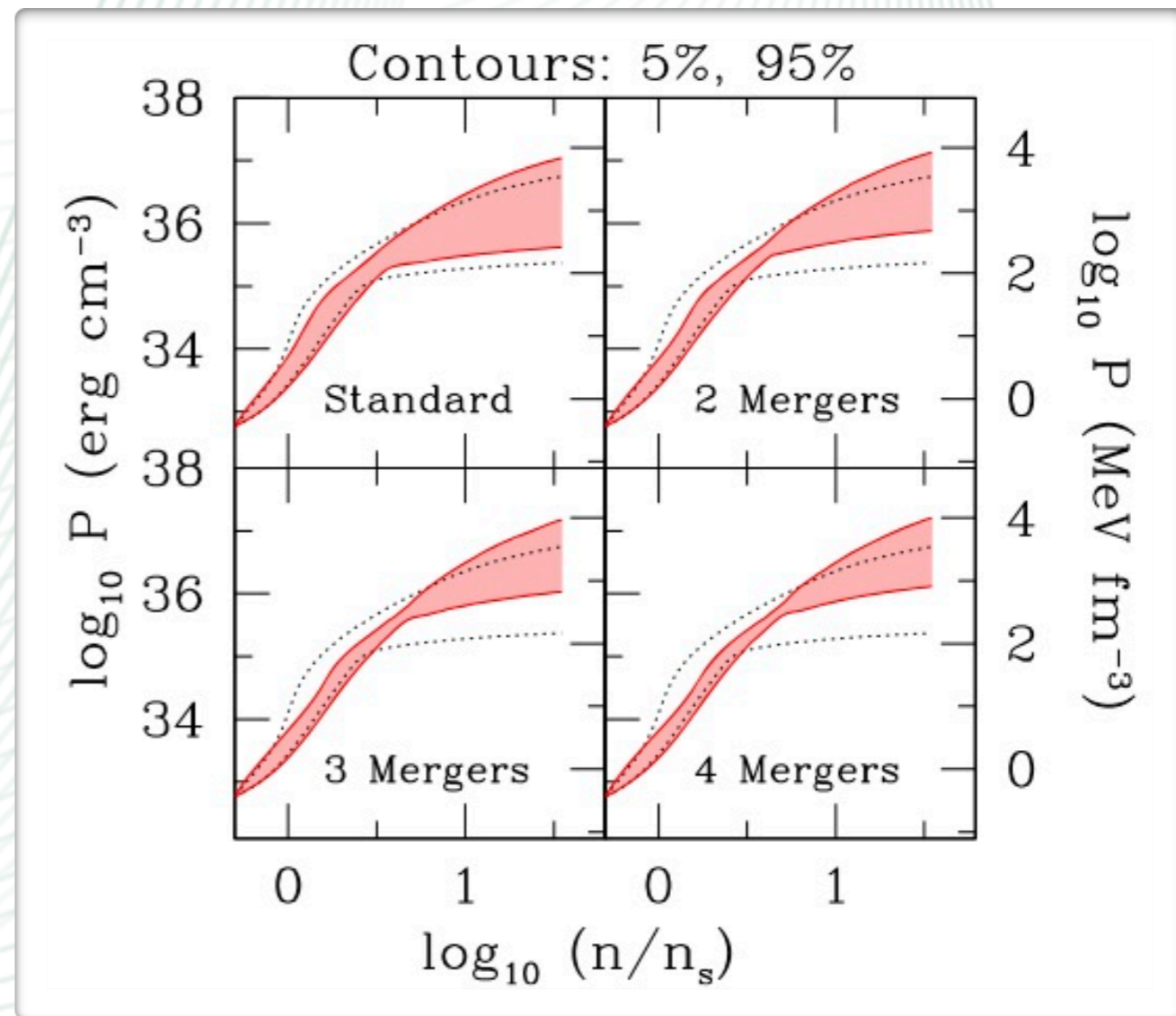
[<https://sci.esa.int/web/lisa/-/61367-mission-summary>]



↓
pandemic starts
delays ensue

LIGO: O4 and beyond

- * What can we gain from more detections: e.g. improvements on **tidal deformability constraints**
- * More stringent upper limits
 - * **continuous waves**
 - * stochastic background
- * If really lucky:
 - * galactic magnetar/supernova



[Miller, Chirenti & Lamb, 2020]

LIGO: O4 and beyond

Continuous Waves

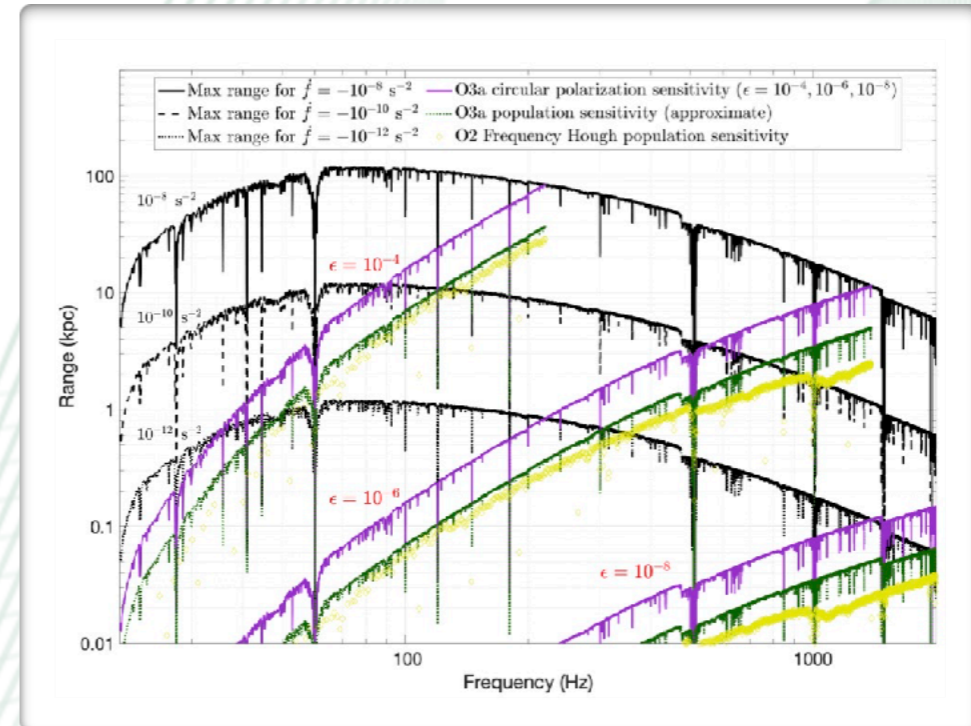
NS with a
“mountain”



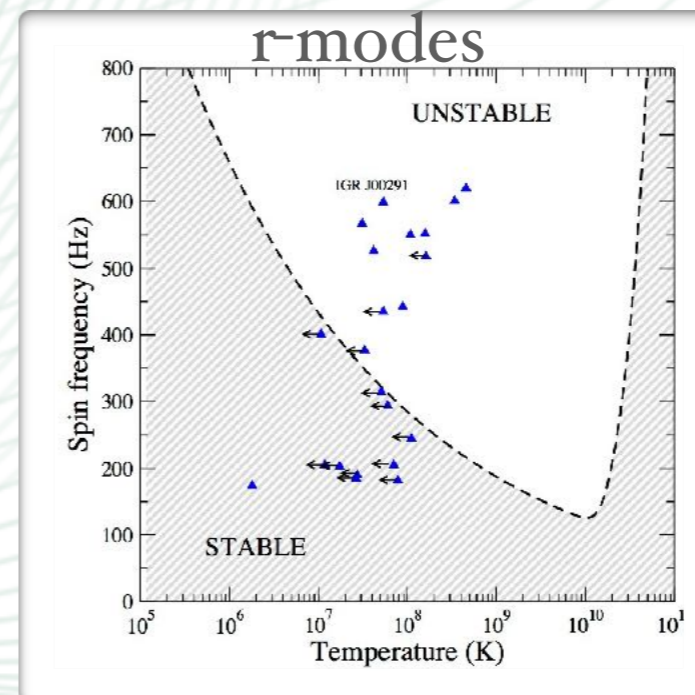
[Saint-Exupéry, 1943]

- * upper limits on the gravitational wave emission limit the ellipticity of the NS
- * the stronger the crust, the higher the mountain it can support
- * the highest height of the NS “mountain” could be < 1 mm!

[Horowitz & Kadau, 2009; Gittins & Andersson, 2021]



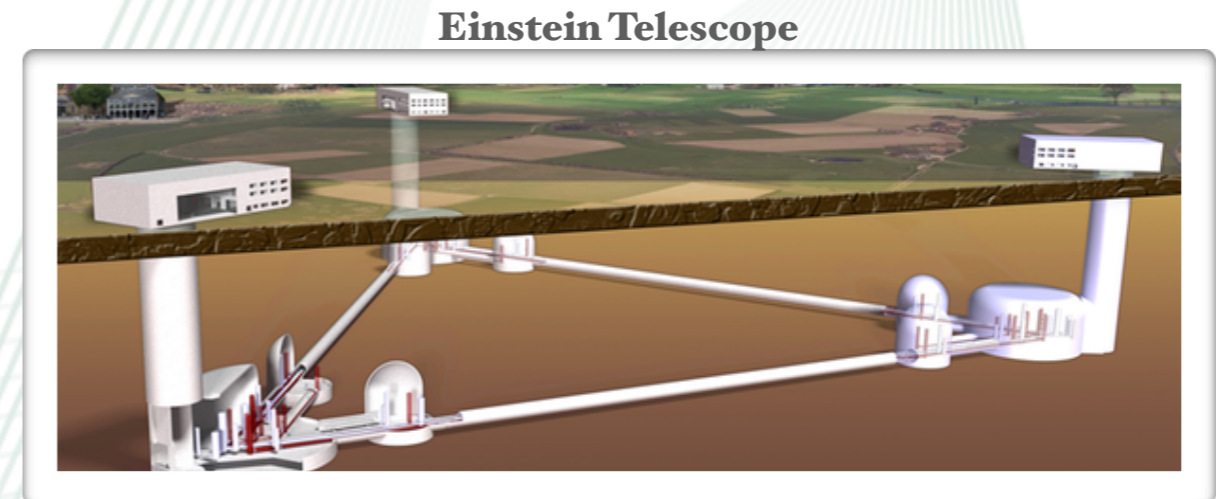
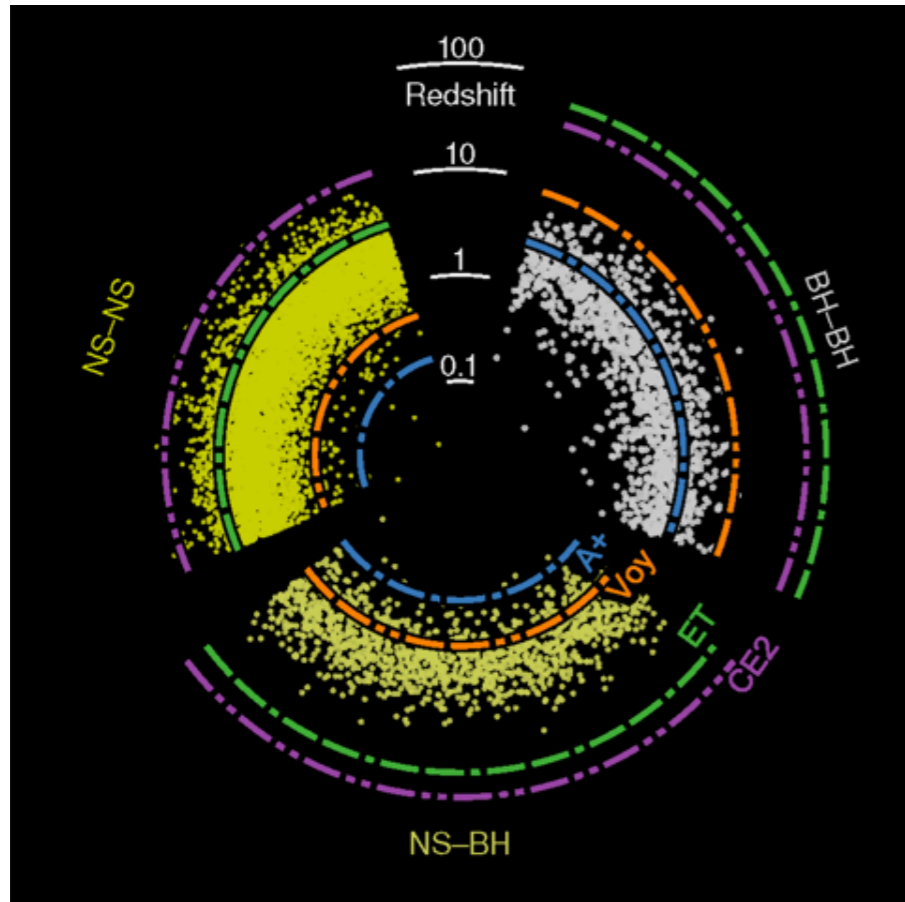
[LIGO, Virgo, KAGRA, 2021]



[Haskell, Degenaar & Ho, 2012]

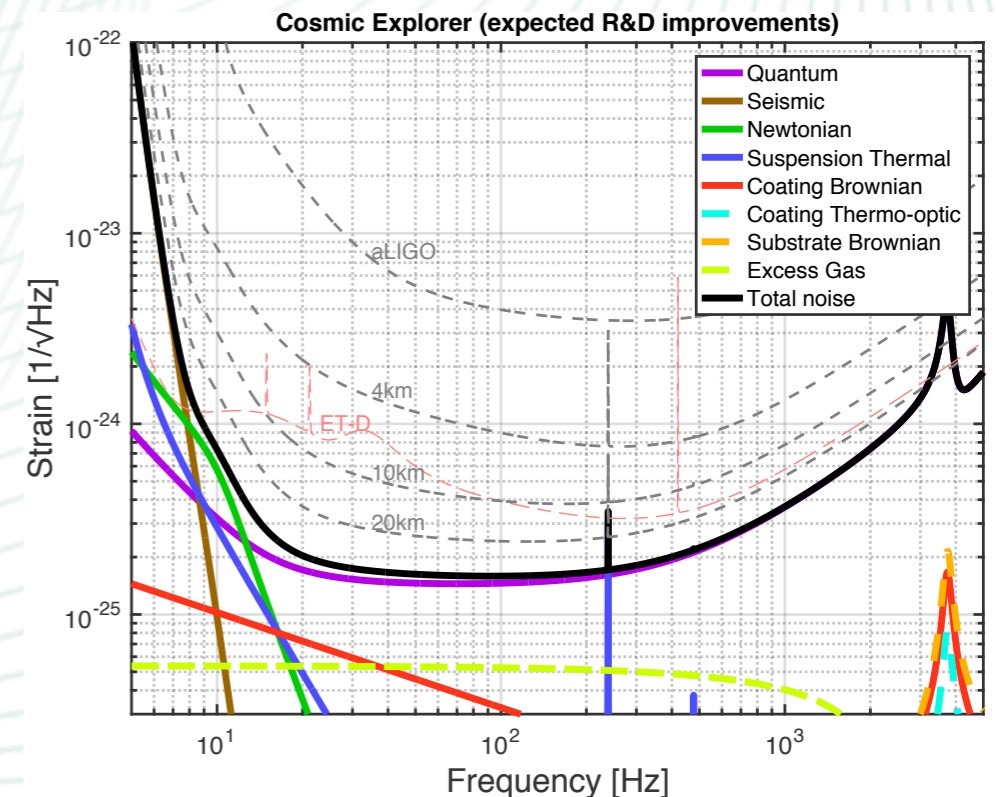
Shape of the instability window depends on NS bulk and shear viscosities

3G: Einstein Telescope/Cosmic Explorer



Einstein Telescope

- ◆ ET: 10 km (underground), could detect NS-NS mergers up to $z \sim 2 - 3$
- ◆ CE: 40 km, could detect **all** NS-NS mergers (up to $z \sim 6$)



[Abbott et al., 2017]

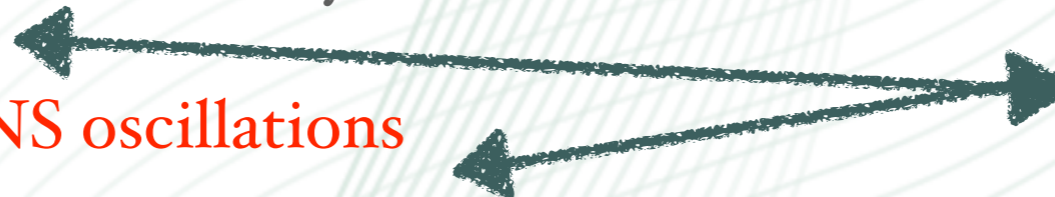
3G Detectors: ET/CE

- * Low frequency sensitivity
 - * Advance warning for EM counterparts



better kilonova observations

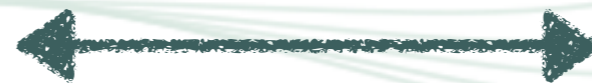
- * High frequency sensitivity
 - * pre-merger: tidal deformability and **dynamical tides**
 - * post-merger: **HMNS oscillations**



Neutron star asteroseismology!

- * Overall improved sensitivity
 - * better upper limits (maybe detections?)

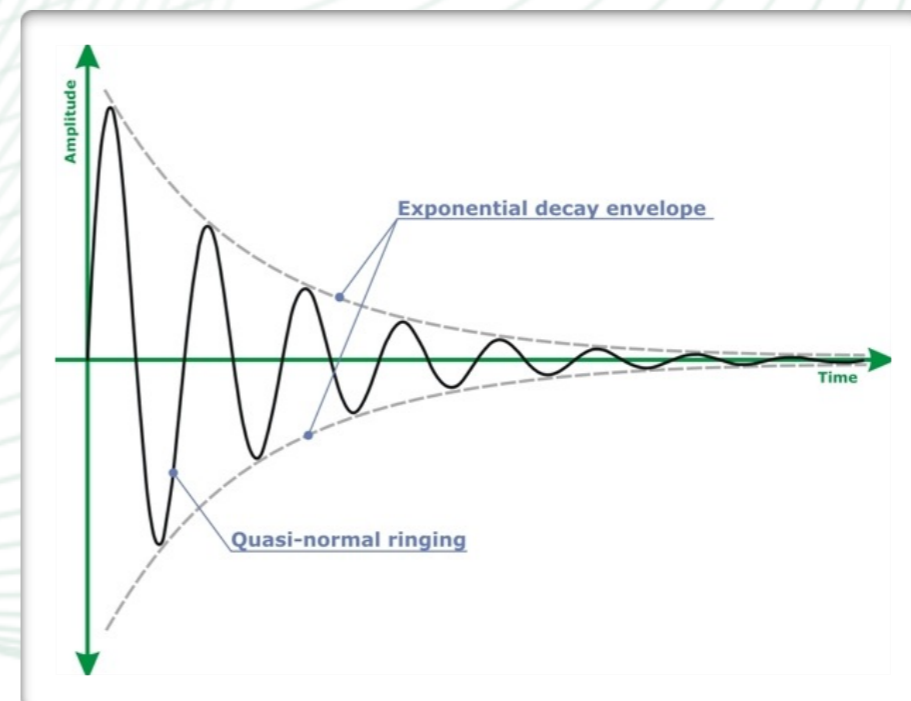
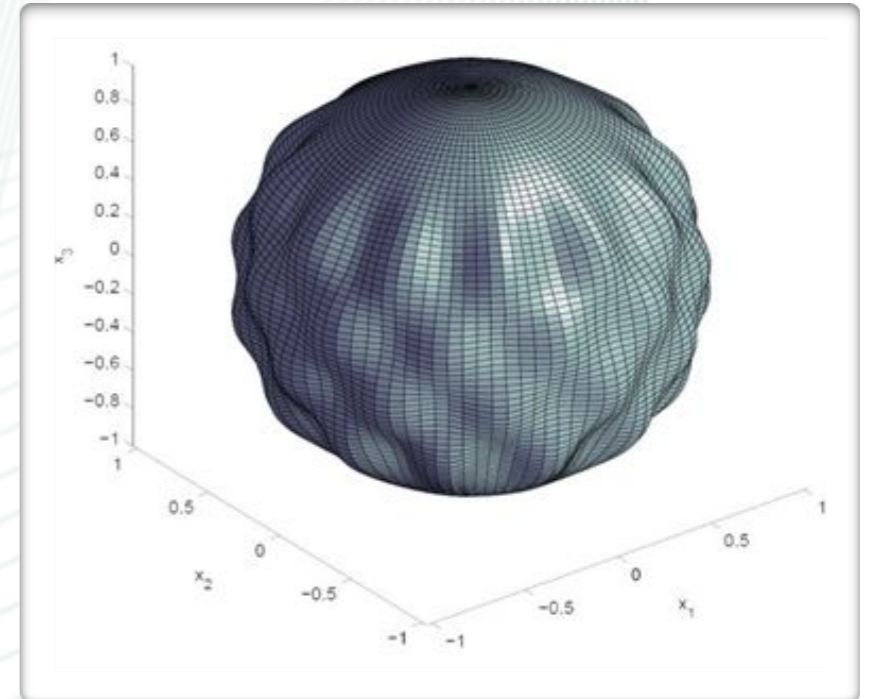
- * If really lucky:
 - * galactic **magnetar/supernova**



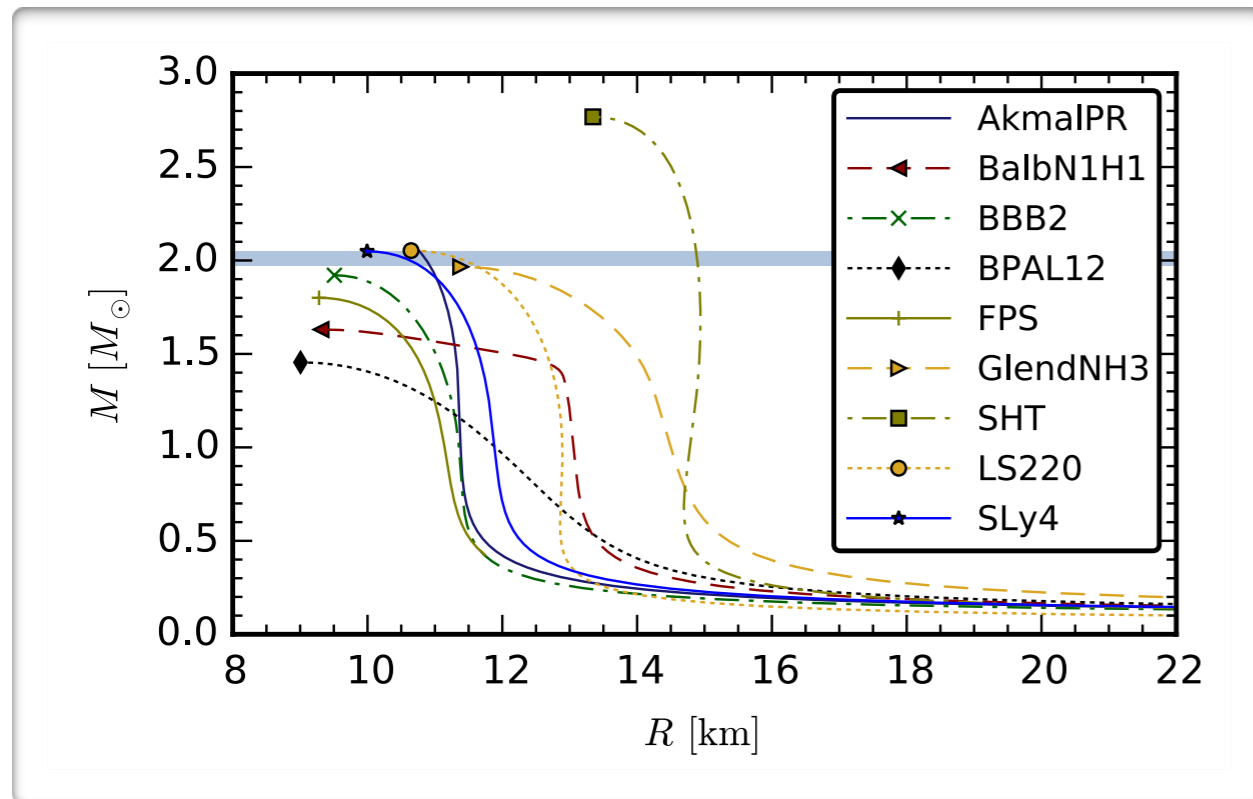
more multimessenger observations!

Neutron Star Asteroseismology (Quasinormal mode frequencies)

- * Oscillation modes of the fluid coupled to the emission of gravitational waves
- * Different families of modes \leftrightarrow different restoring forces
- * For non-rotating (and non-magnetized) stars
 - * f-modes (fundamental)
 - * p-modes (pressure)
 - * g-modes (gravity)
 - * w-modes (spacetime modes), etc



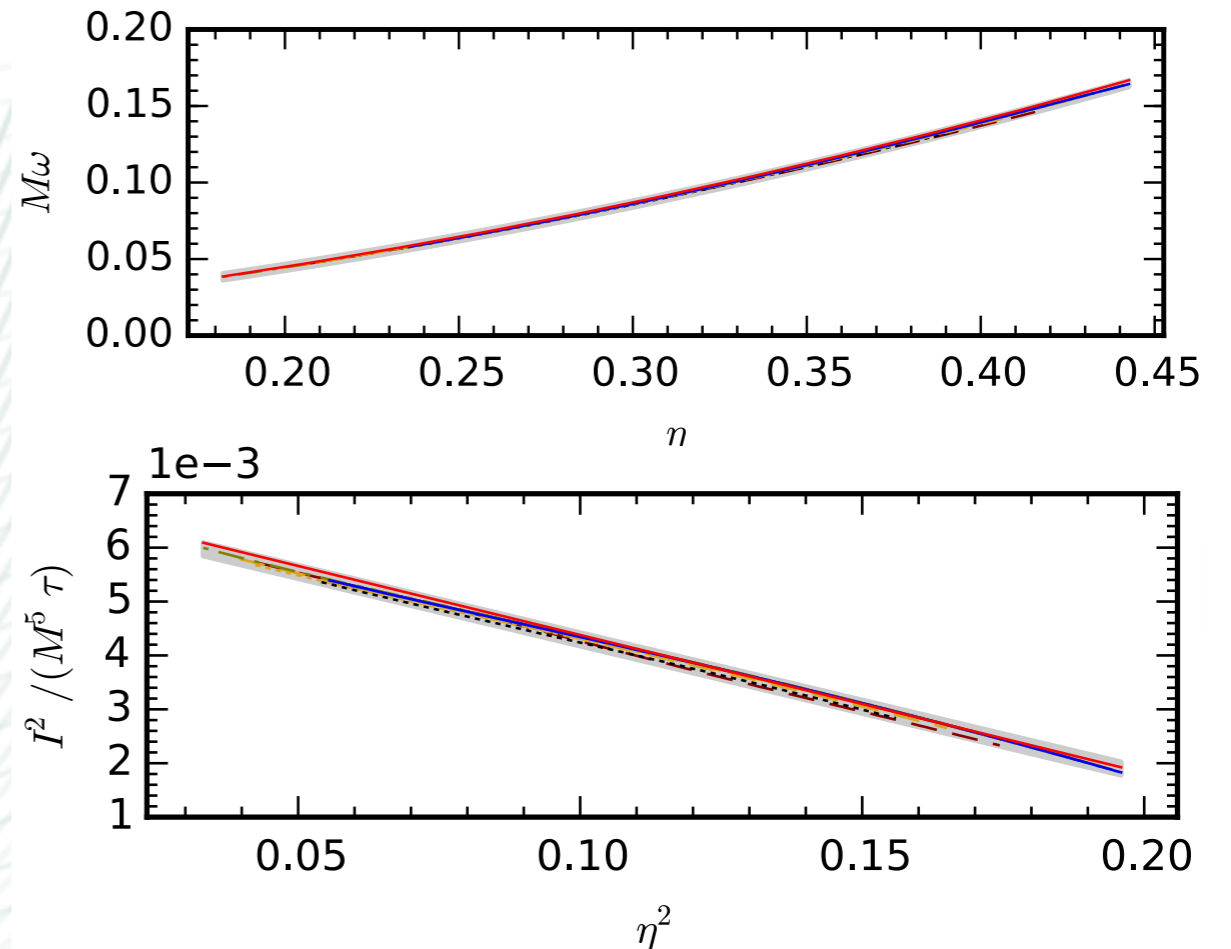
What can we learn from QNMs? Example: Universal relations and the inverse problem



We can use EOS-independent information to learn about the EOS

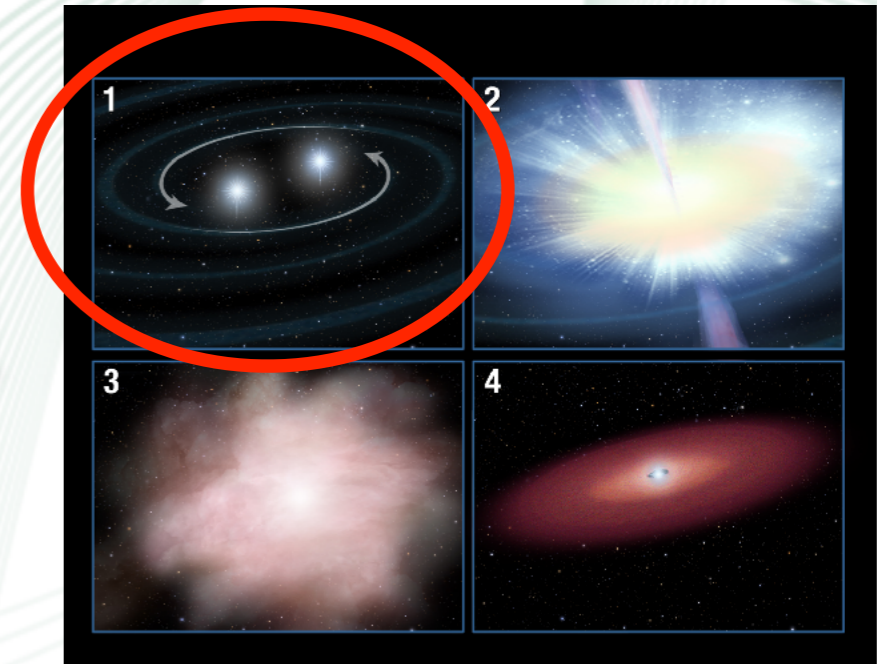
See also: [Andersson & Kokkotas, 1998; Benhar, Ferrari & Gualtieri, 2004; Lau, Leung & Lin, 2010; Maselli et al. 2013; Sotani & Kumar, 2021, ...]

f-modes



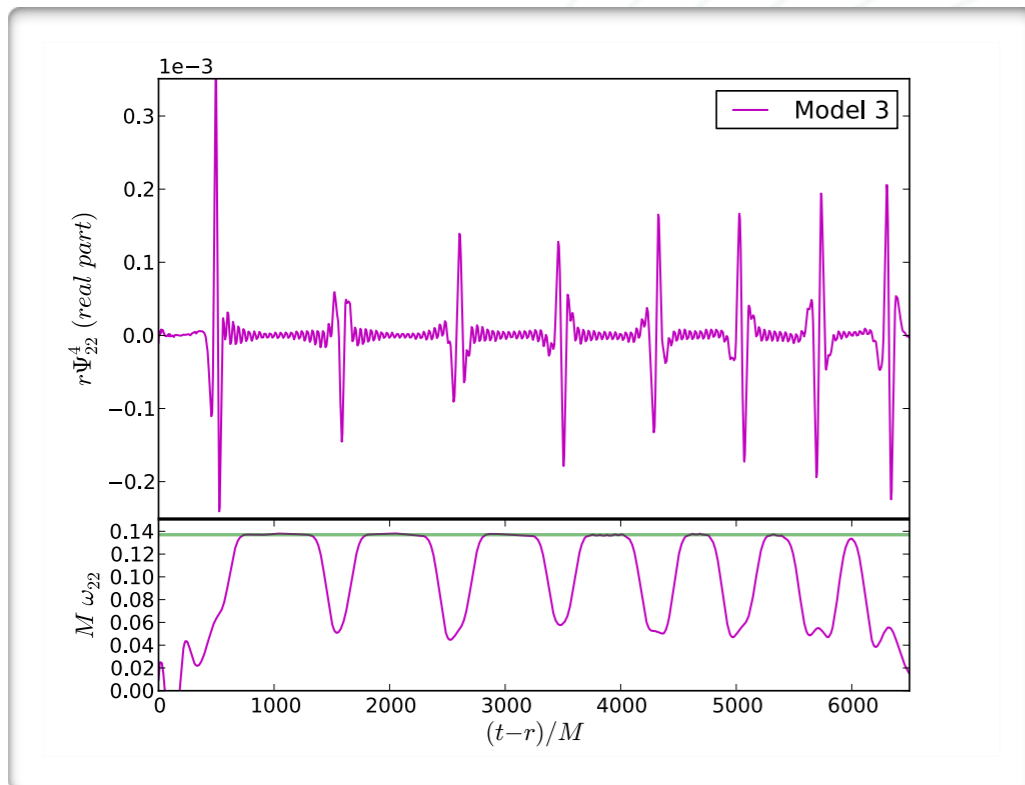
Effective compactness: $\eta \equiv \sqrt{M^3/I}$
[Chirenti, de Sousa & Kastaun, 2015]

Pre-merger: Oscillations in the inspiral

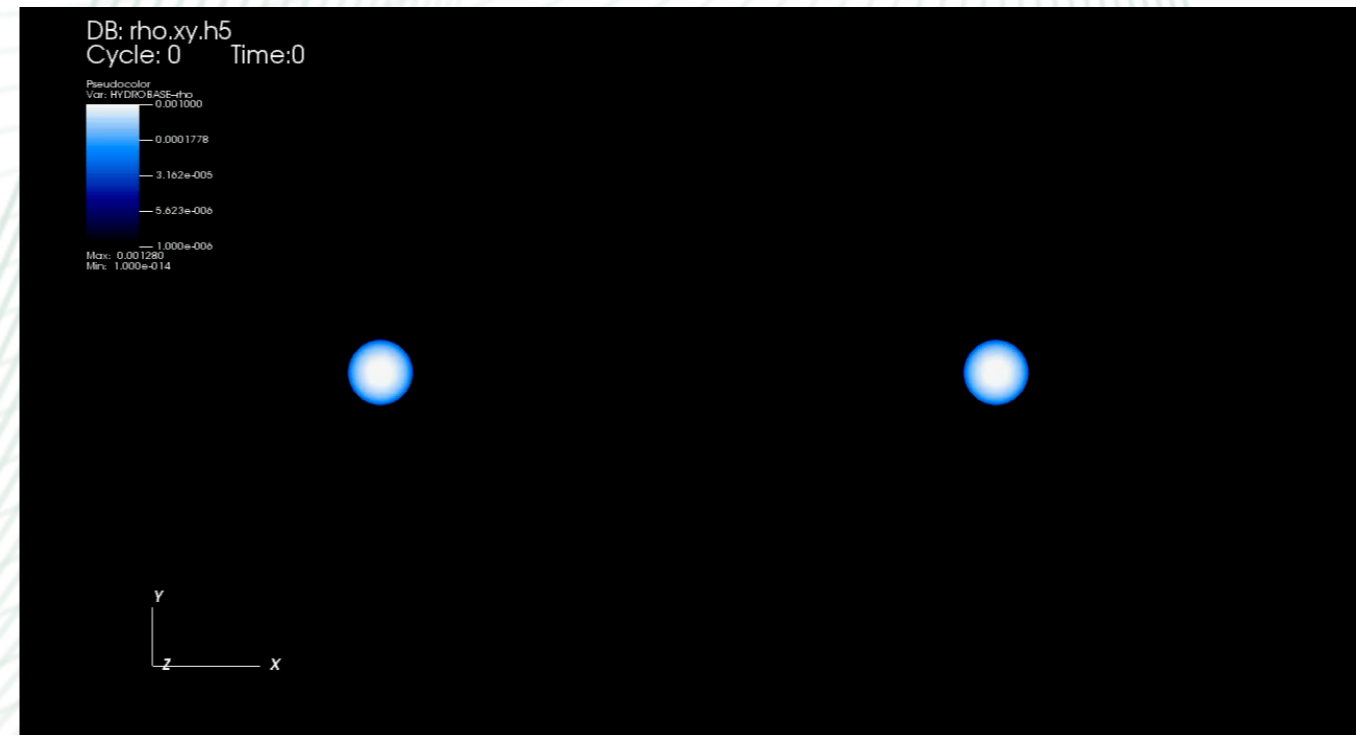


Tidal excitation of f-modes in eccentric binaries could be detectable with 3G!

[Chirenti, Gold & Miller, 2017]



[Gold et al., 2012]

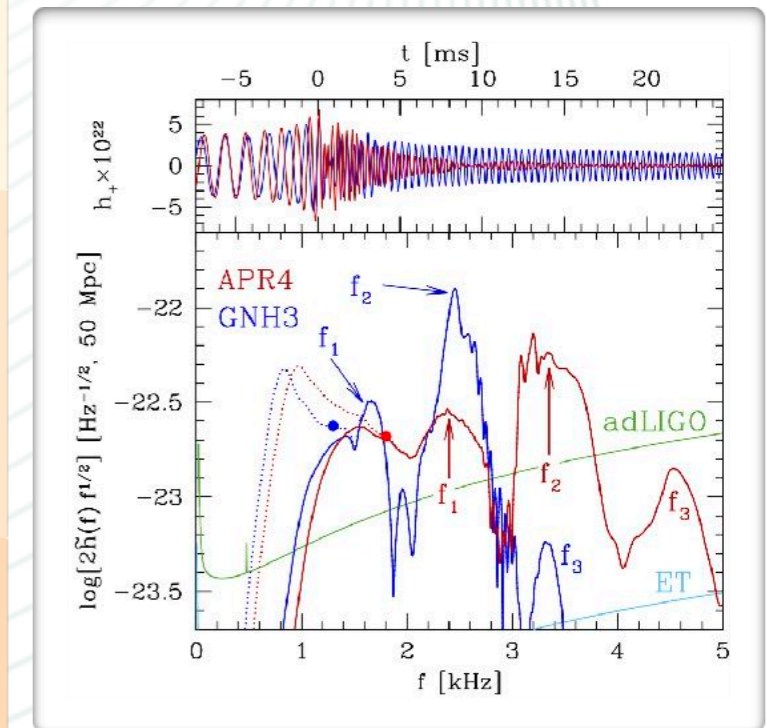
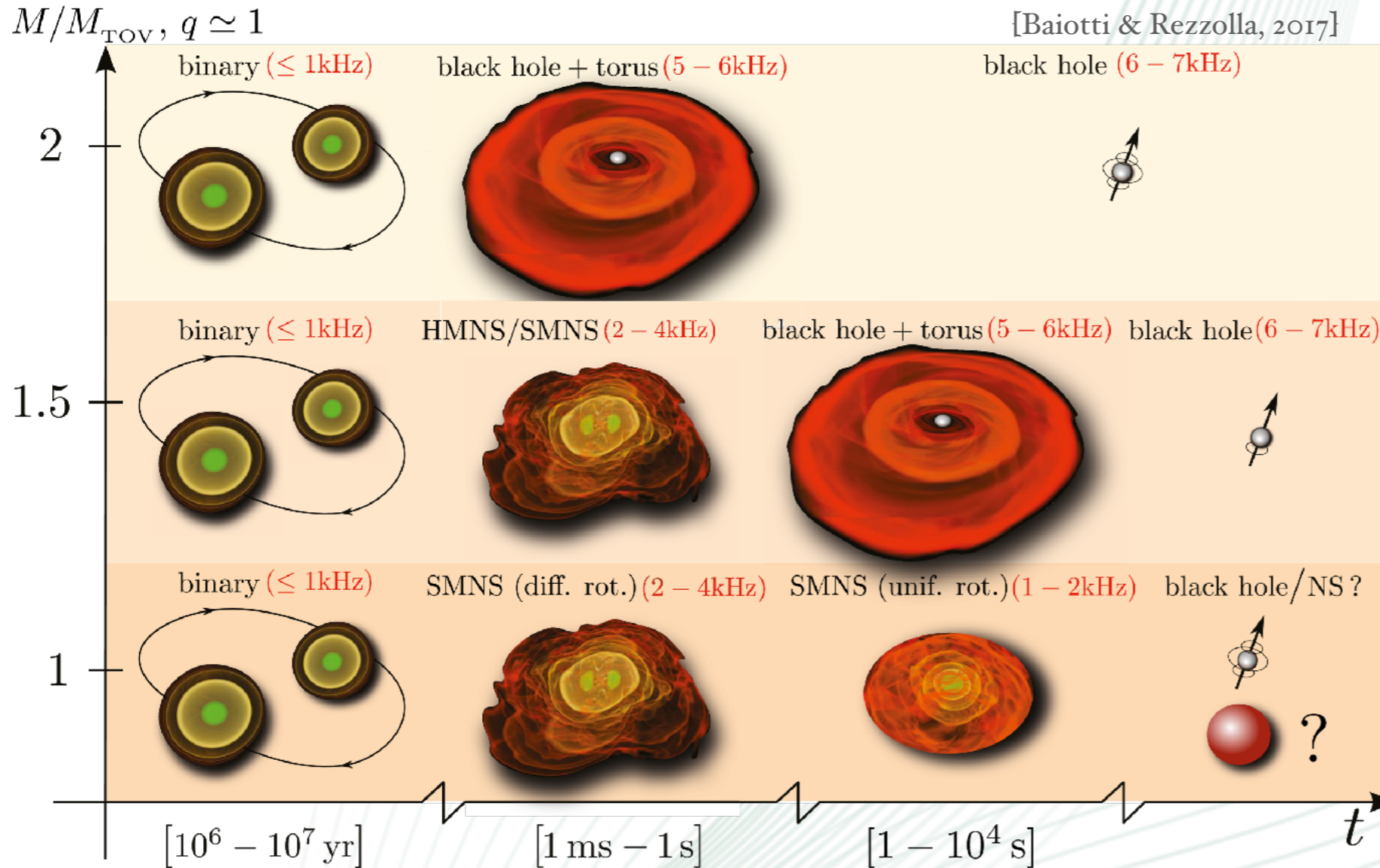
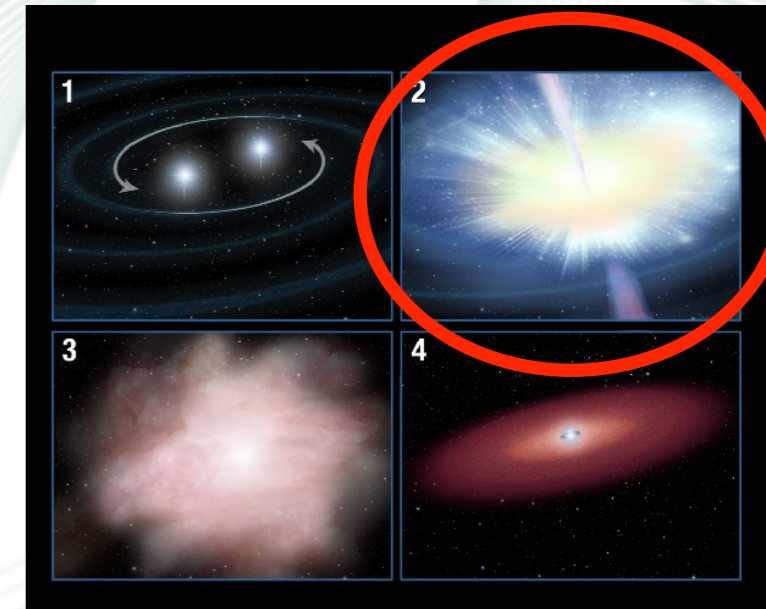


[Simulation by Shawn Rosofsky]

f-modes could also be detectable in the very late stages of circular binaries

[Schmidt & Hinderer, 2019]

Post-merger: HMNS oscillations

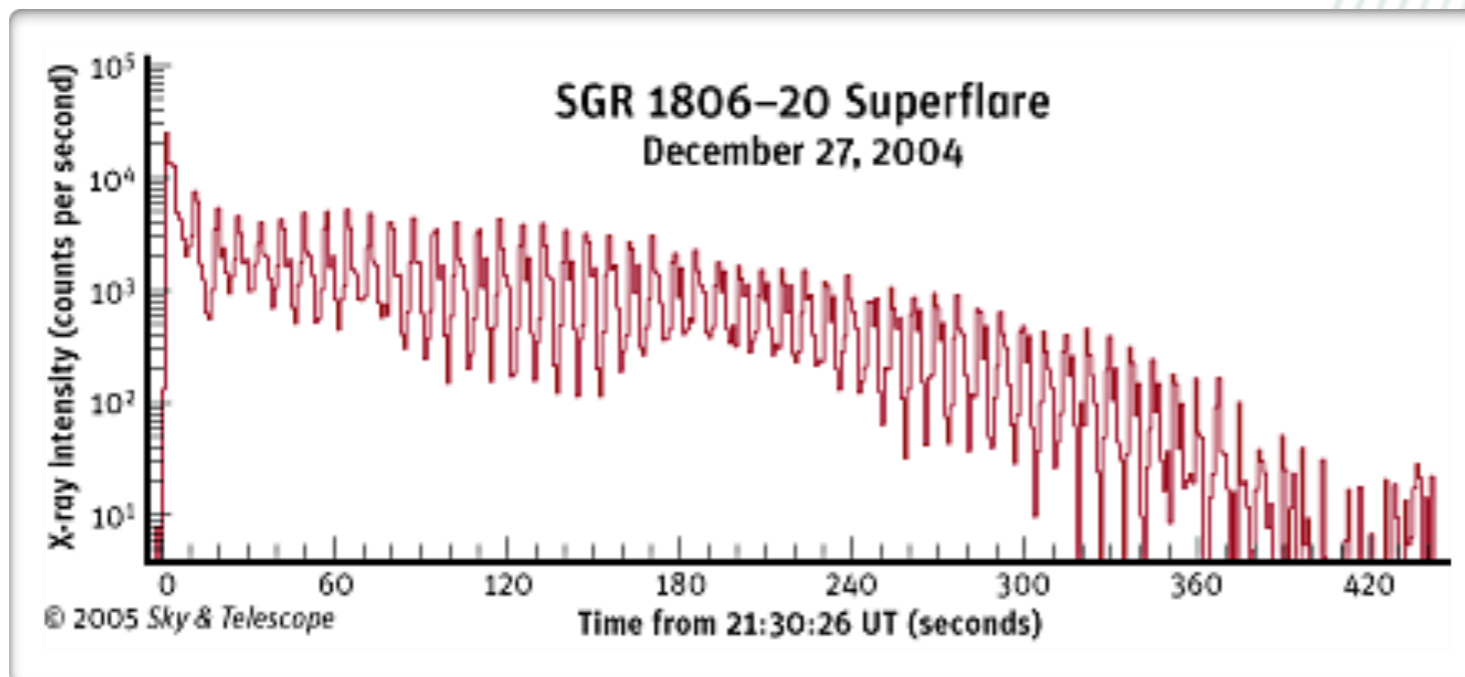


[Takami, Rezzolla & Baiotti, 2014]

Frequencies carry information on the hot EOS.
Oscillations may modulate the SGRB signal.
[Chirenti et al., 2019]

Universal relations
for HMNSs?
[Bauswein et al., 2012; Lioutas,
Bauswein & Stergioulas, 2021]

Galactic observations: Magnetar giant flares



Gravitational waves from
galactic magnetar giant flares
may be detectable.

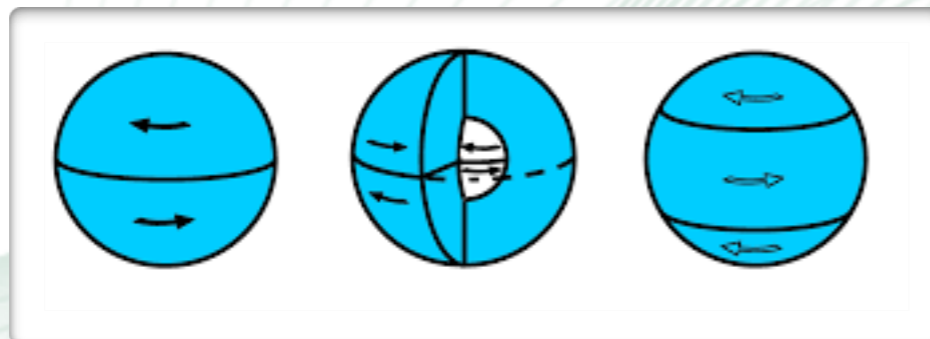
[Zink, Lasky & Kokkotas, 2012]

* 18, 26, 29, 92.5, 150, 625.5 and 1837 Hz

[Israel et al, 2005; Watts & Strohmayer, 2006; Strohmayer & Watts, 2006, Miller et al, 2019]

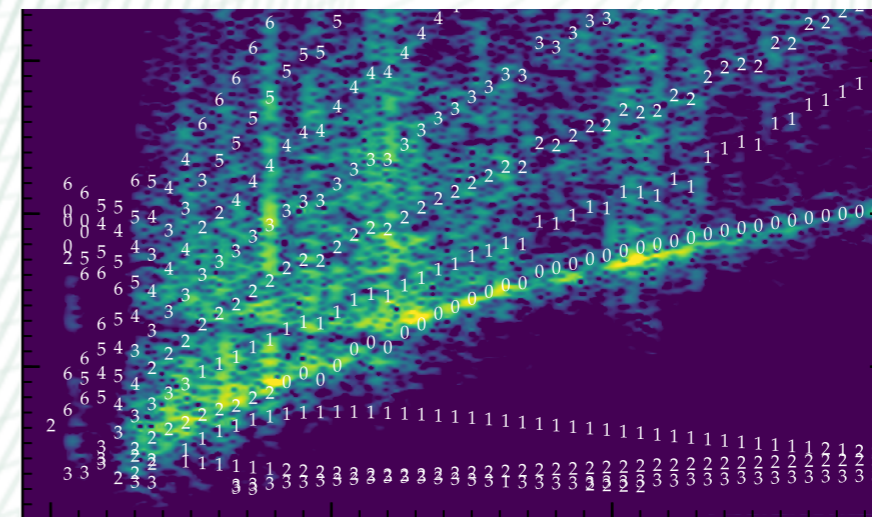
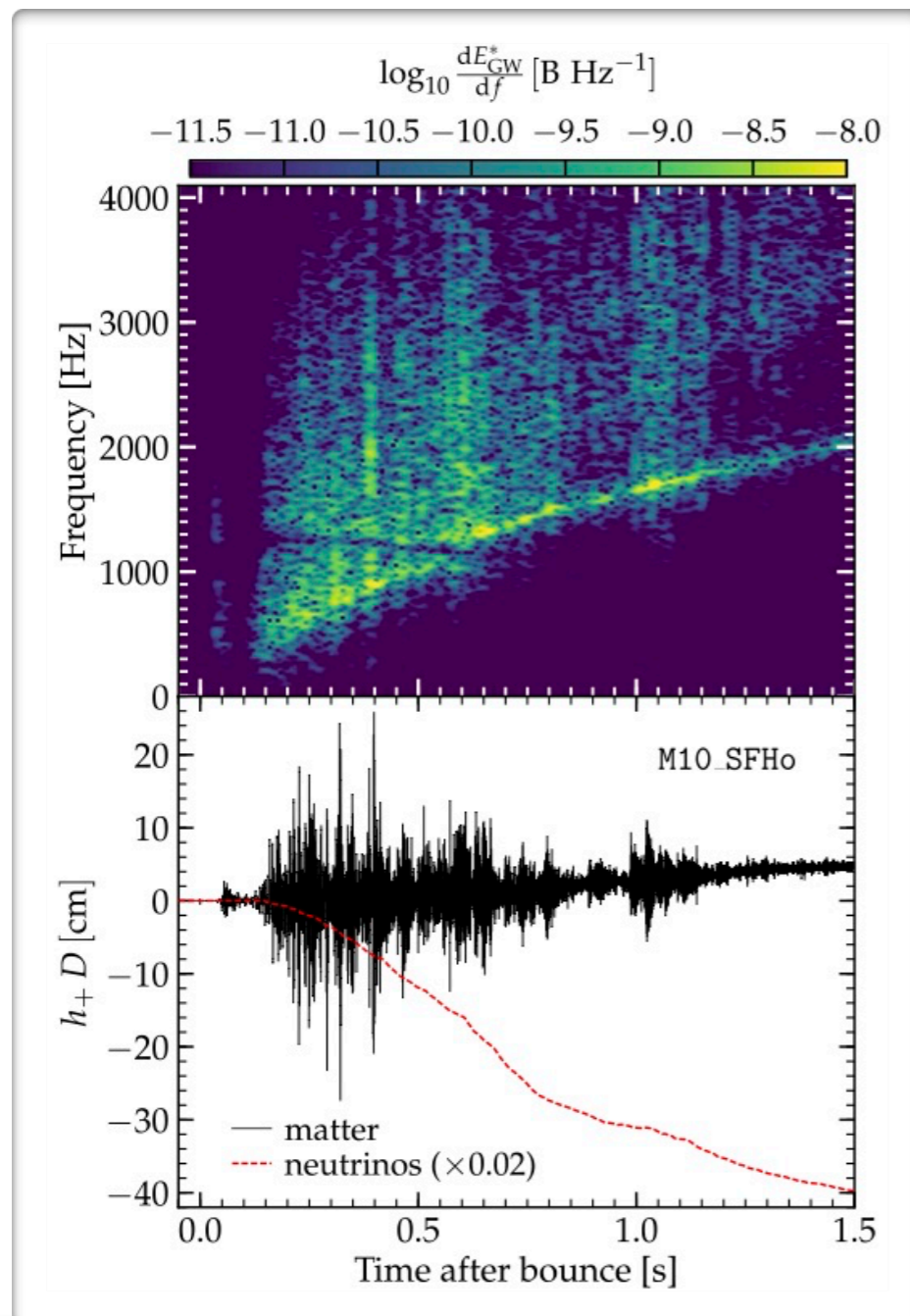
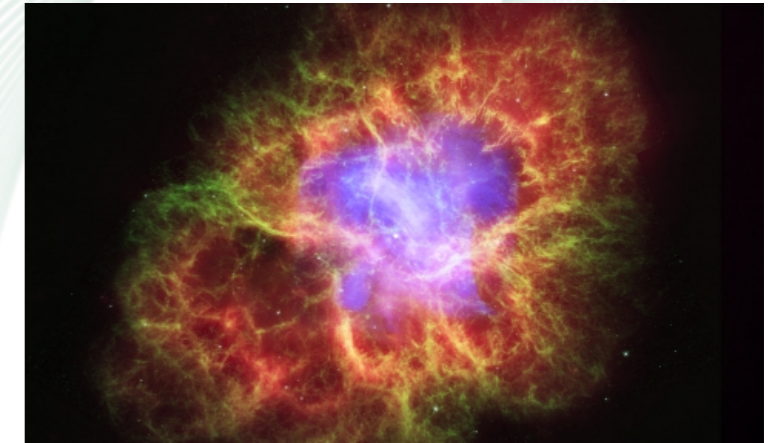
Rare events - or not?

[Burns et al, 2021]



Torsional crustal modes?

Galactic observations: Core Collapse Supernovae



Signal is templatable and can be described by the quasinormal modes of the proto neutron star!

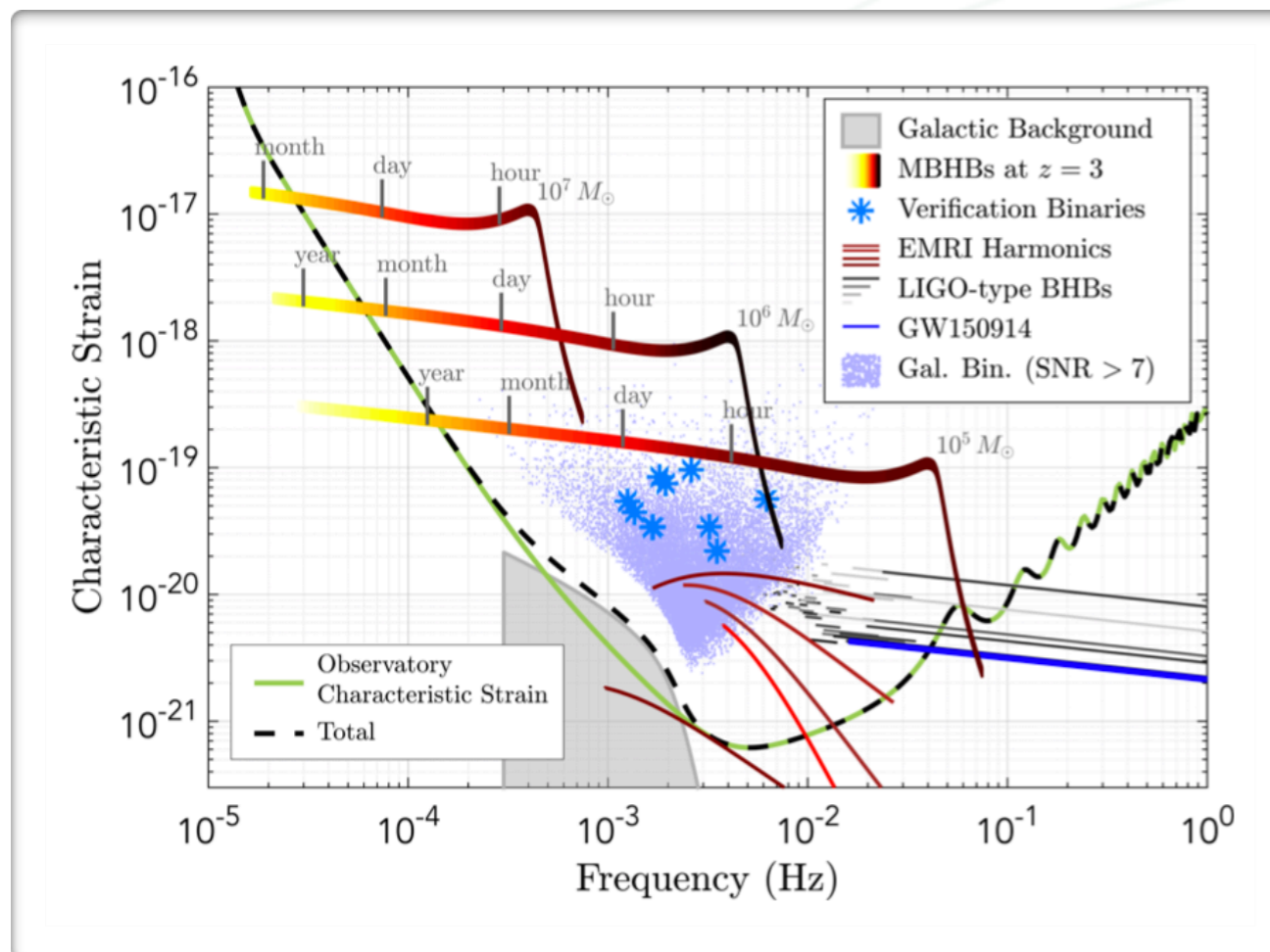
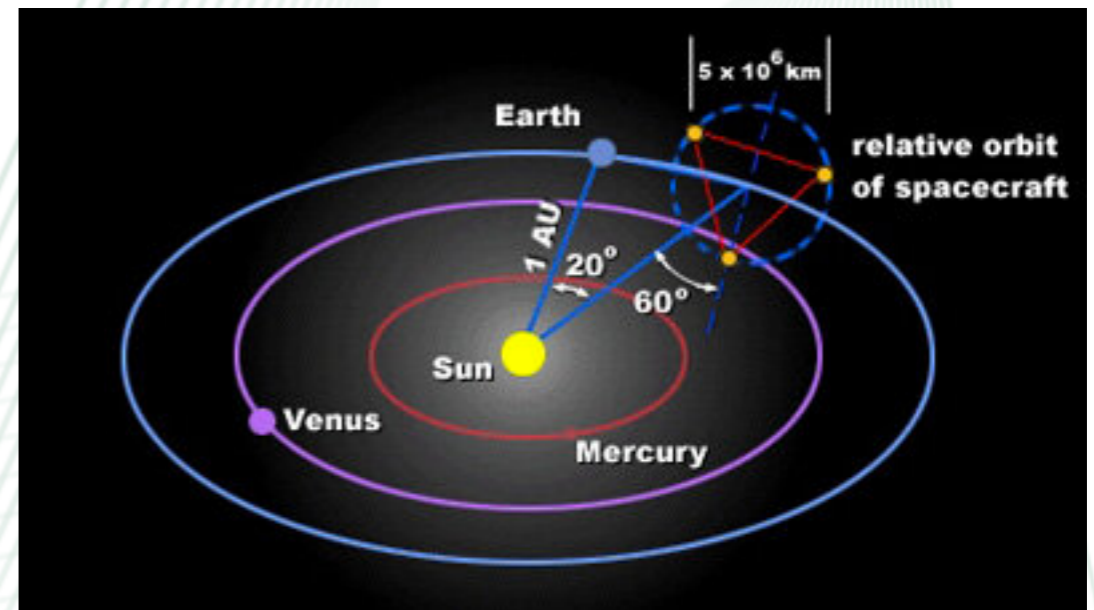
Universal relations for PNSs?

[Morozova et al, 2018]

[Torres-Forné et al, 2019]

LISA

LISA will be able to see supermassive black hole binaries, and early stages (larger separations) of stellar mass black hole binaries



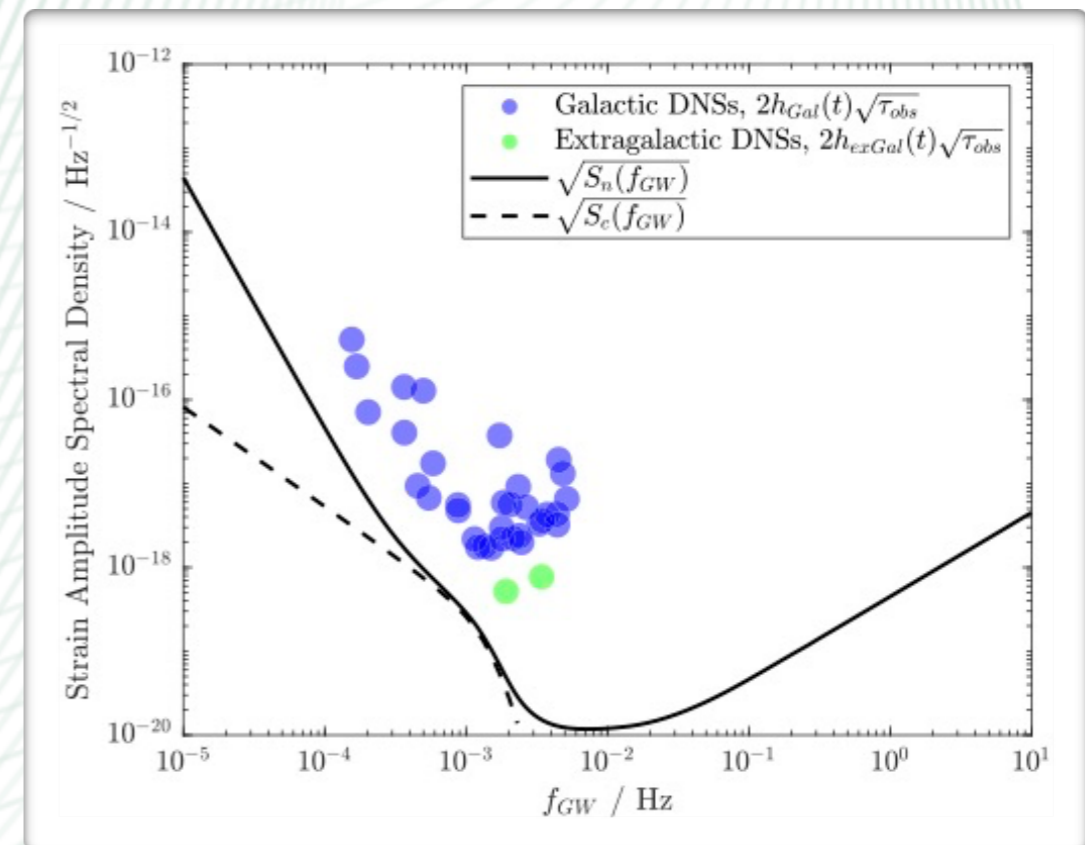
[Amaro-Seoane et al., 2017]

Sounds great!
And what about neutron stars?
Not obvious.

LISA and Neutron Stars

~ 35 binary neutron stars
should accumulate SNR > 8
during the 4 year LISA mission

At LISA frequencies, many of the
binaries will be eccentric
(expected median eccentricity 0.11)



[Lau et al., 2020]

Determination of orbital properties could
provide information on progenitors,
formation channels and natal kicks

Conclusions and Outlook

- * Future gravitational wave observations can provide important information on the EOS of cold catalyzed matter.
- * In particular, neutron star oscillations can be particularly helpful. But they aren't easy to observe! There are already indications of observations in X-ray data, and maybe also in radio.
- * Gravitational wave observation of neutron star oscillations will require 3G detectors. Oscillations from hypermassive neutron stars can provide information on the hot EOS.
- * LISA observations can help probing formation channels of binary neutron star systems.

References, further reading and videos

- * Jocelyn Bell: The Discovery of Pulsars:
<https://www.youtube.com/watch?v=-335gUOvdhA>
- * What is a pulsar?
https://www.youtube.com/watch?v=gjLk_72V9Bw&t=2s
- * Neutron stars for undergraduates, R. Silbar & S. Reddy
<https://arxiv.org/abs/nucl-th/0309041>
- * Gravity from the Ground Up, B. Schutz
<http://www.gravityfromthegroundup.org>
- * Black Holes, White Dwarfs and Neutron Stars, S. L. Shapiro & S. A. Teukolsky
- * Gravity: an Introduction to Einstein's General Relativity, J. B. Hartle
- * Gravitational Waves, vols. 1 & 2, M. Maggiore

Questions?

