



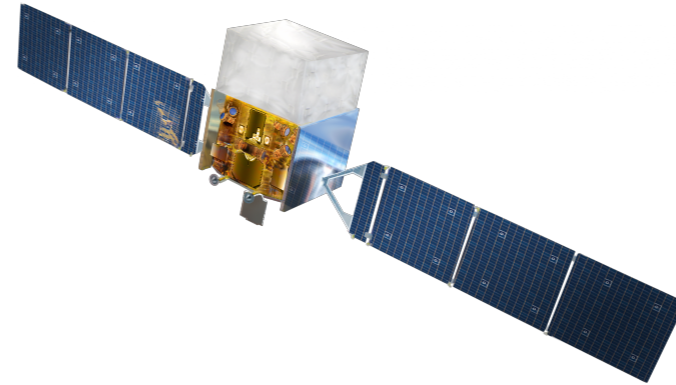
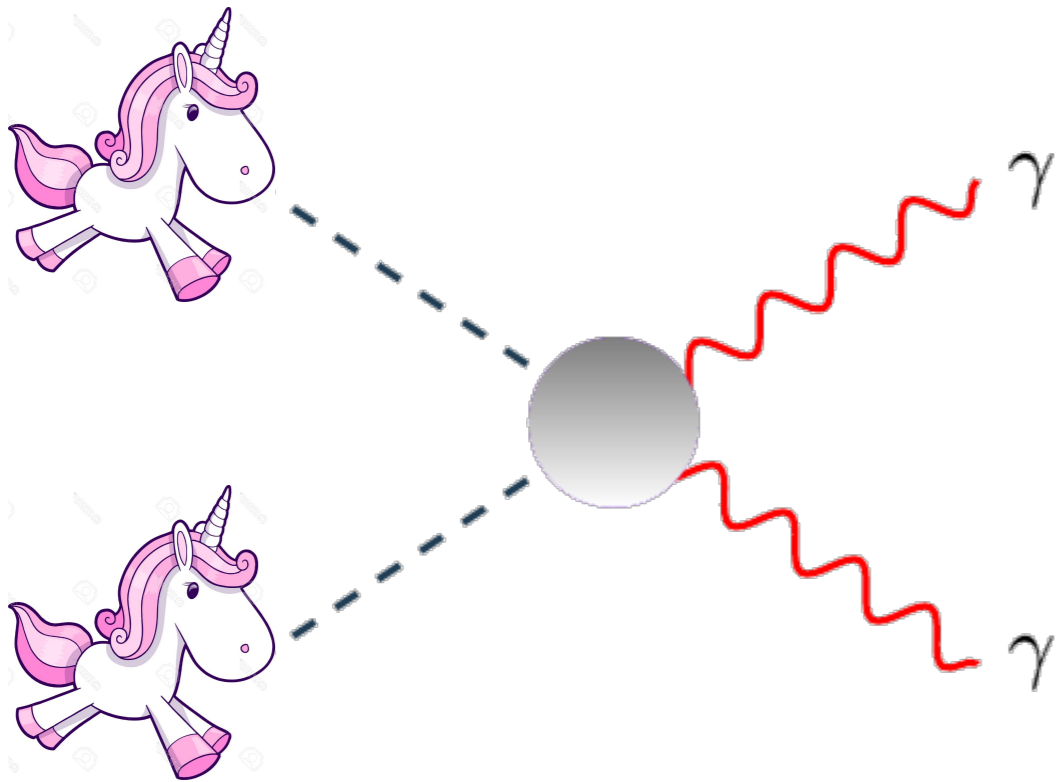
**UCLA**

# **Recurrent deconvolution background method (RDBM)**

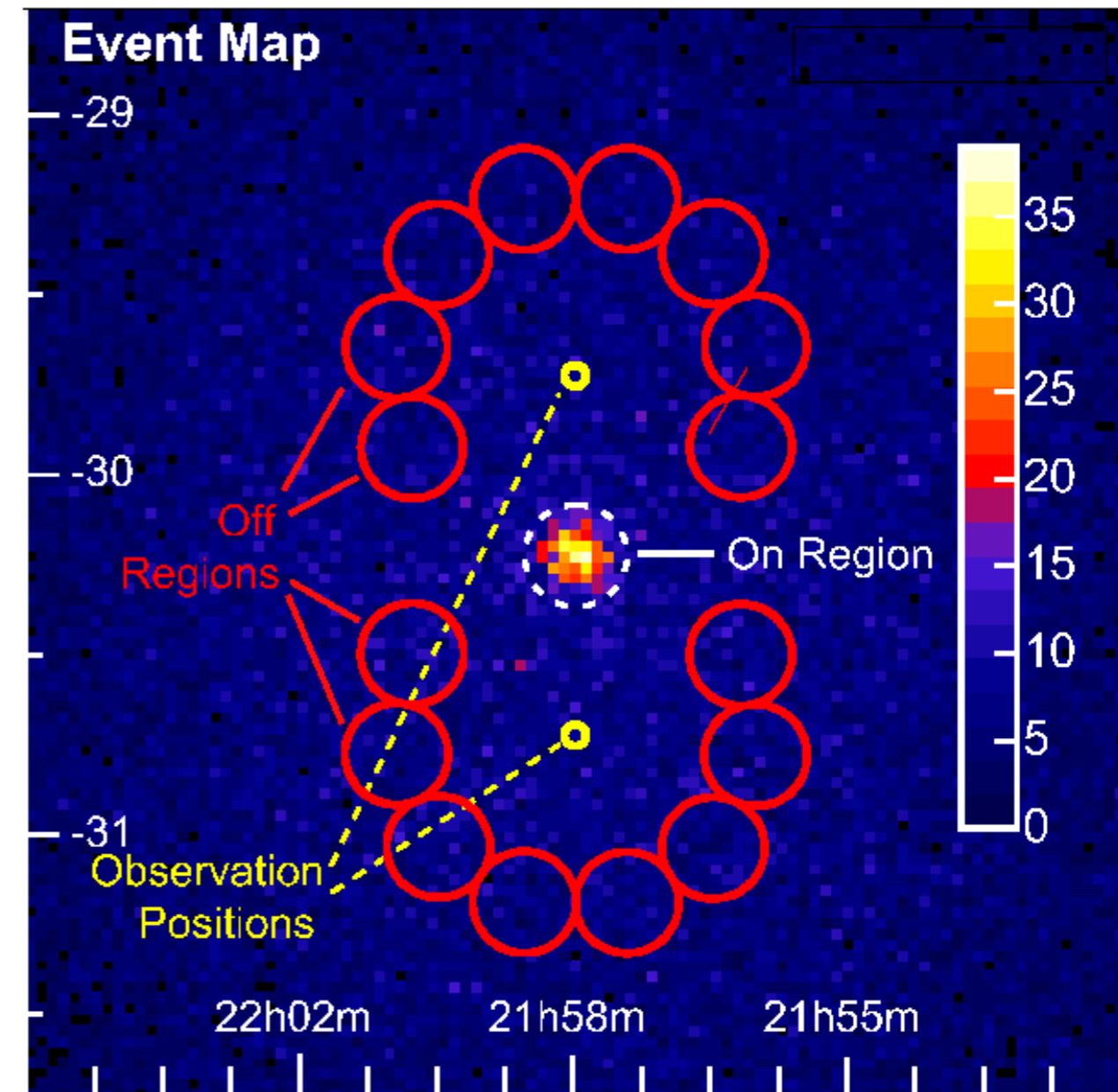
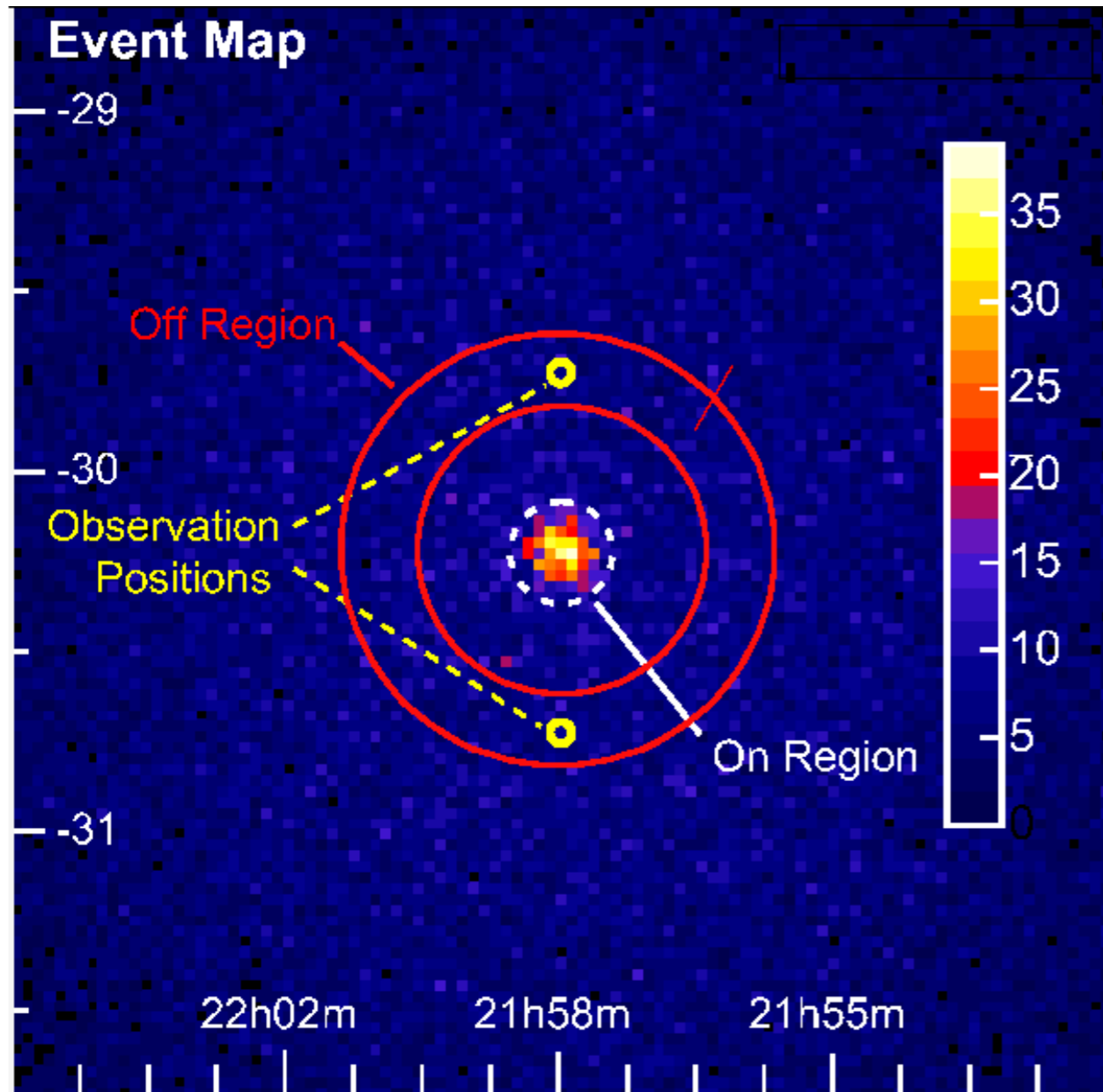
## **2019 Fermi School**

**Ruo Yu Shang and Vladimir Vassiliev**

# Search for **Dark Matter** via high energy $\gamma$ ray.



## Traditional background methods: **dark space** in telescope FoV.

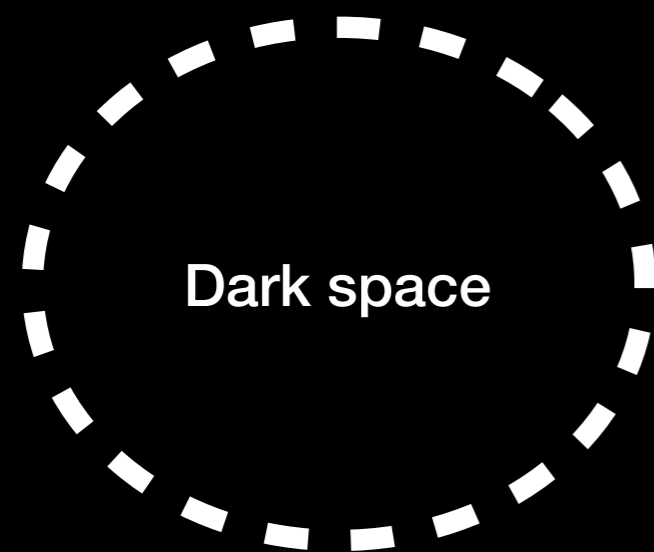


**Sizes of extended sources are larger than telescope FoV.**

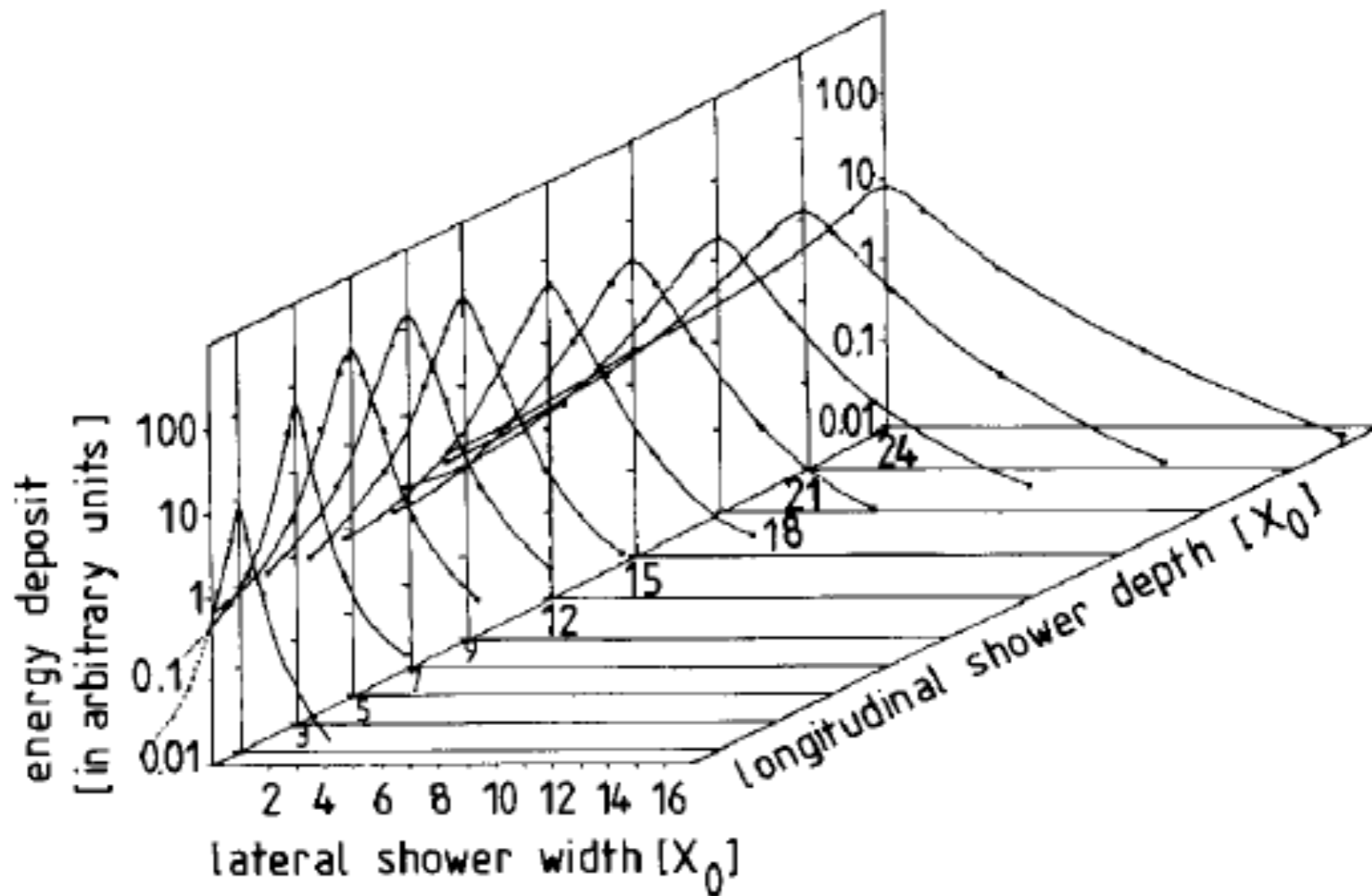
**Traditional background methods do not work.**



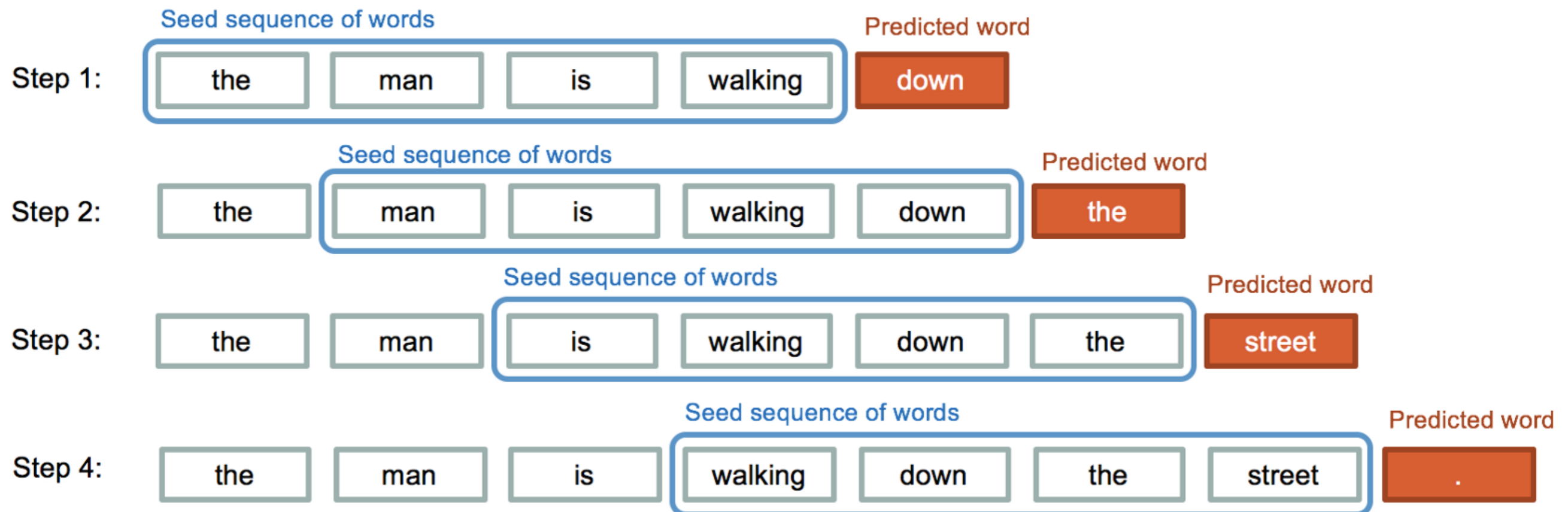
Taking OFF region from a different pointing is **expansive** and difficult to control **systematic uncertainties**.

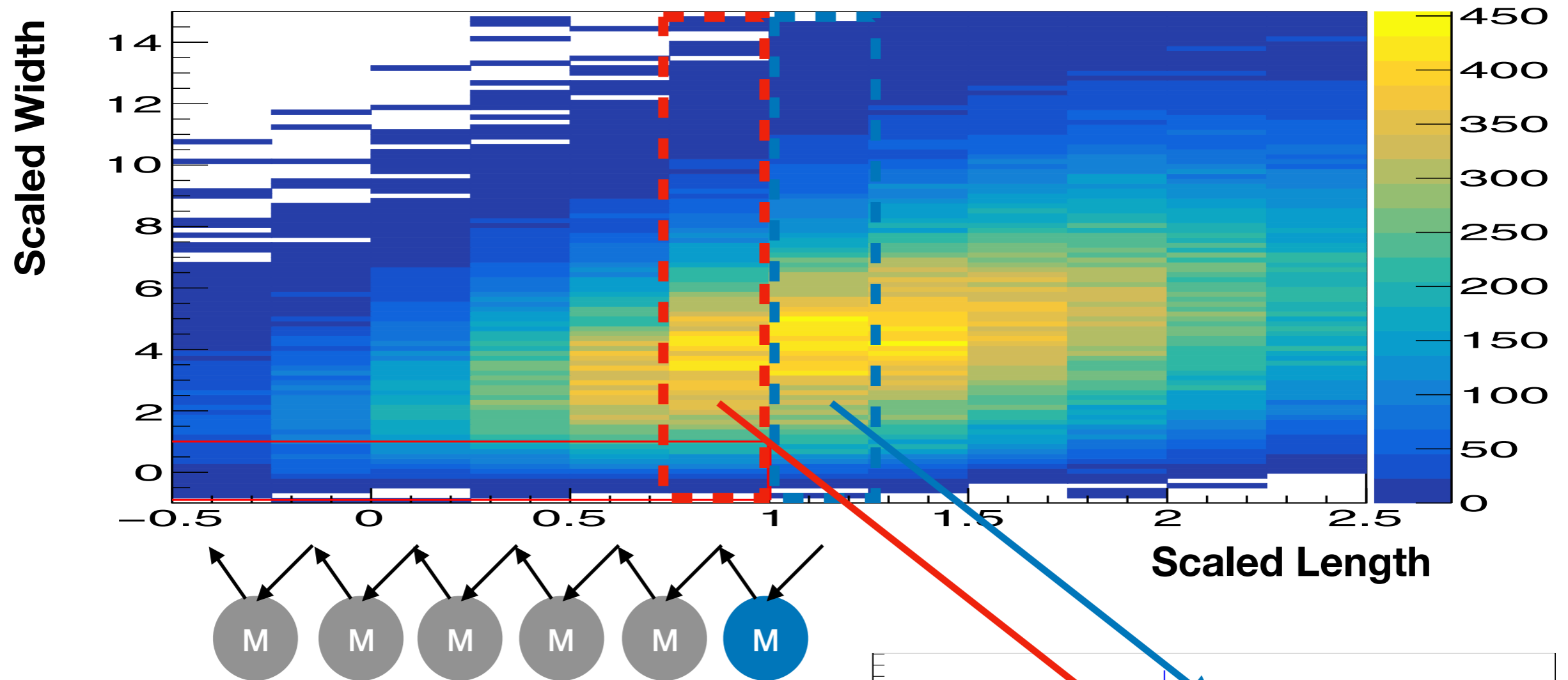


A new method exploits the correlation between shower **longitudinal** and **lateral** development.

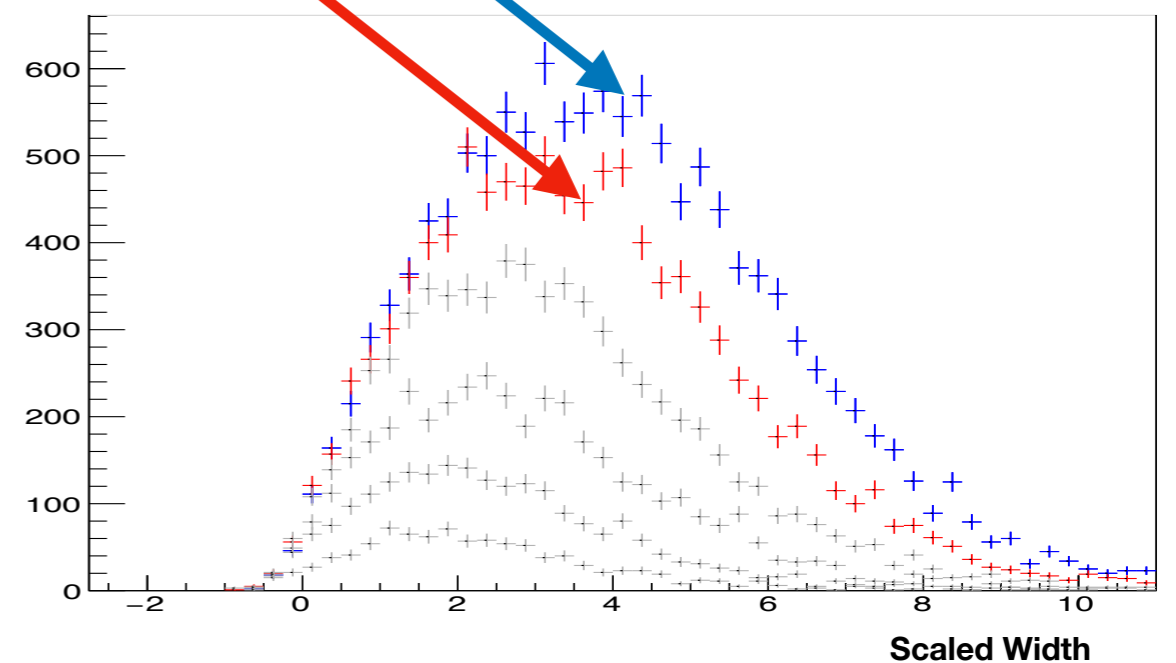


And it also borrows the idea of **Recurrent Neural Network**.  
(the algorithm that automatically generates text in your cell phone)

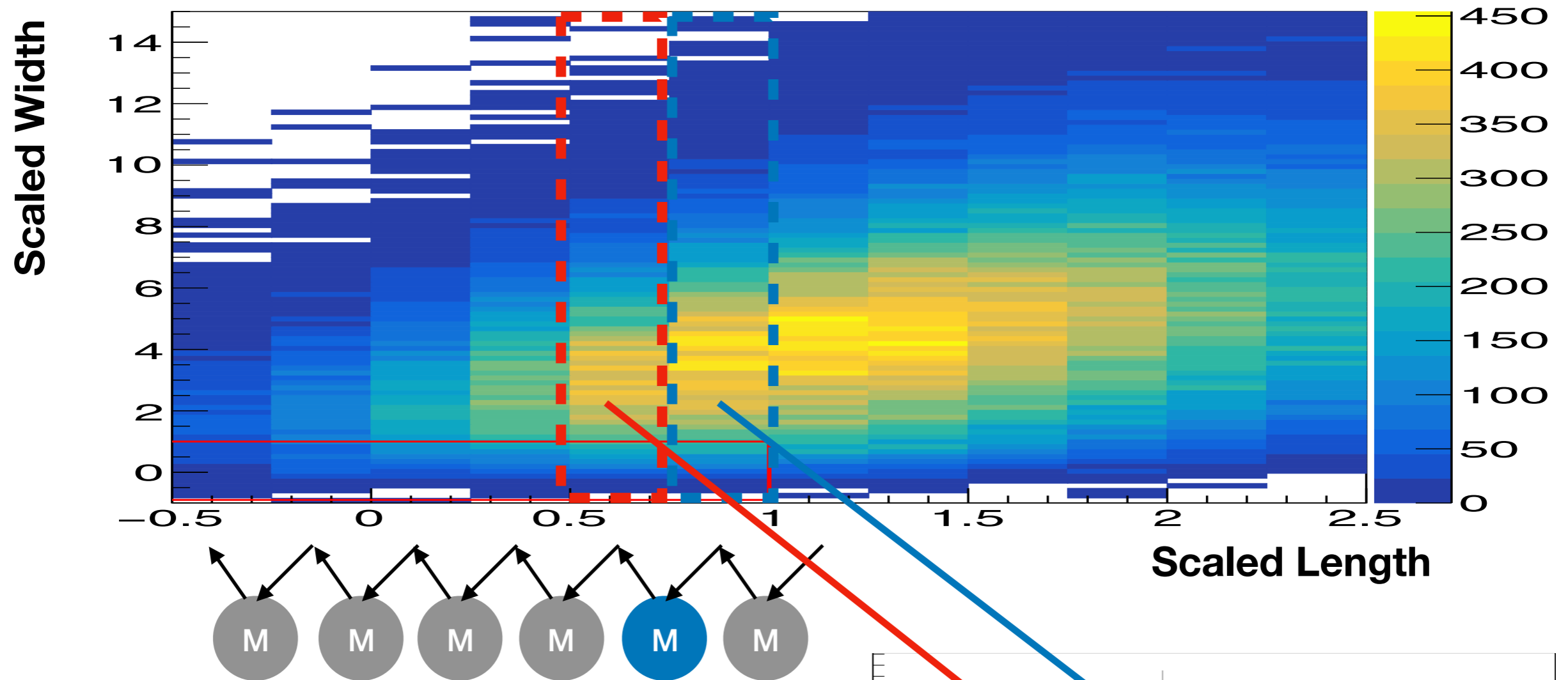




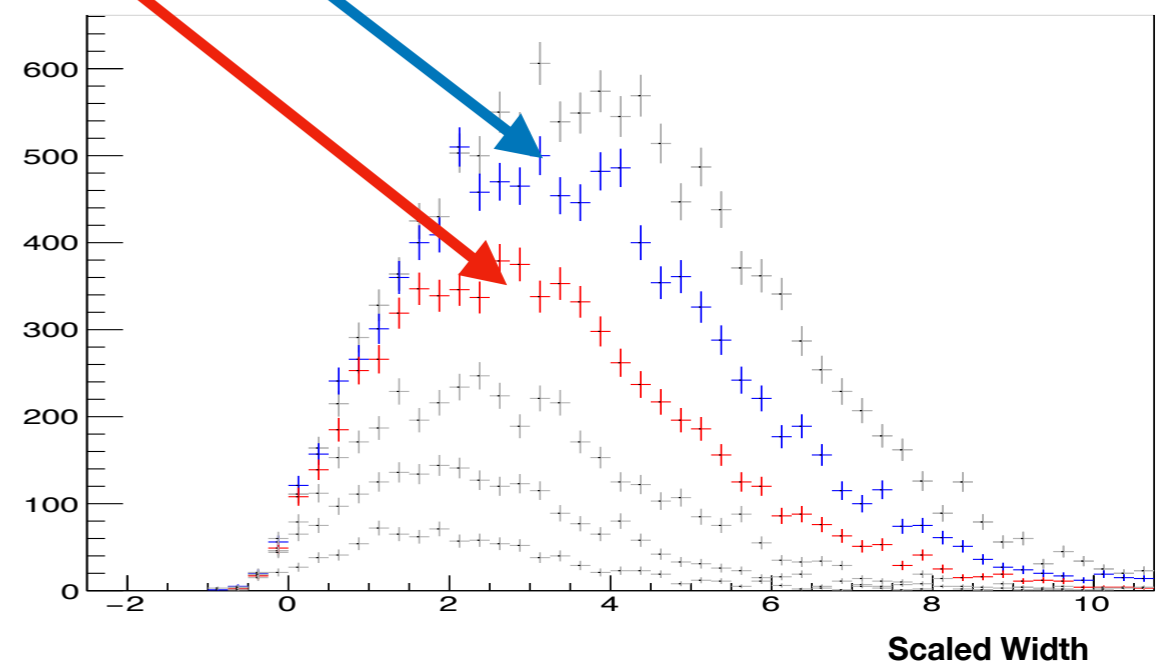
We will build a mapping function  $M$ , which transforms the blue layer to the red layer.

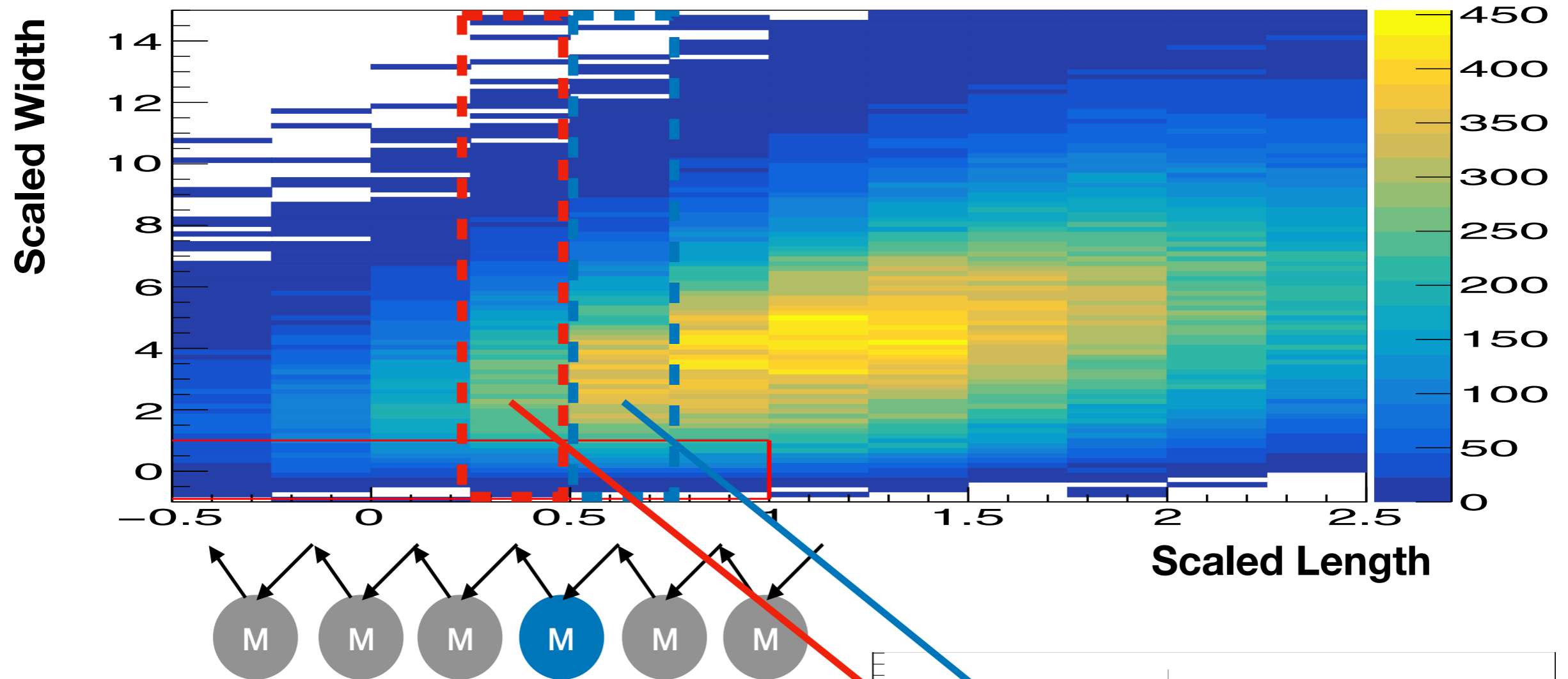




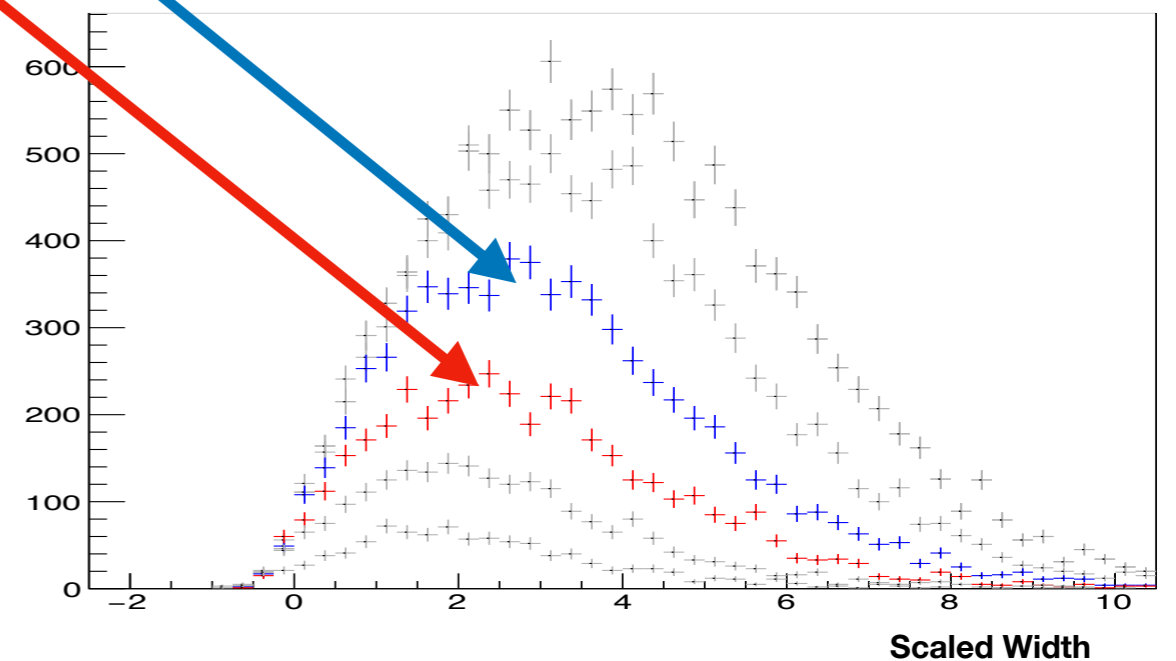


**If we succeeded, we can continue  
the same process for the next  
layer...**

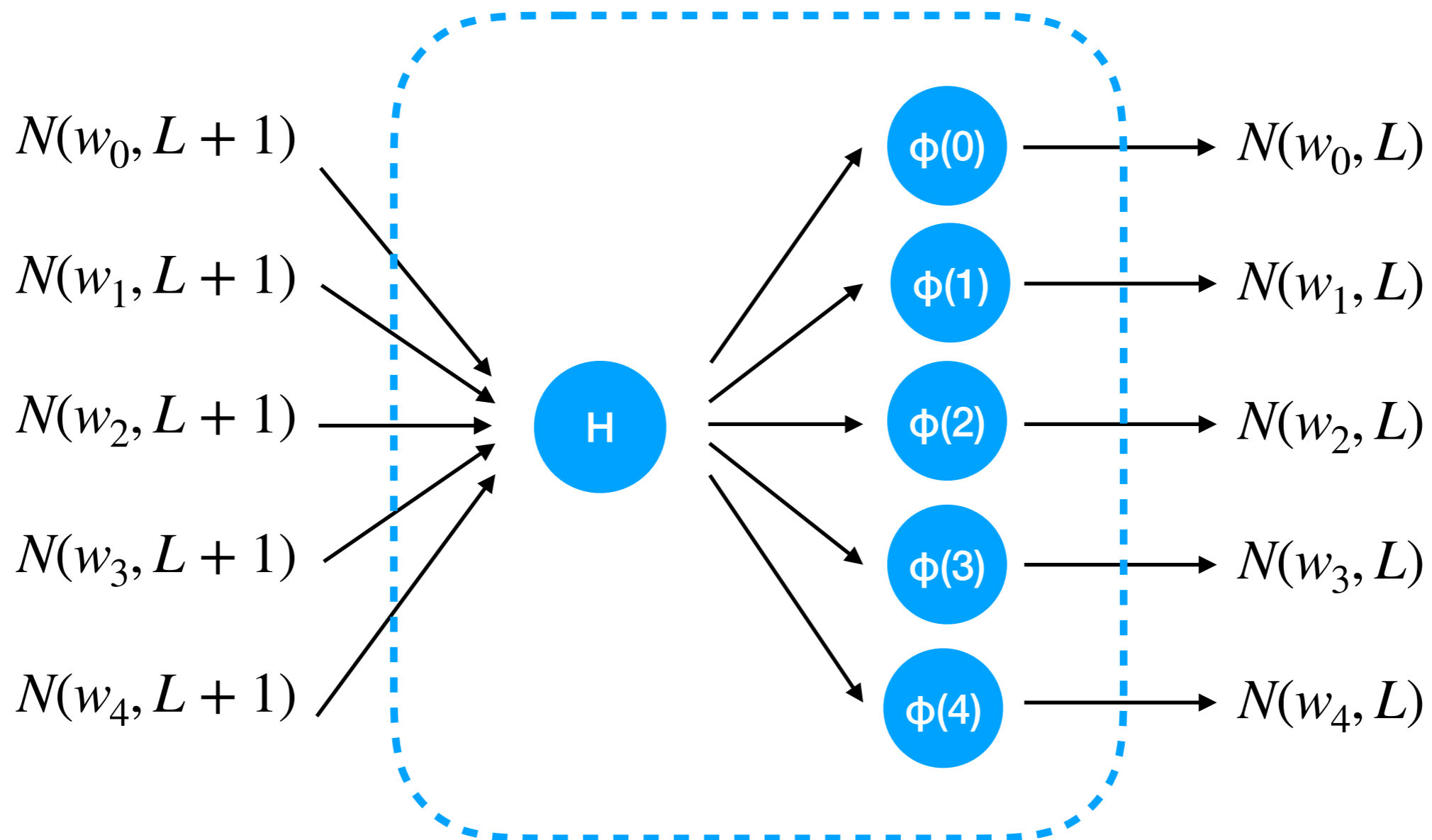




**... until we complete the prediction for the blinded region.**



Here is the structure of the mapping function:



$$N(w_i, L) = \phi(w_i) \sum H(w_i - w_j) N(w_j, L + 1)$$

**The inverse kernel in the mapping function has a Gaussian form:**

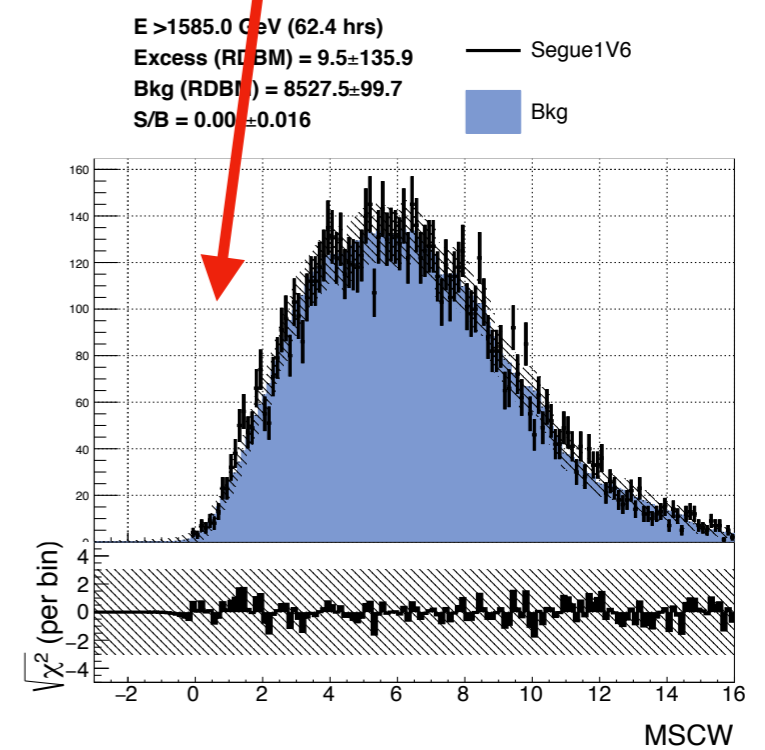
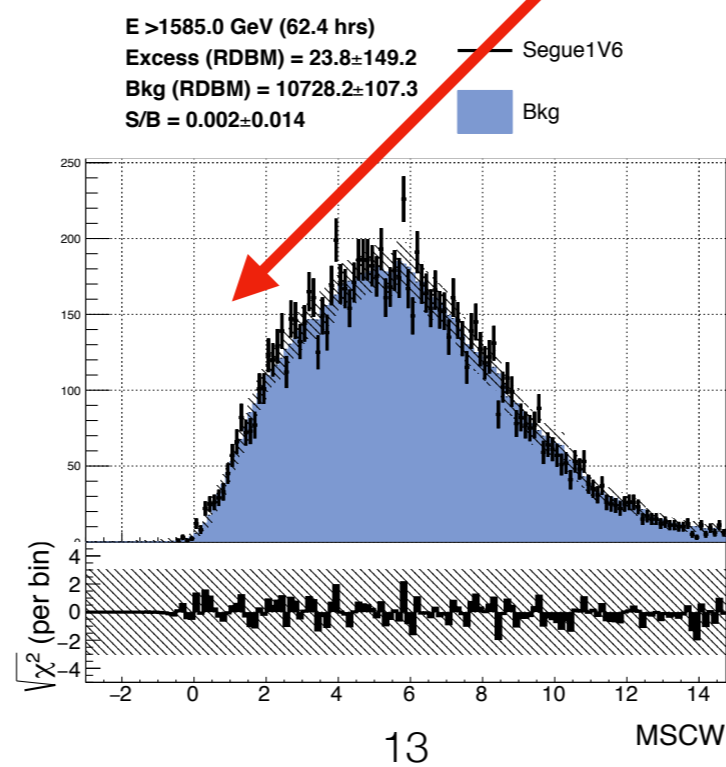
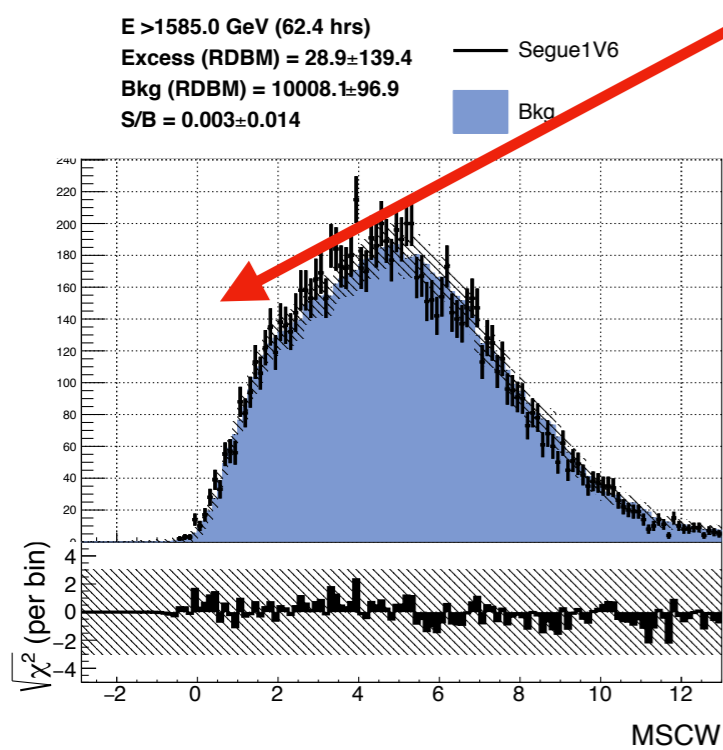
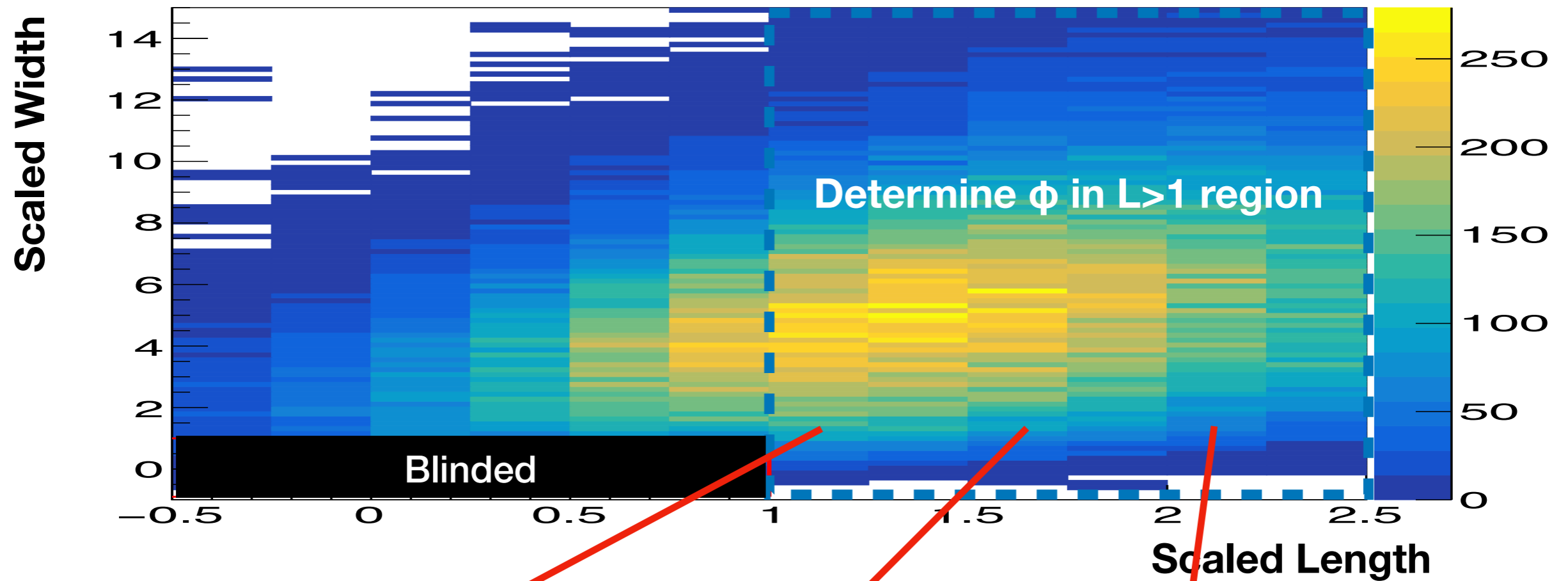
$$H^{-1}(w_i - w_j) = A \exp\left(-\frac{(w_i - w_j - x)^2}{2\sigma^2}\right)$$

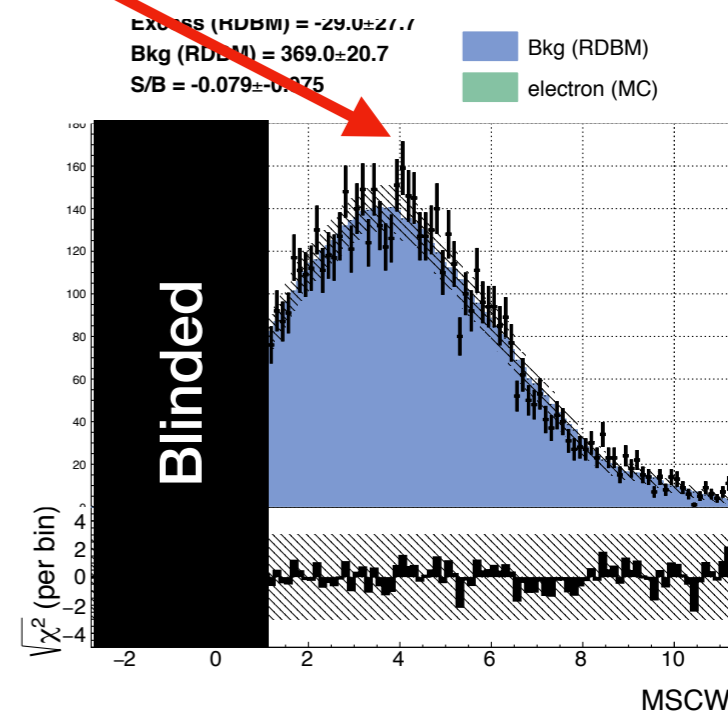
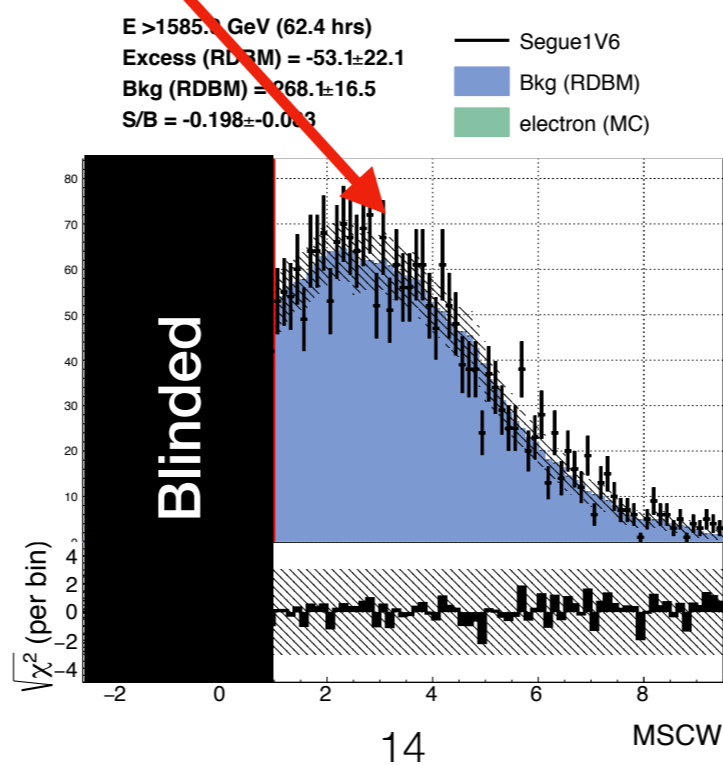
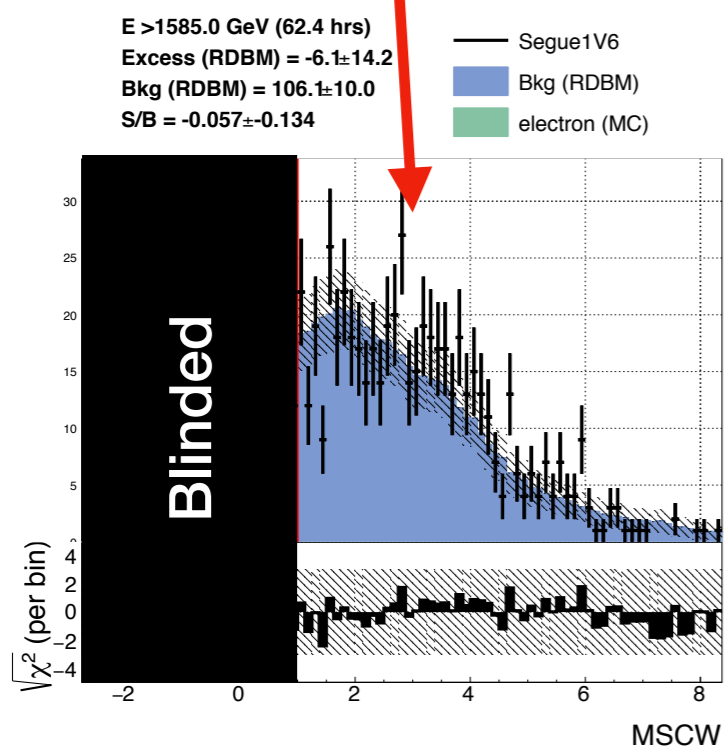
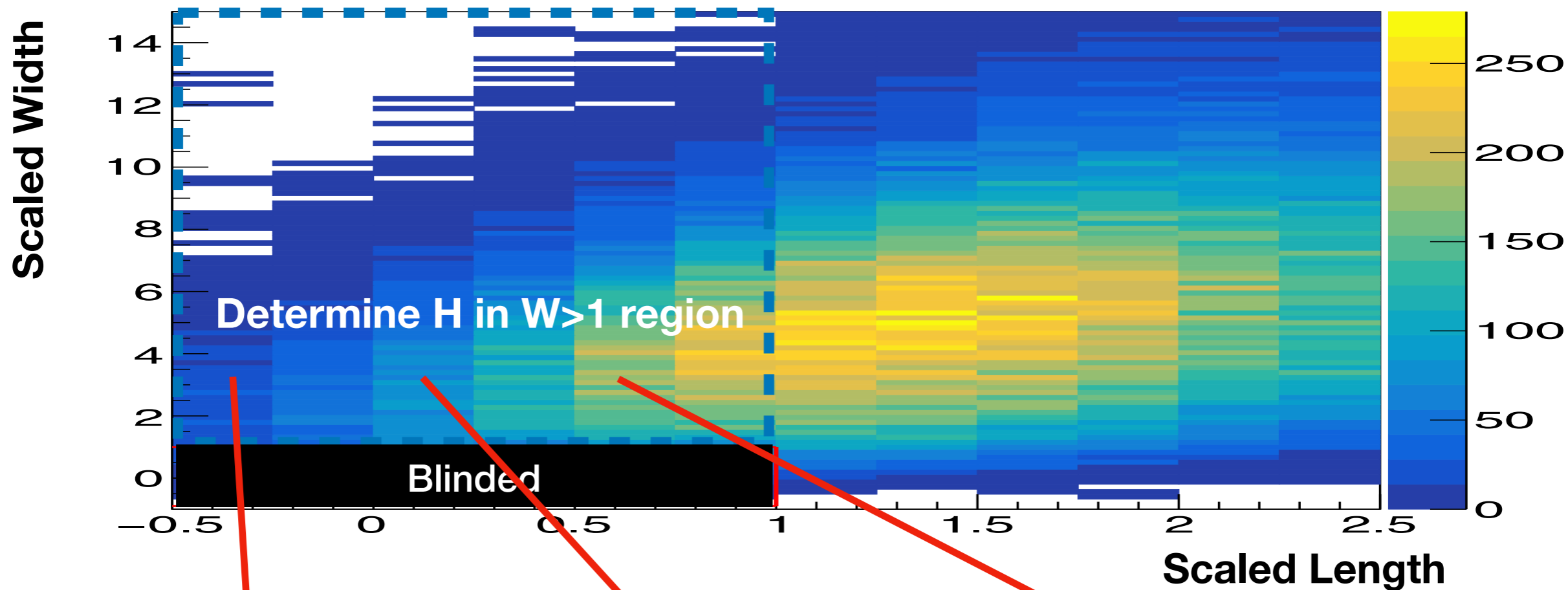
**And an activation function:**

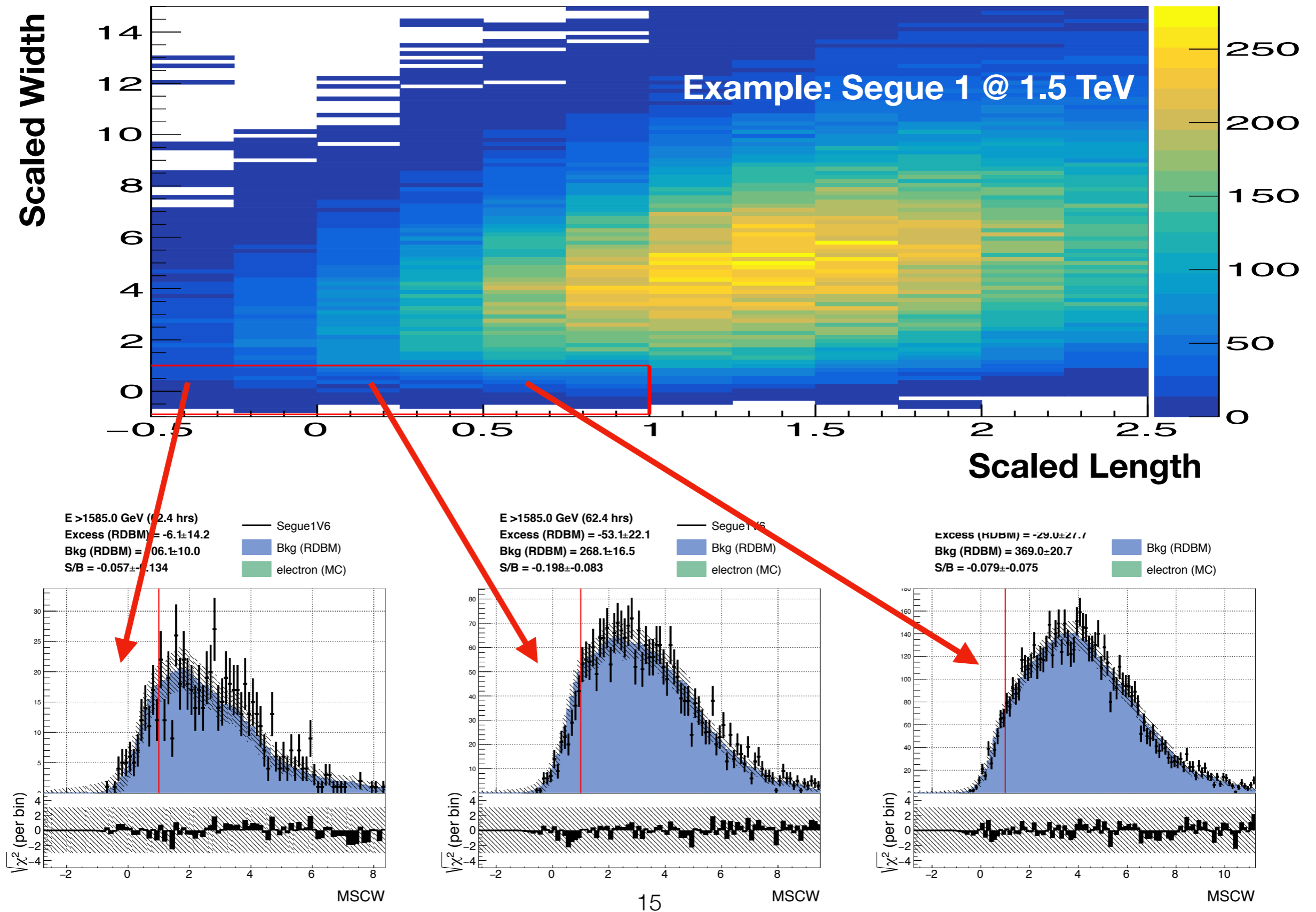
$$\phi(w_i) = \begin{cases} 1, & \text{if } w_i - t_1 \geq 0 \\ 0, & \text{if } w_i - t_2 \leq 0 \\ ((w_i - t_2)/(t_1 - t_2)), & \text{otherwise} \end{cases}$$

**These parameters are determined by minimizing:**

$$\chi^2 = \sum_{\text{unblinded}} \frac{(N_{data}(w) - N_{bkg}(w))^2}{\sigma_{data}^2 + \sigma_{bkg}^2}$$







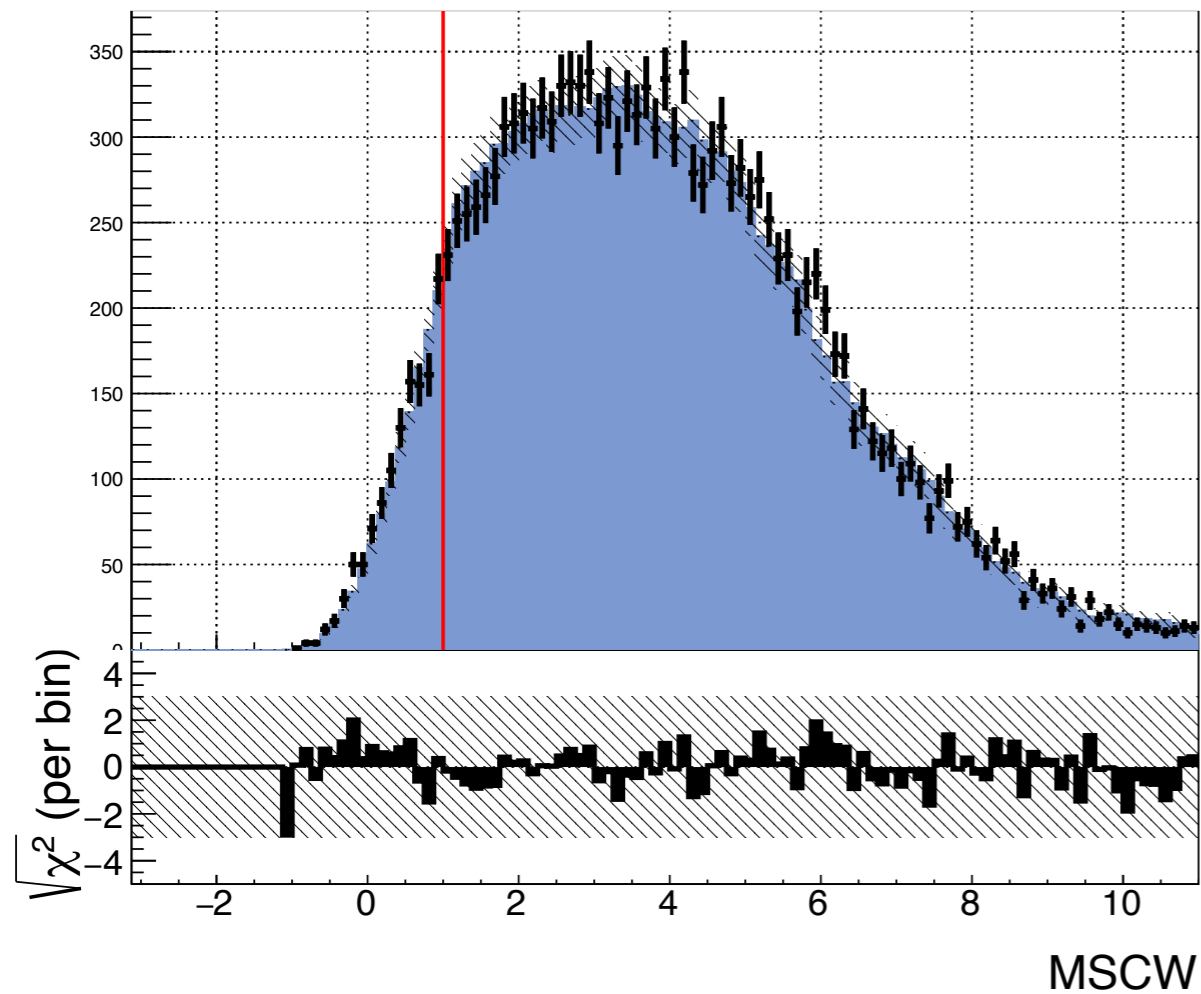
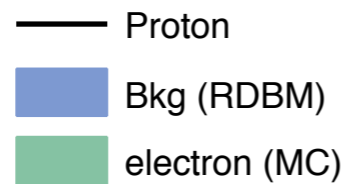
# Examples of Closure Tests

**E >2239.0 GeV (3.3 hrs)**

**Excess (RDBM) =  $54.3 \pm 45.3$**

**Bkg (RDBM) =  $1195.7 \pm 28.3$**

**S/B =  $0.045 \pm 0.038$**



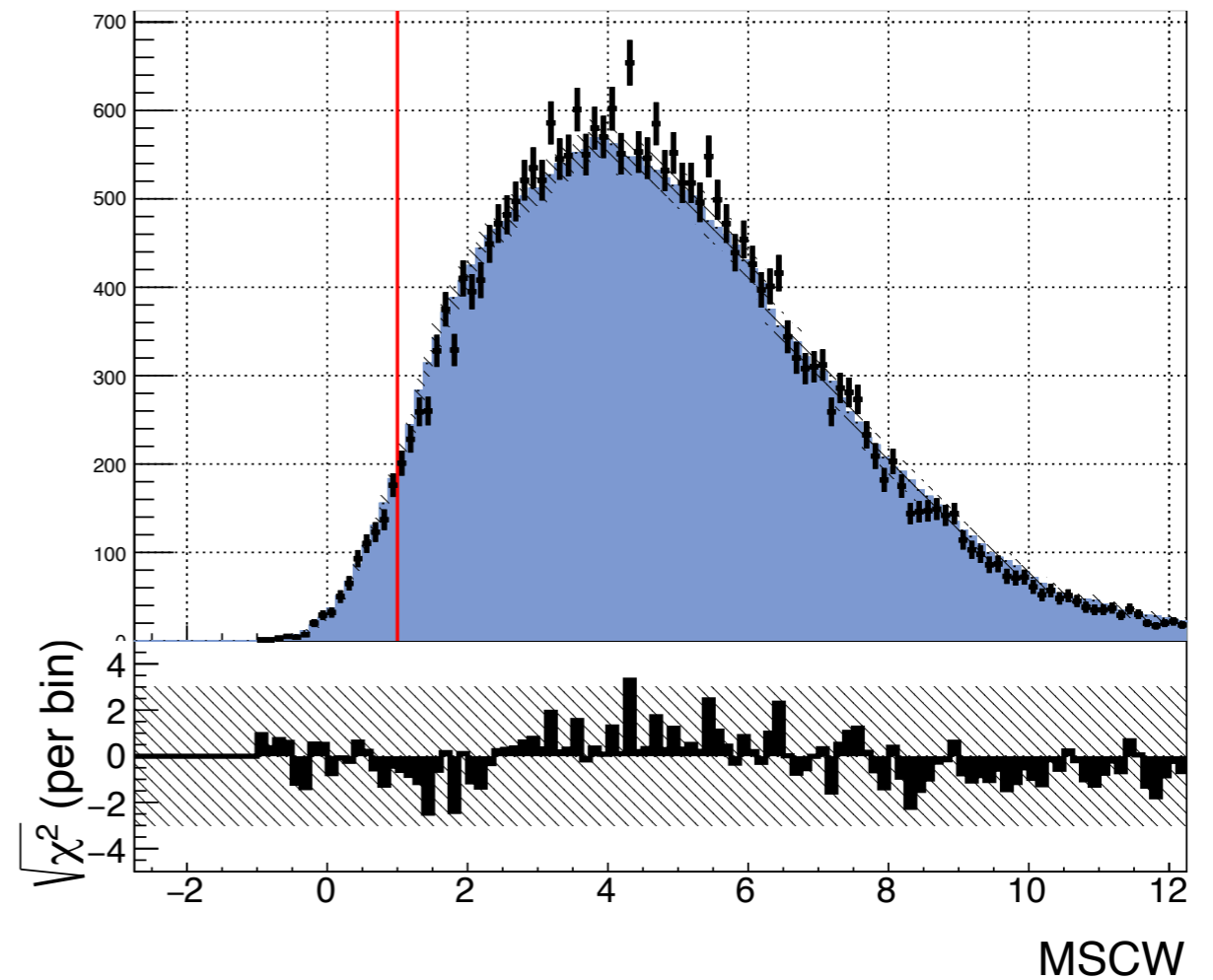
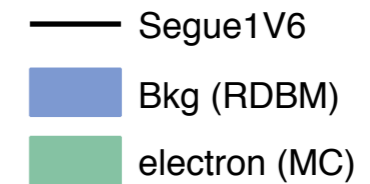
**Proton MC**

**E >2239.0 GeV (62.4 hrs)**

**Excess (RDBM) =  $-28.1 \pm 35.3$**

**Bkg (RDBM) =  $884.1 \pm 19.8$**

**S/B =  $-0.032 \pm 0.040$**



**Data from Segue 1**



# Conclusion

- Recurrent Deconvolution Background Method has a wide range of applications (**large clusters, Galactic halo**) for current and future gamma-ray telescope arrays.
- It utilizes the correlation between **longitudinal** and **lateral** shower developments and the idea of **Recurrent Neural Network**.
- It's **NOT a real neural network**. We impose strong constraints on the “neuron”, parameter space of the model is largely limited. But it also allows us to interpret the **parameters with physical meanings**.

**Backup**

# Example of validations on 8 point sources (ON region excluded)

