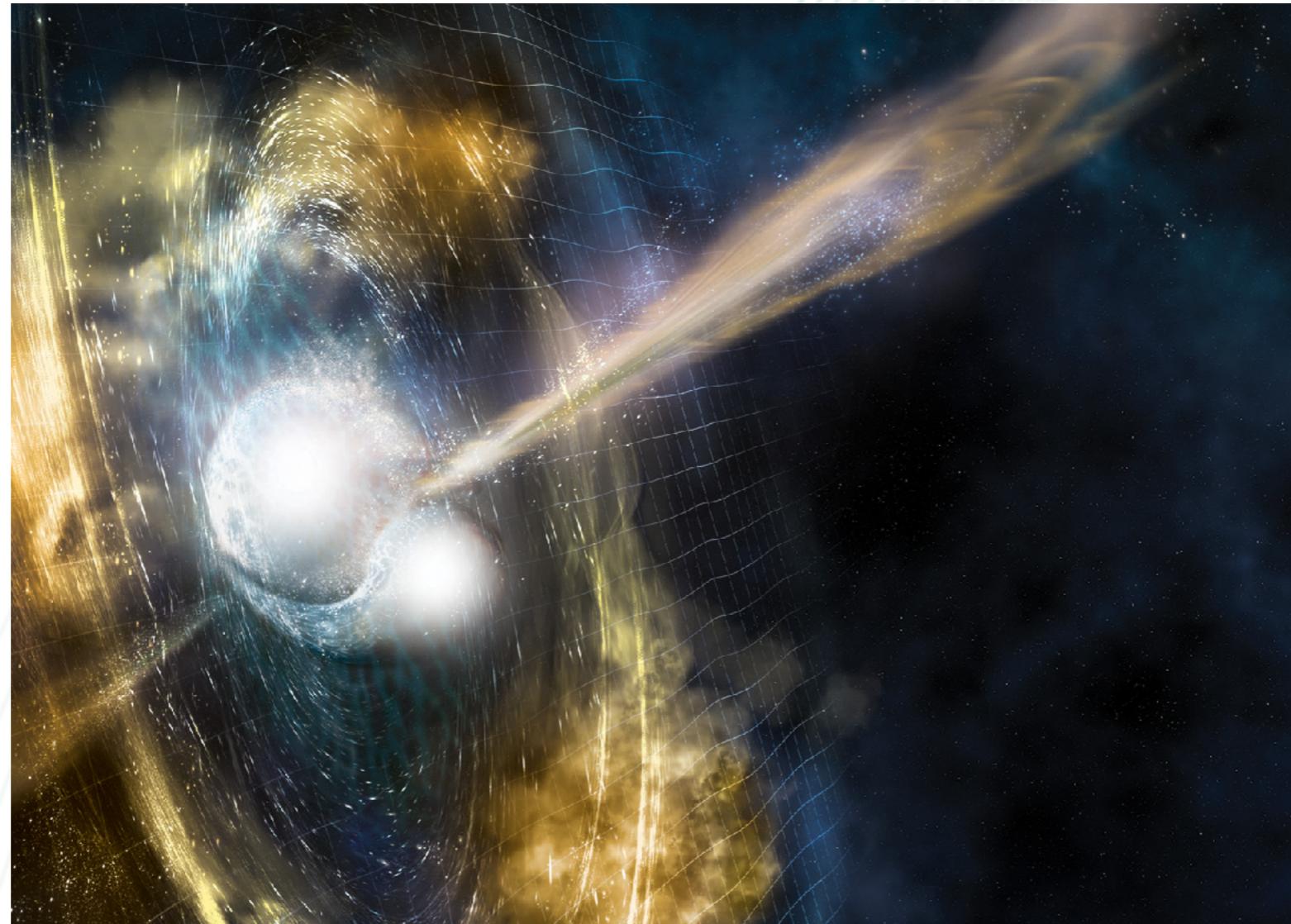




# Neutron Stars and Gravitational Waves - Part 1

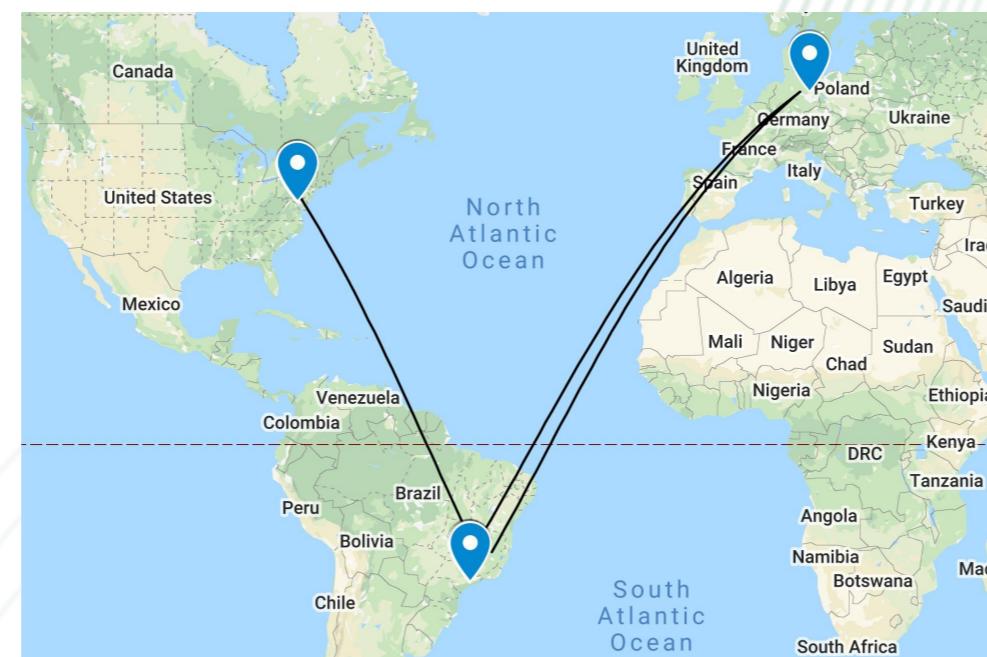


Cecilia Chirenti

Fermi Summer School - Lewes DE - June 2 2022

# Introductions

4 (Visiting) Associate Research Scientist UMD/GSFC/CRESST



1 Physics BSc and PhD at University of São Paulo, Brazil



2 Postdoc at MPI for Gravitational Physics Albert Einstein Institute (AEI), Germany



3 Assistant (and then Associate) Professor of Applied Mathematics at UFABC, Brazil



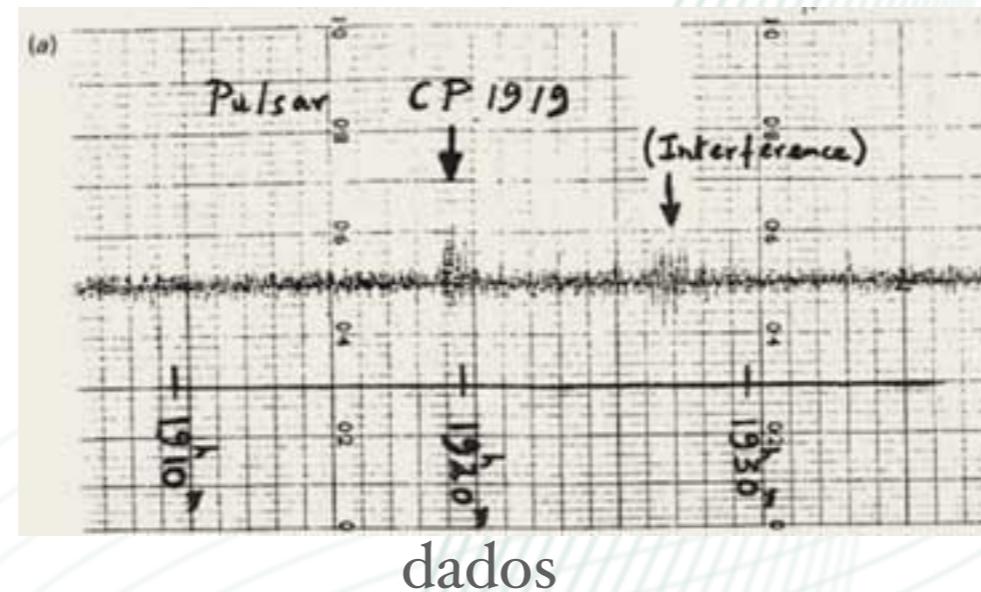
# Neutron stars: how it all began



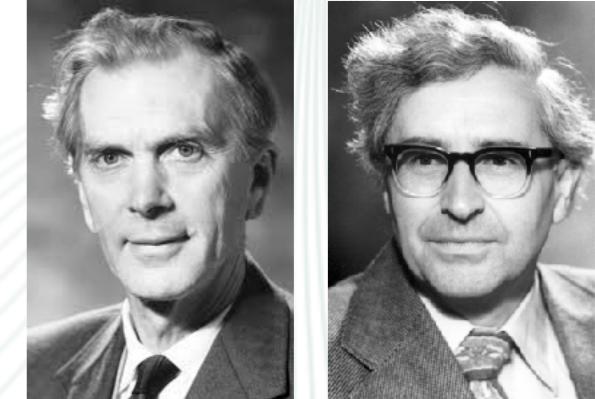
Jocelyn Bell - 1967

Little Green Men?  
 $LGM_1, LGM_2, LGM_3$

## The discovery of pulsars



“telescope” in Cambridge

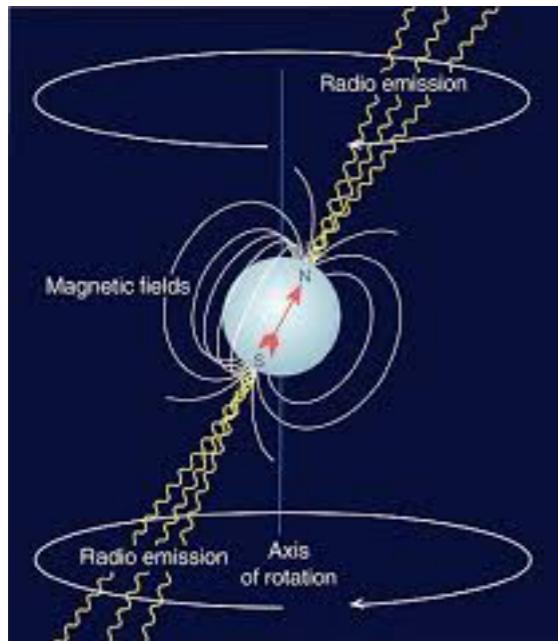


Physics Nobel Prize 1974



Breakthrough Prize 2018

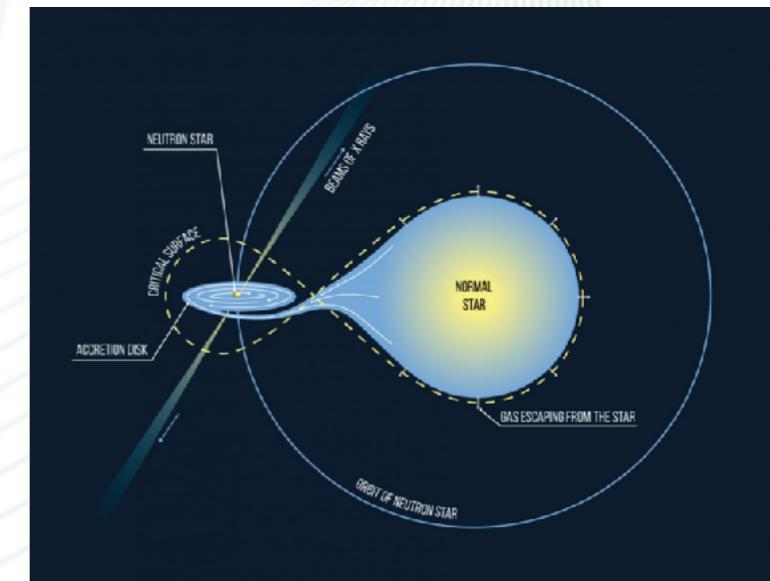
# How do we observe neutron stars?



Radio pulsars



Crab Nebula

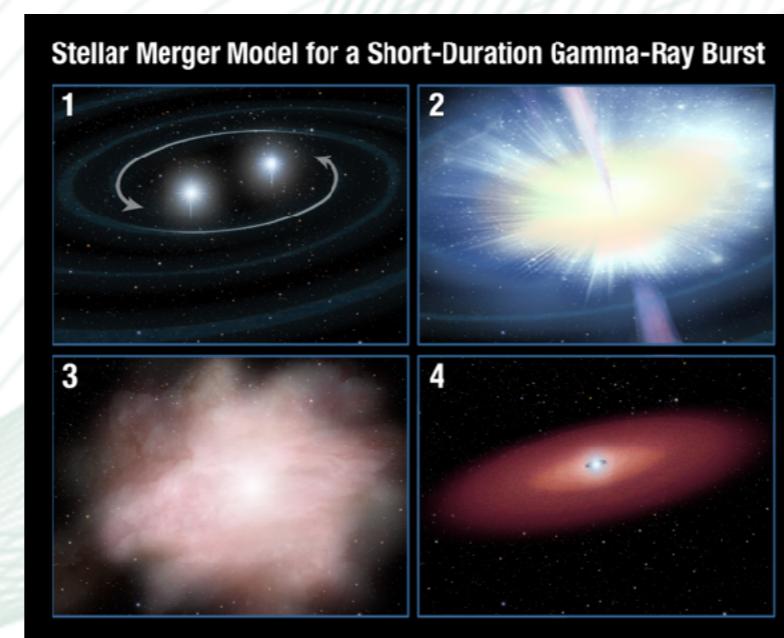


X-ray binaries

Gravitational waves



LIGO



Kilonova

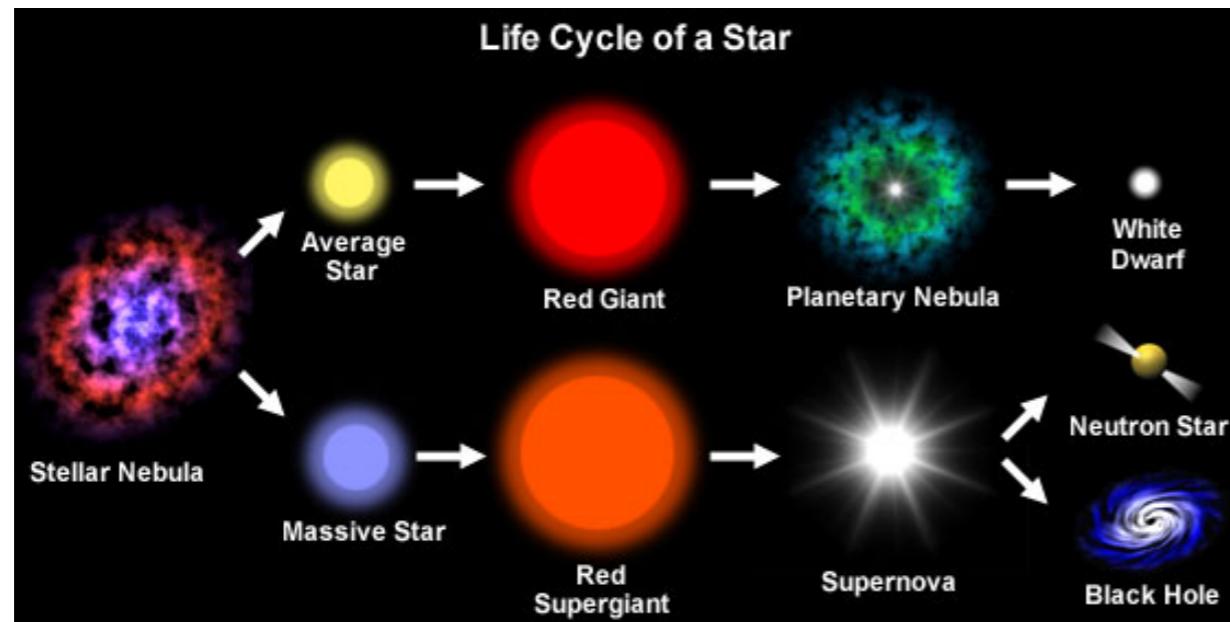
Short gamma-ray burst



Fermi

# How are neutron stars born?

## Supernovae! (*not* type Ia)



The initial mass determines the fate of the star

1<sup>st</sup> supernova  
observation  
in 184 AD!



"The heavens are not immutable?"

Poll:

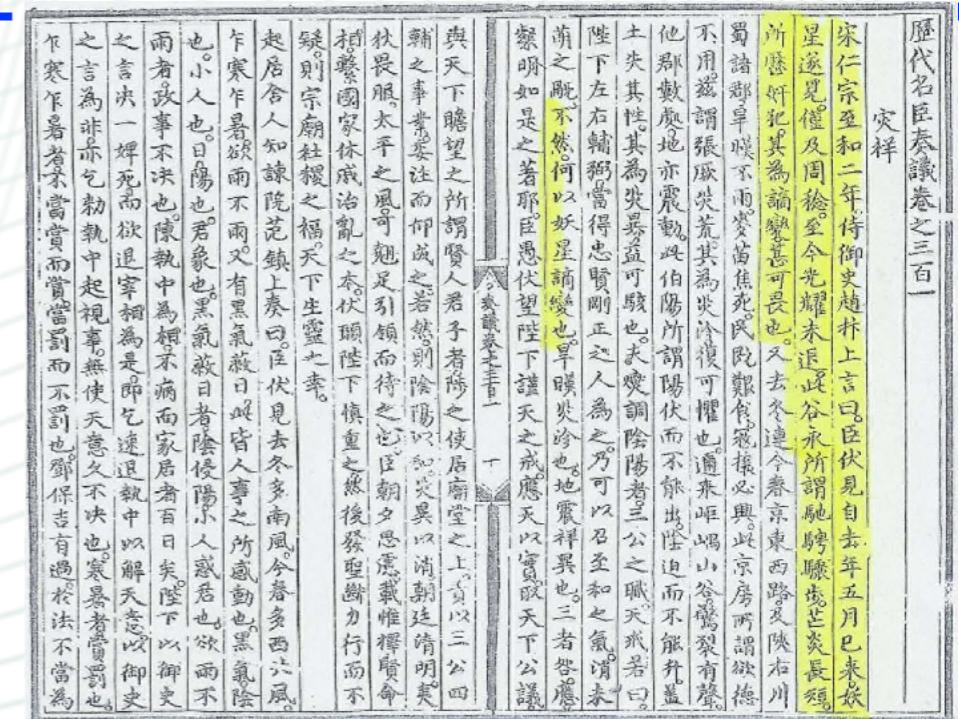
Are supernovae rare events?

Estimate:

One per galaxy per century!

What is the total number of supernovae per second in the universe?

- a) 30,000; b) 30; c) 0.03; d) 0.00003;
- e) 0.00000003 / s



The crab supernova was observed by Chinese astronomers in 1054 AD:  
a guest star

# Why neutrons?



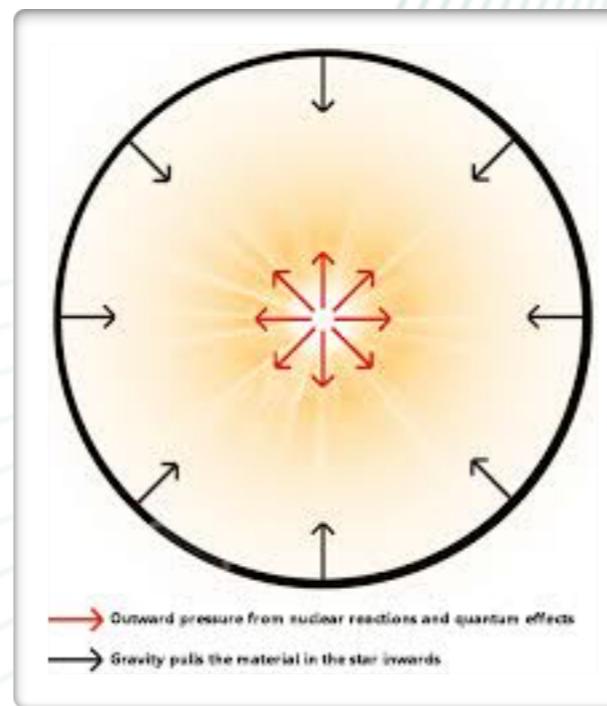
S. Chandrasekhar and wife - 1939

Pauli's exclusion principle  
(fermions)

Maximum mass:  
white dwarfs  $\sim 1.4M_{\odot}$   
(Chandrasekhar limit)

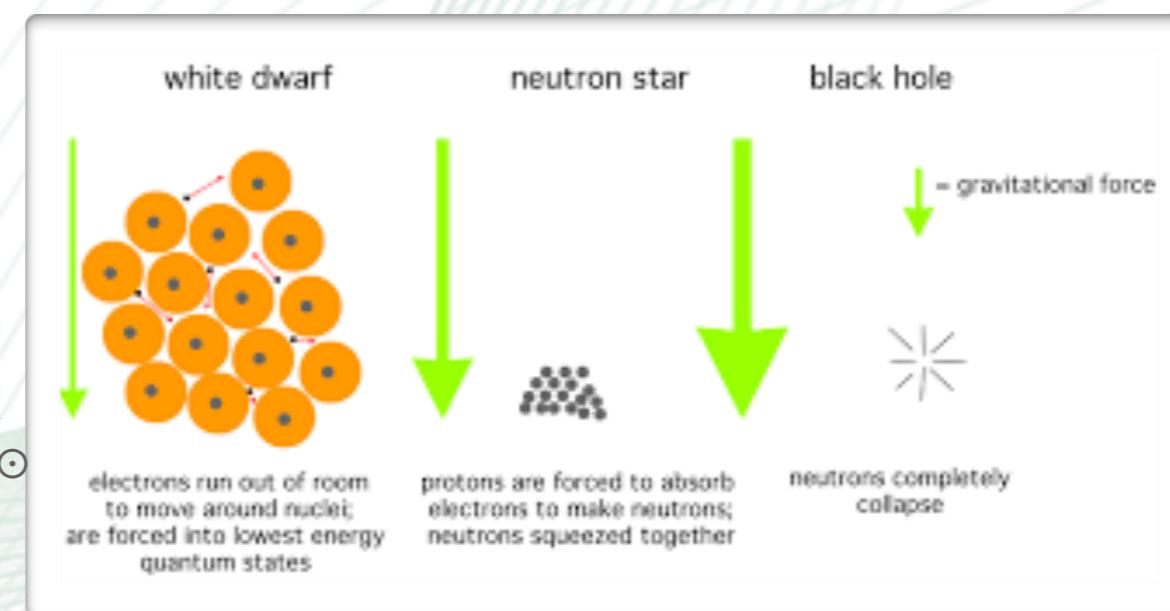
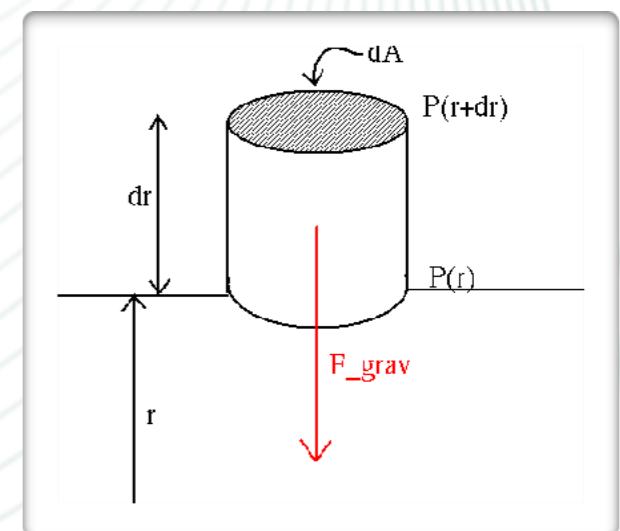
neutron stars  $\sim 2.2 - 3M_{\odot}$

Stellar equilibrium



Gas pressure balances the gravitational attraction

$$F_{\text{gas}} = F_{\text{gravitational}}$$



$$F_{\text{gas}} = \frac{P}{A}, \quad m = \rho V$$

$$F_{\text{gravitational}} = -\frac{GMm}{r^2}$$

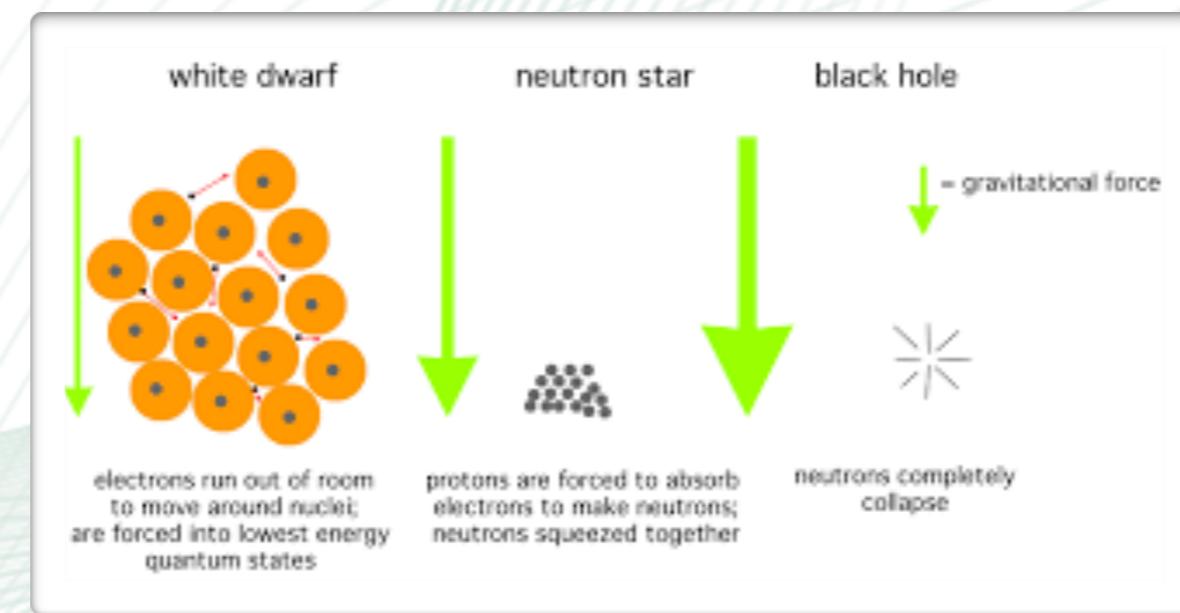
$$\frac{dP}{dr} = -\frac{GM(r)\rho(r)}{r^2}$$

Hydrostatic equilibrium

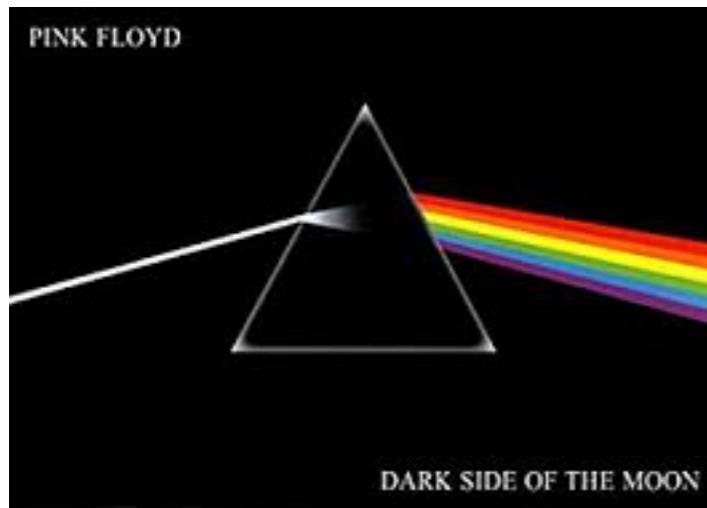
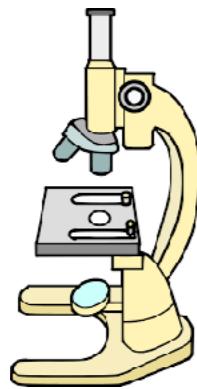
# Group discussion question

*Can there be stars more compact than neutron stars?*

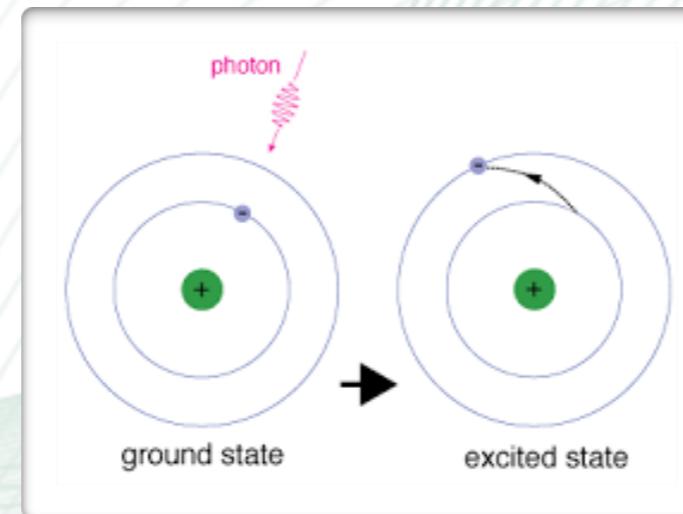
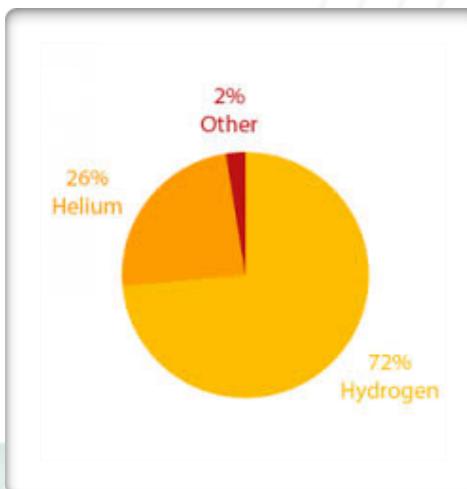
*What would they look like?*



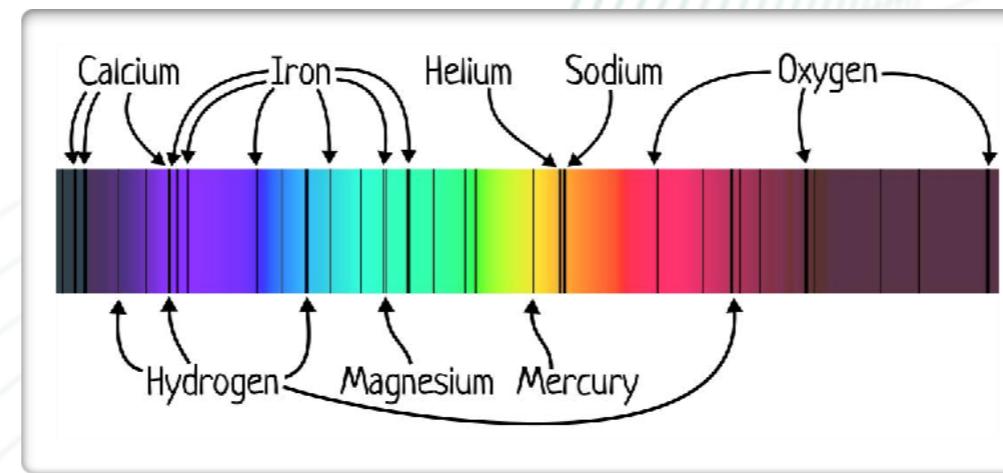
# What are stars made of?



Composition of the sun



Spectral lines of the sun



ionized atom

Astronomer's Periodic Table

Element	Relative Abundance
H	72%
He	26%
Others	2%



Cecilia Payne - 1925

Astronomer's Periodic Table

Metals

Element	Relative Abundance
H	72%
He	26%
Others	2%

“astronomer periodic table”

Periodic table

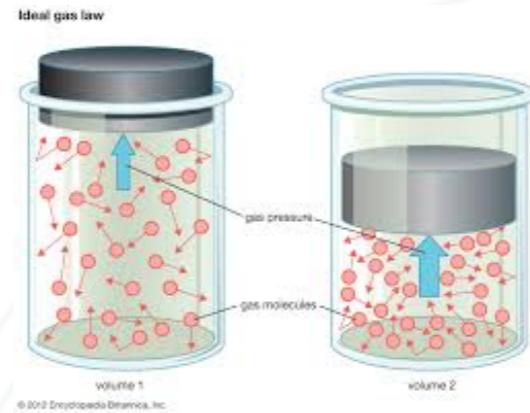
# Equation of State (EOS)

Unfortunately, spectroscopy doesn't work for neutron stars: the spectrum has no lines! (*Why?*)

For an ideal gas:

$$PV = nRT$$

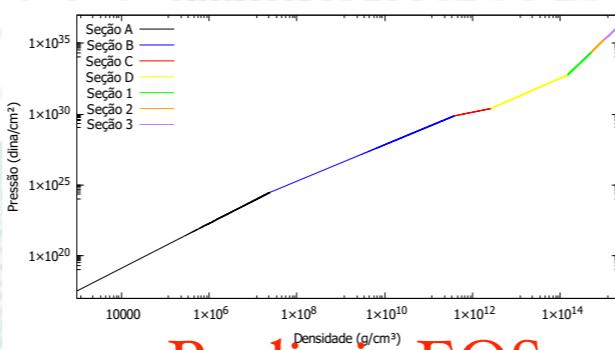
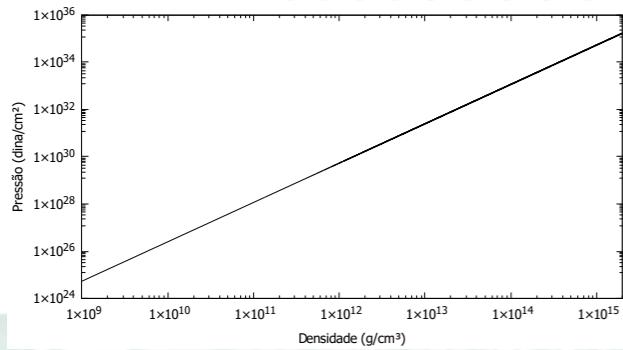
$$P = P(\rho, T)$$



Simplifying (a lot) more:

$$P = P(\rho) = \kappa \rho^\Gamma$$

Polytropic EOS



Realistic EOS

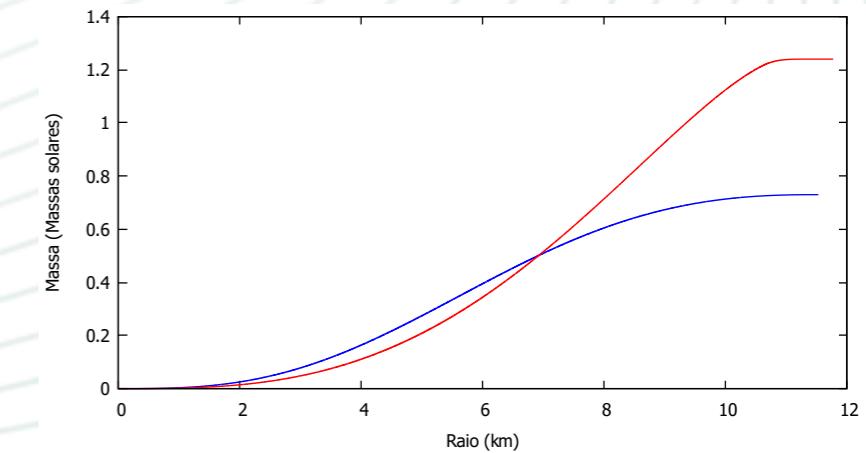
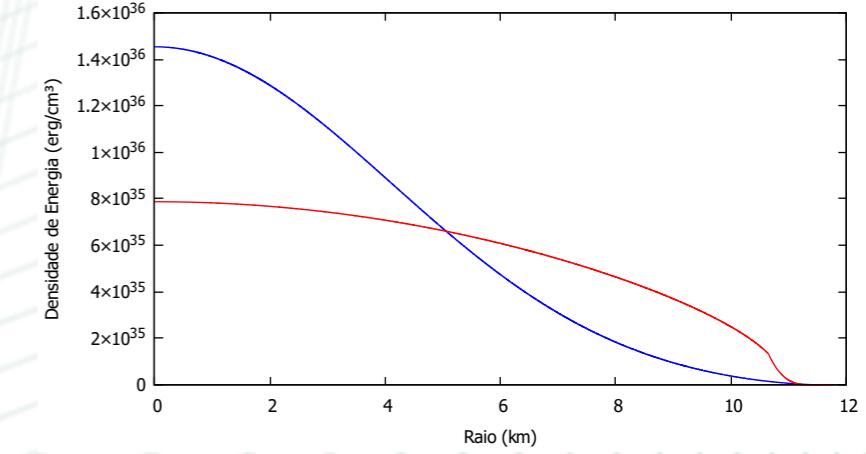
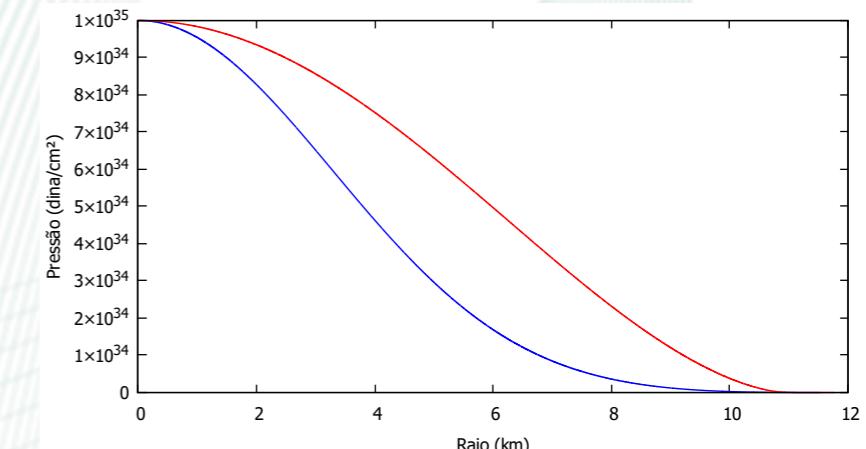
pressure

density



nuclear density:  
 $2 \times 10^{35} \text{ erg/cm}^3$

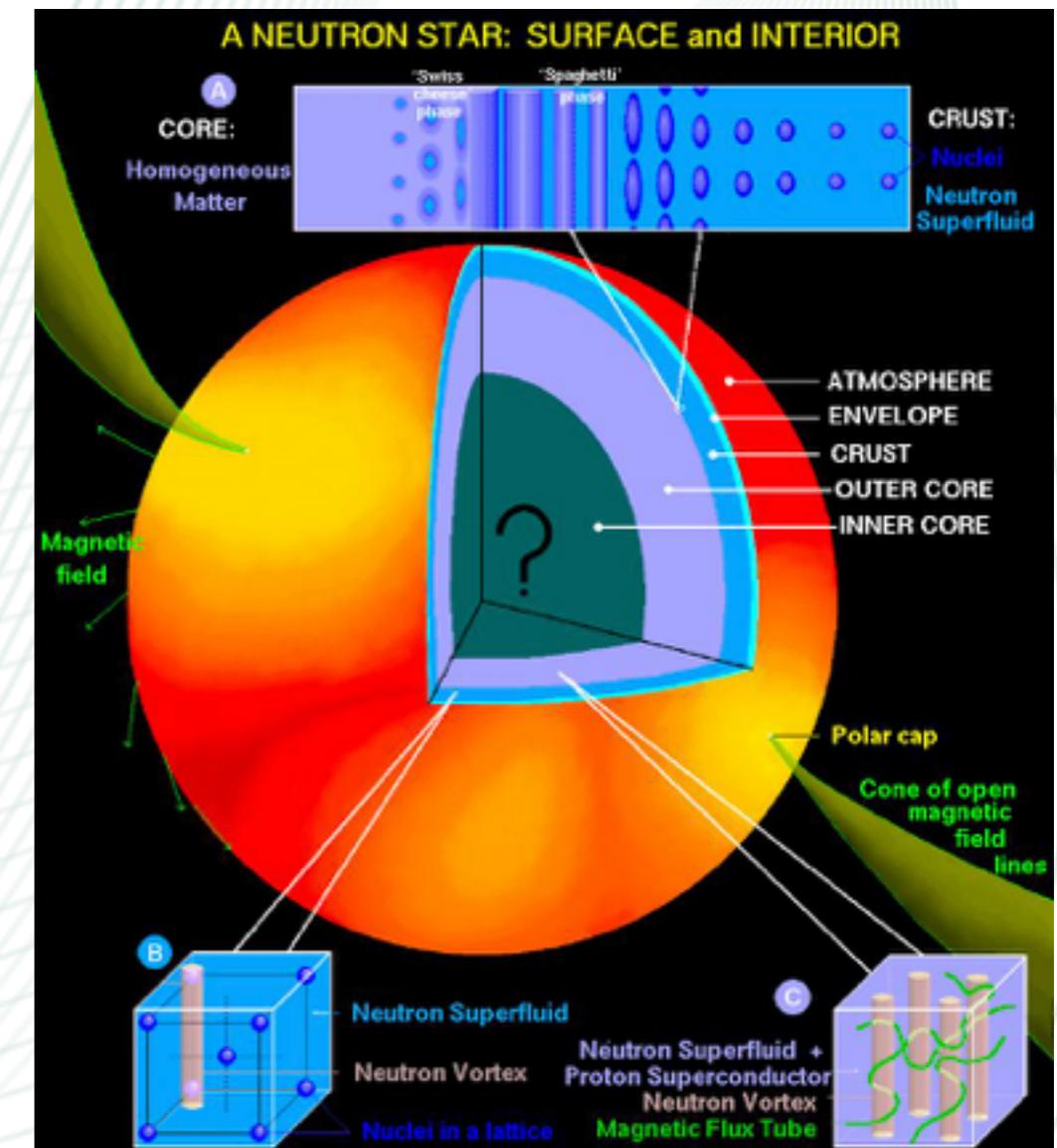
mass



radial profiles of  $p(r)$ ,  $\rho(r)$ ,  $M(r)$   
inside the star

# Inside a neutron star

- \* The core of a neutron star is at several times the nuclear density
- \* The composition is unknown:
  - \* Nucleons?
  - \* Strange matter?
  - \* Quark matter?
  - \* Condensates?



<http://www.astroscu.unam.mx/neutrones/NS-picture/NStar/NStar-I.gif>

# A particle physics problem?

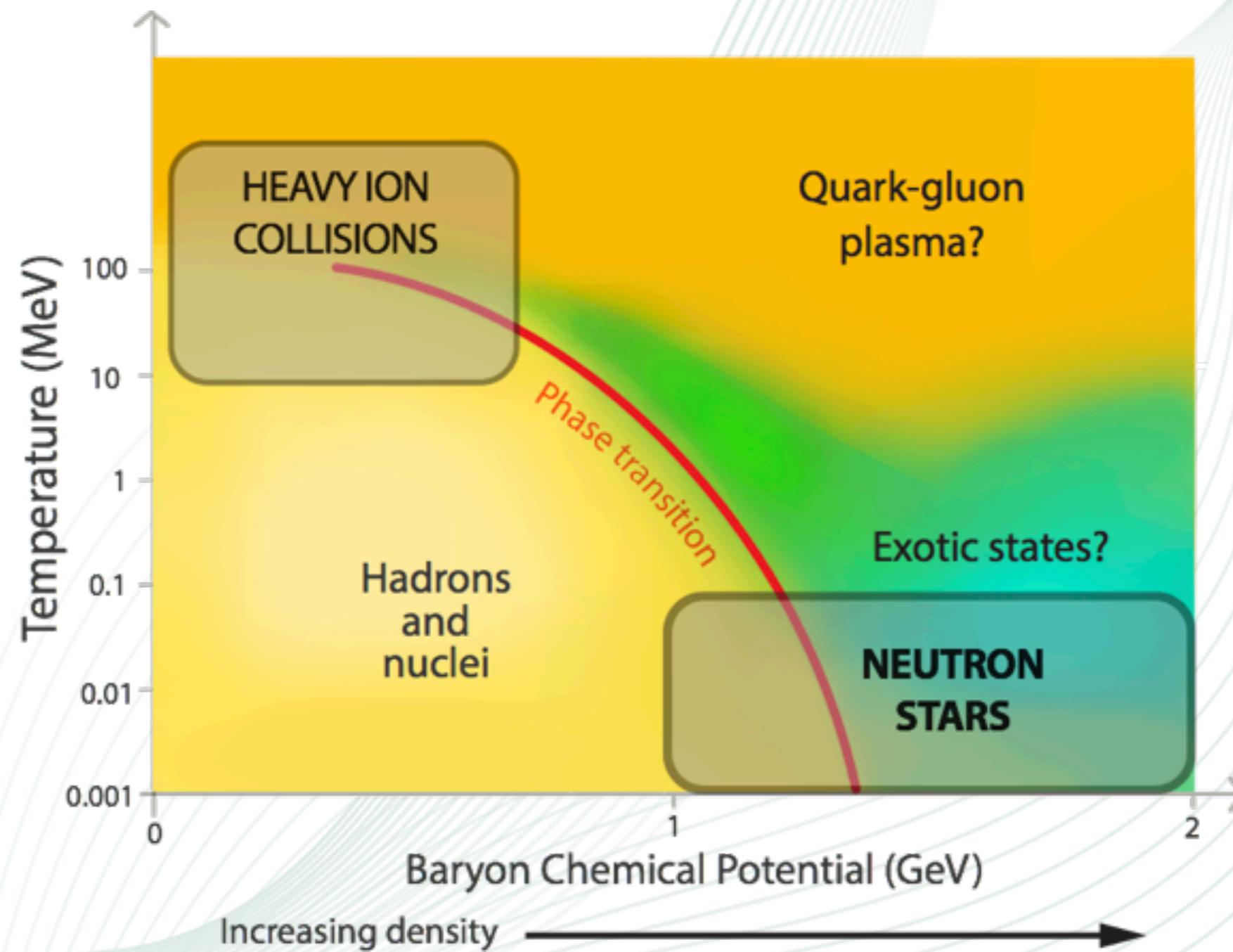


Figure: Watts et al. 2016

# Particle physics vs. Curved spacetime

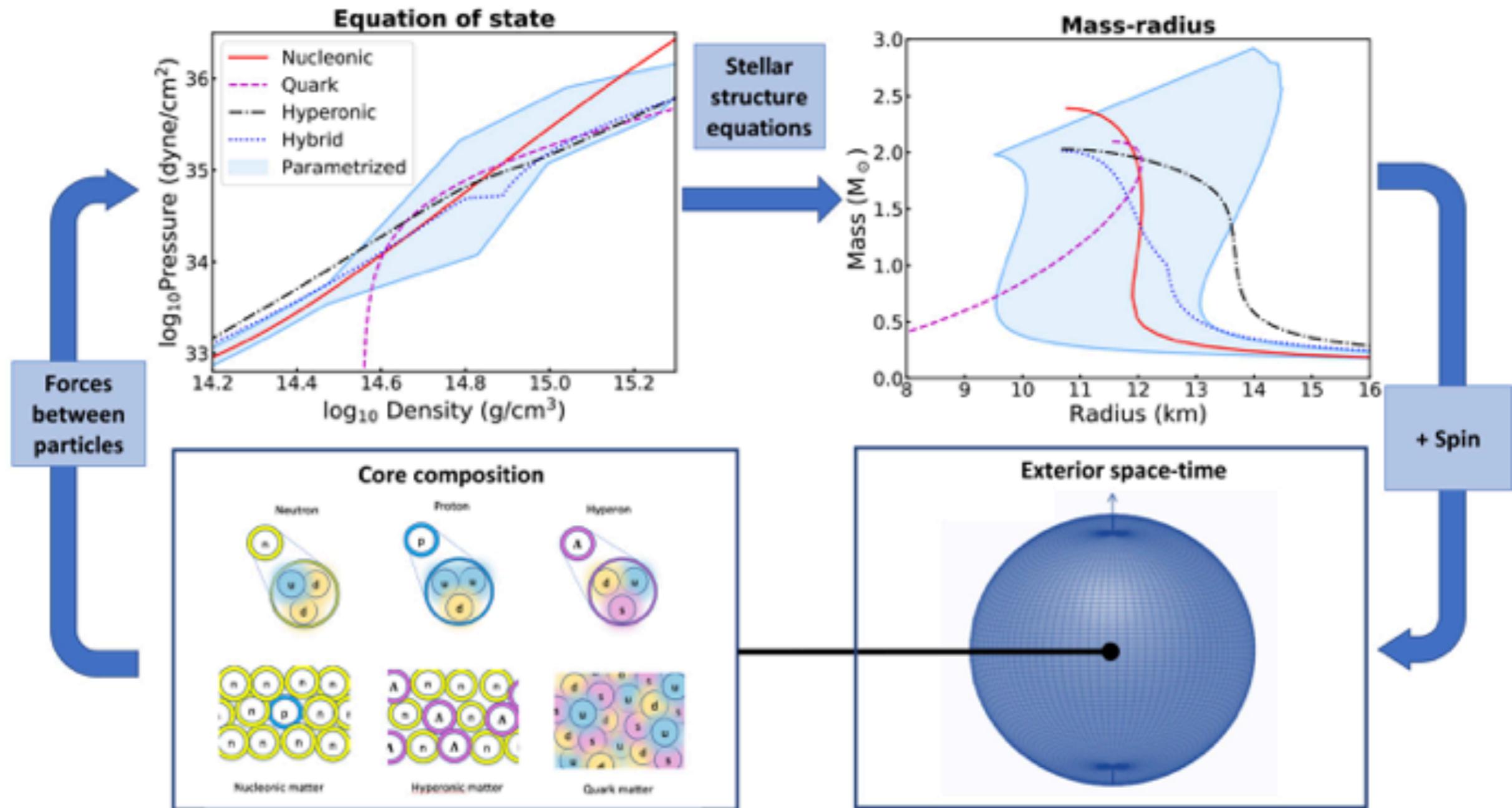


Figure: Adapted from Ray et al. 2019

# Maximum Mass

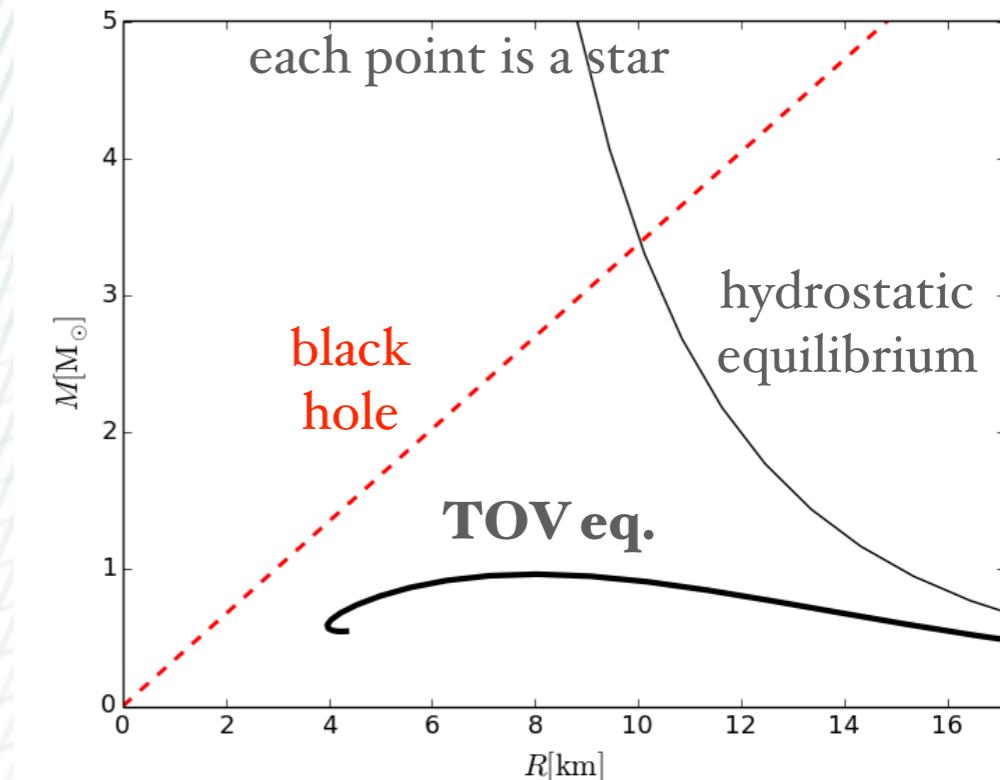
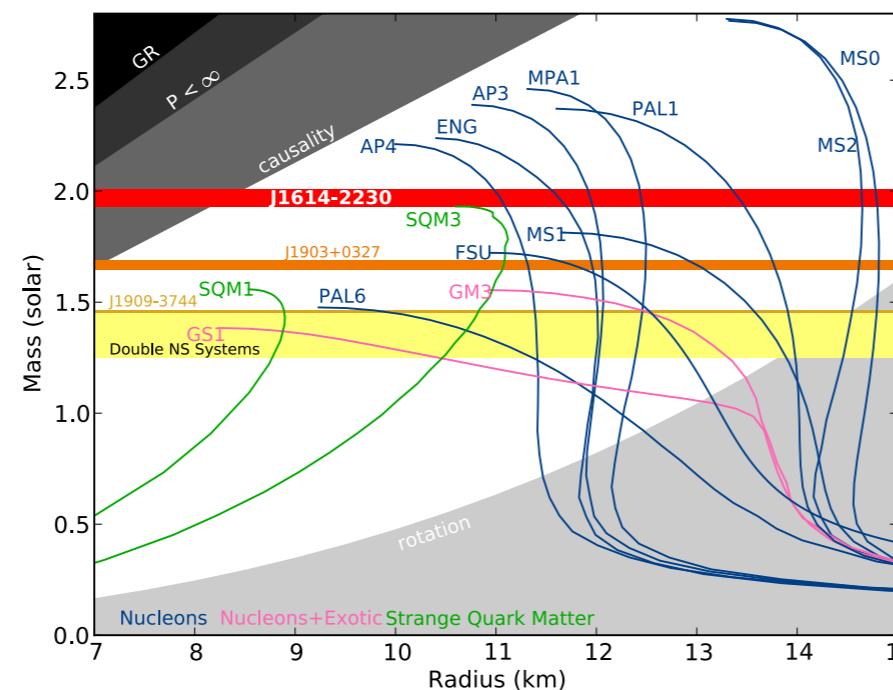
If the central density increases,  
then the total mass must  
increase, right? *Wrong!*

Tolman-Oppenheimer-Volkoff (TOV) eq.

$$\frac{dP}{dr} = -\frac{G}{r^2} \left[ \rho(r) + \frac{P(r)}{c^2} \right] \left[ m(r) + \frac{4\pi r^3 P(r)}{c^2} \right] \left[ 1 - \frac{2Gm(r)}{rc^2} \right]^{-1}$$

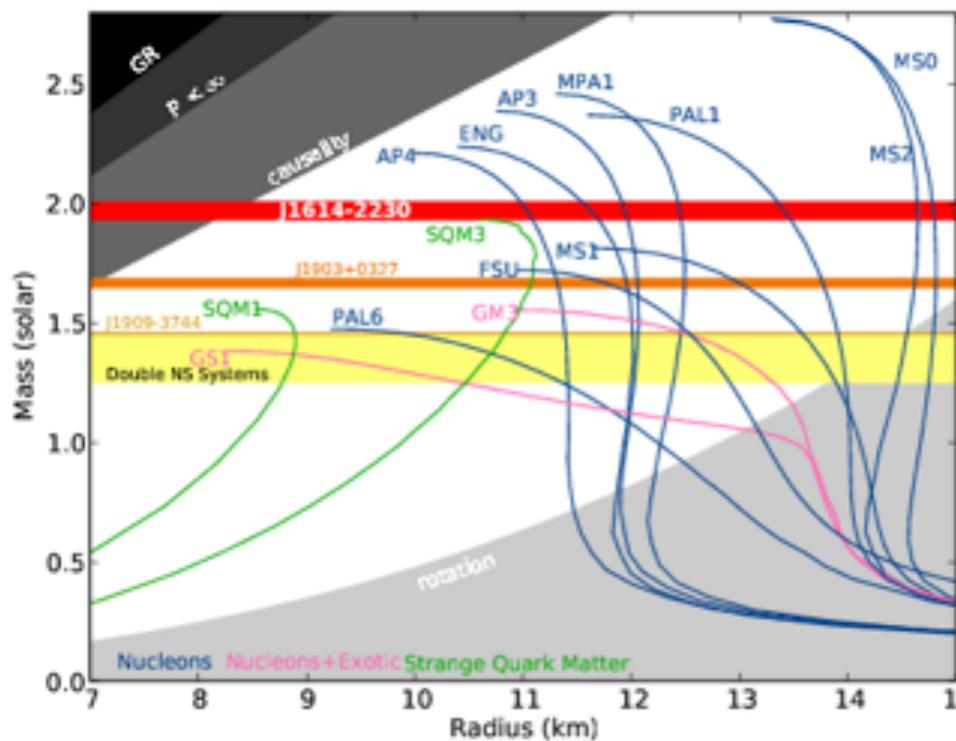
(this is the **relativistic** version of the Newtonian hydrostatic equilibrium: take  $c \rightarrow \infty$ )

Each proposed  
*EOS model*  
produces a  
different curve.  
Which are the  
*viable* models?



The mass radius curves as  
parametrized by the central  
density of the star

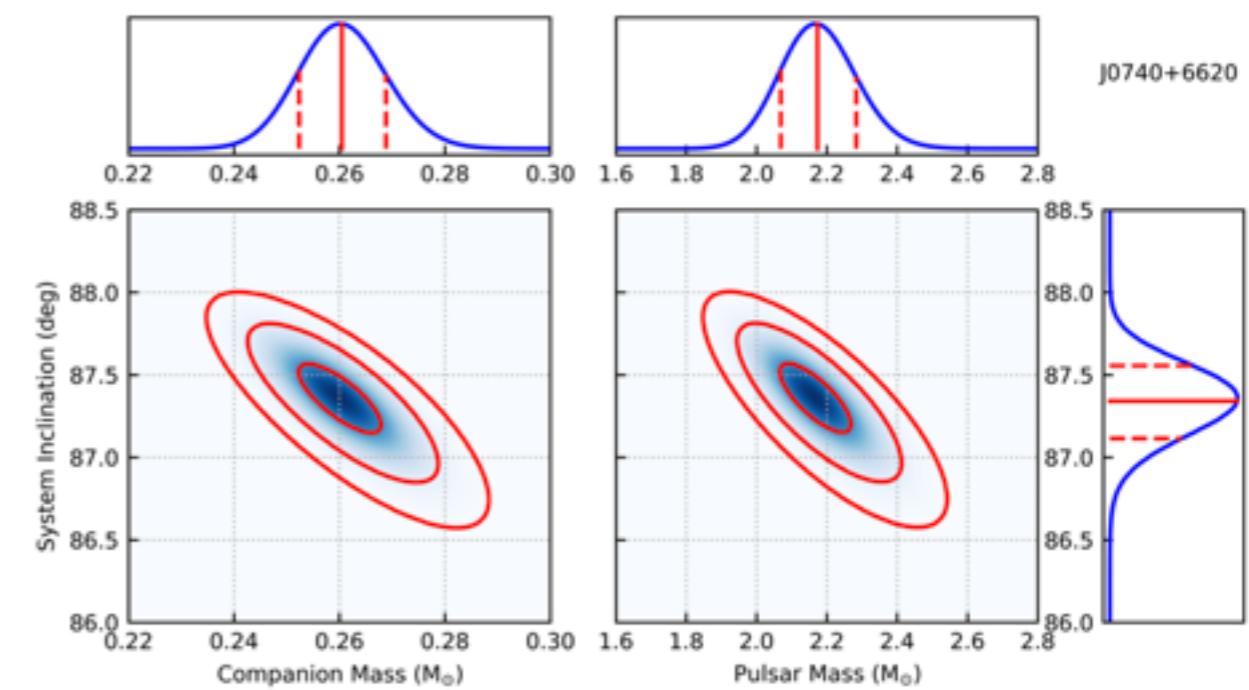
# Observed high masses



Demorest et al. 2010

*softer* EOSs predict a lower maximum mass and more compact stars

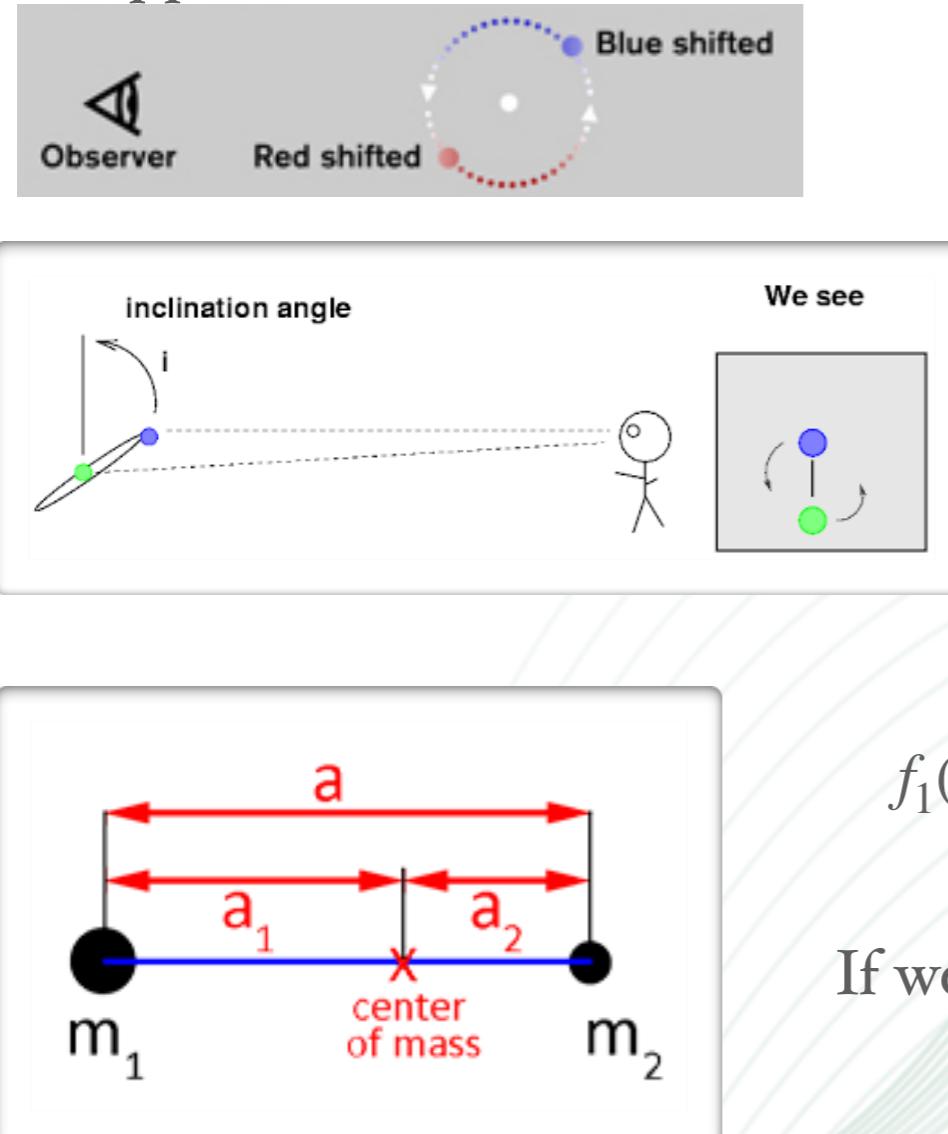
A viable EOS must have a maximum mass larger than the highest observed masses



Cromartie+ 2019

# How to measure the mass of a neutron star (in a binary system)

Doppler effect



$$\begin{aligned} a &= a_1 + a_2 \\ m_1 a_1 - m_2 a_2 &= 0 \\ q &= m_1 / m_2 \end{aligned}$$

If we can measure  
 $P$  - period of the binary  
 $v_1 = \frac{2\pi}{P} a_1 \sin i$  (Doppler)

Using Kepler's 3<sup>rd</sup> law

$$\frac{P^2}{a^3} = \frac{4\pi^2}{G(m_1 + m_2)}$$

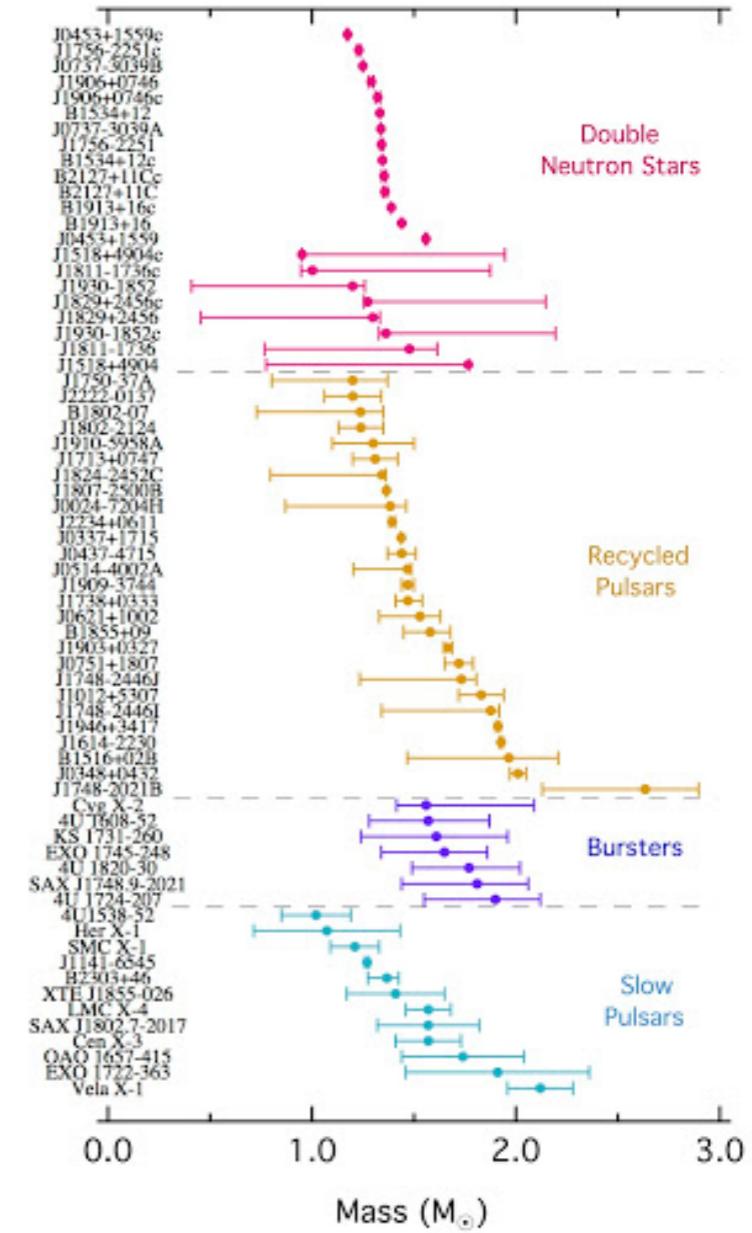
we can write

$$f_1(m_1, m_2, i) \equiv \frac{m_2^3 \sin^3 i}{(m_1 + m_2)^2} = \frac{P v_1^3}{2\pi G}$$

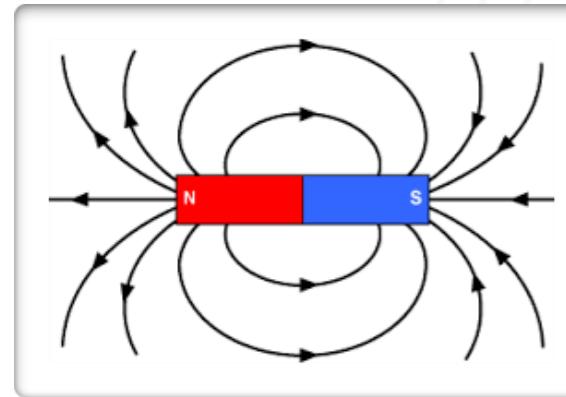
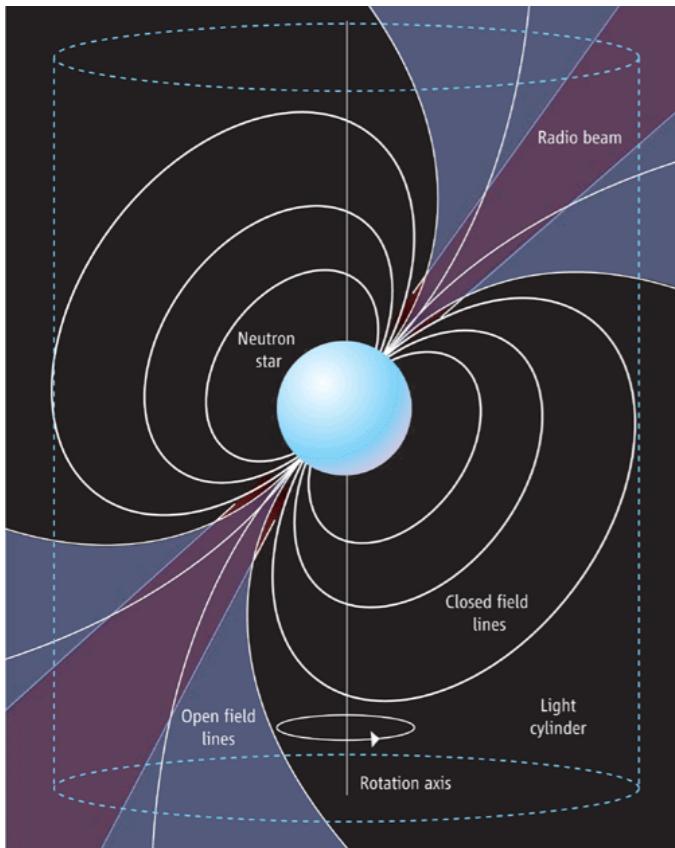
If we are also able to measure  $f_2$  (*how?*) we can find

$$m_2 = \frac{f_2 q (1 + q)^2}{\sin^3 i}$$

and from  $f_2/f_1$  we have  $q$ .



# What is the age of a pulsar?



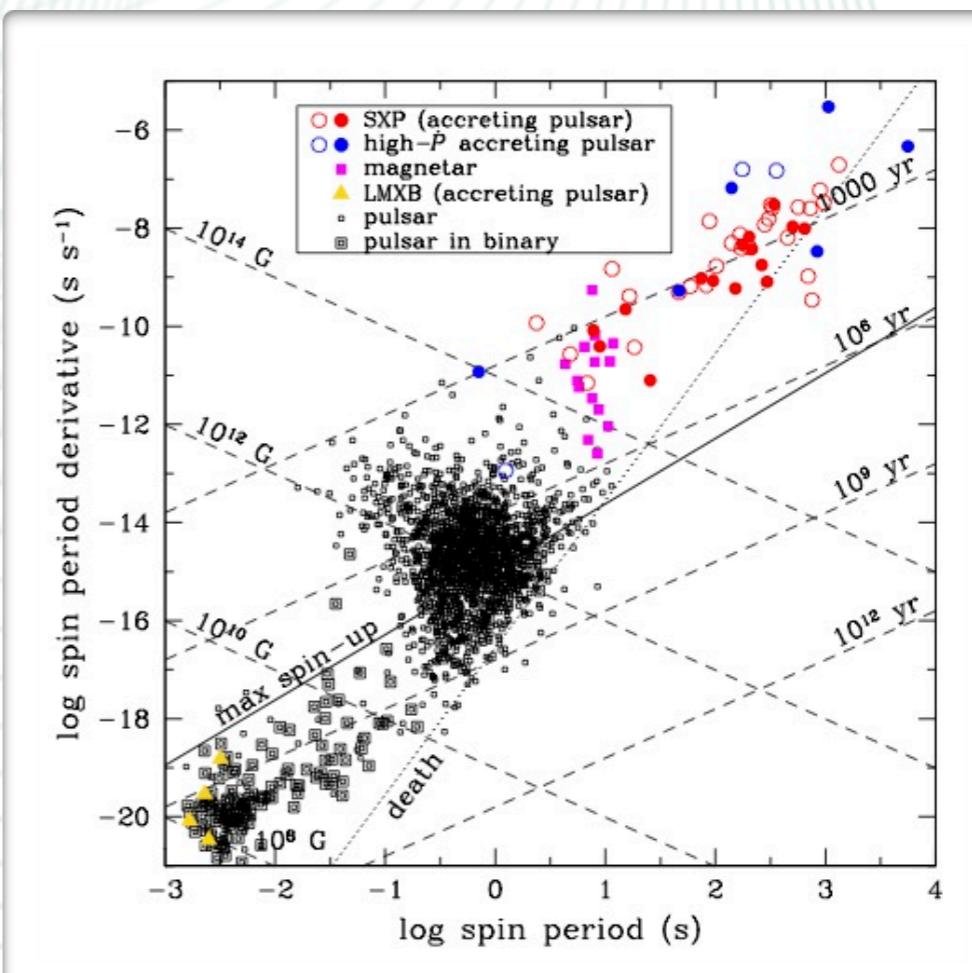
Earth's magnetic field  $\sim 0.5 \text{ G}$   
 solar magnetic field  $\sim 10 \text{ G}$   
**magnetars** can have  $B \sim 10^{15} \text{ G}$

The magnetic field brakes the rotation of pulsars  $\frac{dE}{dt} \propto -B^2$

We can measure:  $P$  - period  
 $\dot{P} = \frac{dP}{dt}$  - rate of change of the period

So we can calculate  $t = \frac{1}{2} \frac{P}{\dot{P}}$ ,  
 the characteristic age

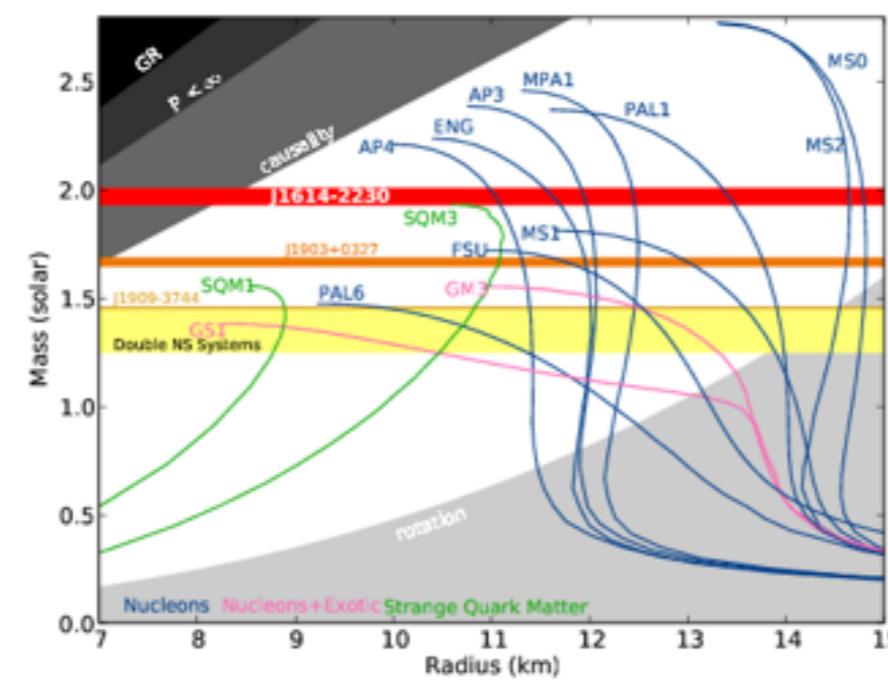
For the Crab pulsar:  
 $P = 0.0331 \text{ s}$  or  $f = 30 \text{ Hz}$   
 $\dot{P} = 4.22 \times 10^{-13} \text{ s/s}$   
 $t = \frac{1}{2} \frac{P}{\dot{P}} \approx 1240 \text{ years}$   
 (30 % overestimate)



# Group discussion question

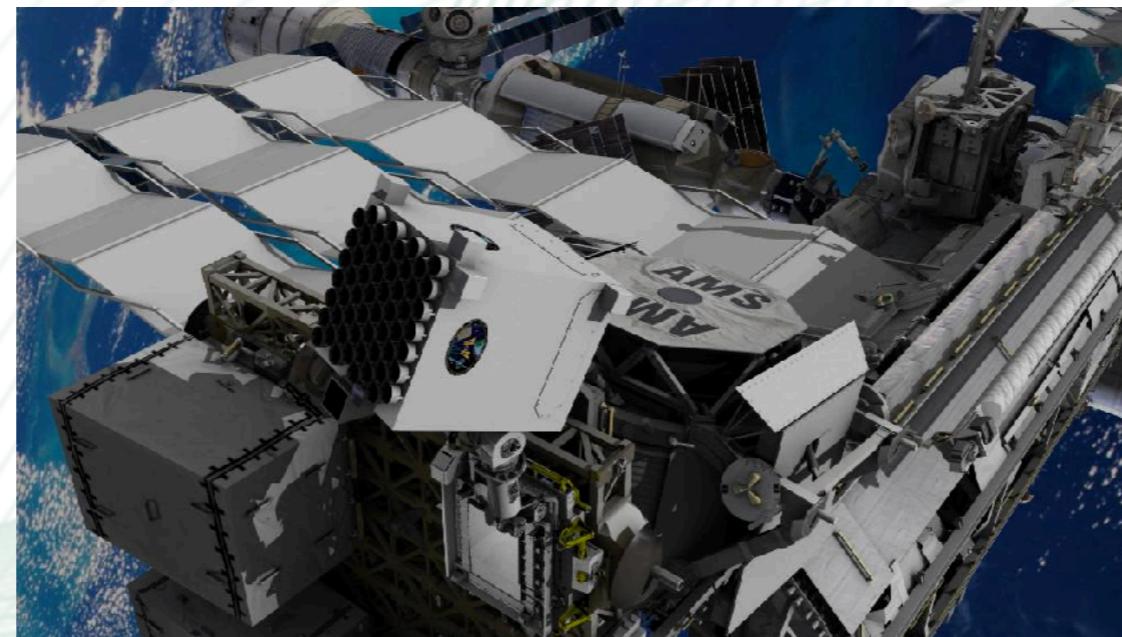
*How can we measure the radius of a neutron star?*

*What accuracy should we have?*

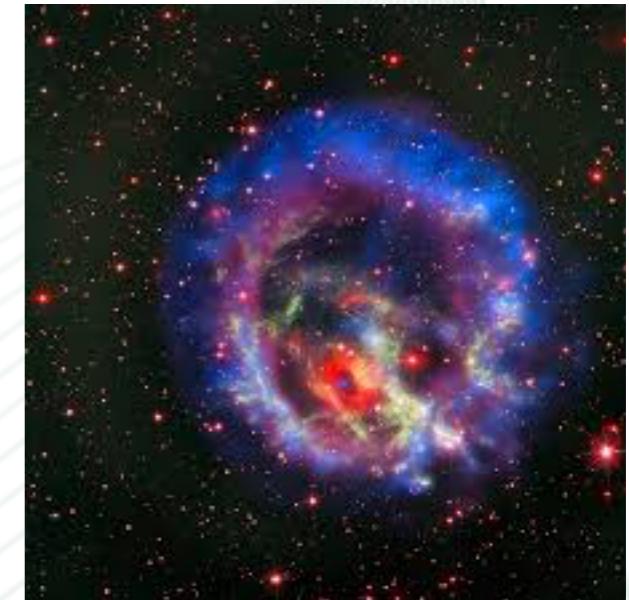
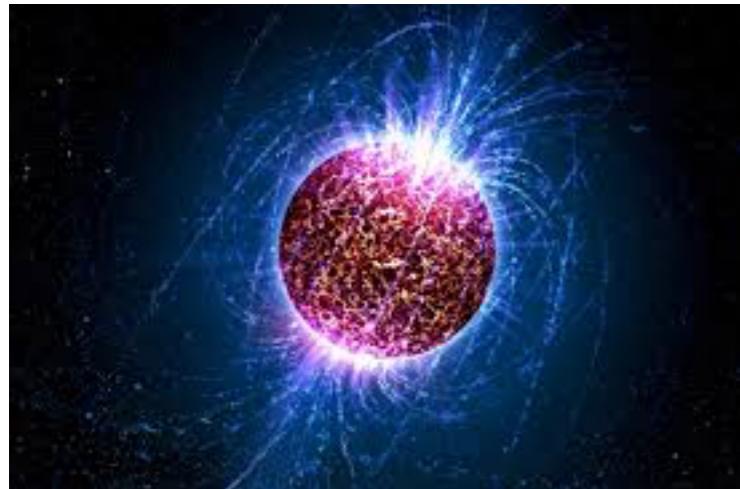


# NICER

The best current estimate for the radius of a  $M = 1.4M_{\odot}$  is  $R = (12 \pm 1)$  km, obtained by NICER (Neutron star Interior Composition ExploreR), onboard the International Space Station. NICER uses X-ray observations and waveform modeling for the emission from hotspots in isolated neutron stars.



# Coffee Break



We'll be back in 30 minutes

