# PARTICLE ACCELERATION IN SUPERNOVA REMNANTS

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**LECTURE II** 

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### **OUTLINE**

- Maximum energy in Diffusive Shock Acceleration (DSA)
- Self-generation of magnetic waves
  - \* Resonant (streaming) instability
  - Non-resonant (Bell) instability
- Non-linear Diffusive Shock Acceleration (NLDSA)
  - Problems for the test-particle approach
  - ▶ Back reaction of accelerated particles
- Application to SNR shocks
  - Radiative processes
  - The role of scattering centers



### MAXIMUM ENERGY

### Is it possible to accelerate protons up to the knee?

The maximum energy is obtained comparing the acceleration time with the age of the accelerator and the energy losses

$$t_{acc} = min[t_{loss}, T_{age}]$$

$$E_{max}$$

Acceleration time:  $t_{\rm acc} = \frac{t_{\rm cycle}}{\Delta E/E}$ 

Energy losses are usually negligible for protons but are important for electrons

Time for one cicle upstream  $\rightarrow$  downstream  $\rightarrow$  upstream:  $t_{cycle} = \tau_{diff,1} + \tau_{diff,2}$ 

Equating the particle injected from downstream with the particles upstream:

$$\frac{nc}{4} \Sigma \tau_{\text{diff},1} = n \Sigma \frac{D_1}{u_1} \longrightarrow \tau_{\text{diff},1} = \frac{4D_1}{c u_1} \wedge \tau_{\text{diff},2} = \frac{4D_2}{c u_2}$$

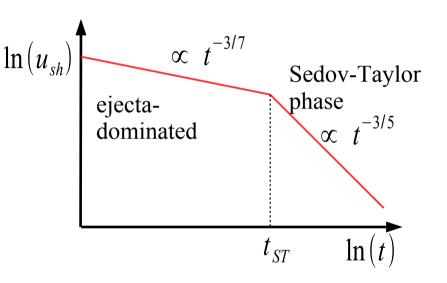
$$\frac{\Delta E}{E} = \frac{4}{3} \frac{u_1 - u_2}{c}$$

$$\frac{\Delta E}{E} = \frac{4}{3} \frac{u_1 - u_2}{c}$$

$$t_{acc} = \frac{t_{cycle}}{\Delta E/E} = \frac{3}{u_1 - u_2} \left(\frac{D_1}{u_1} + \frac{D_2}{u_2}\right) \approx 8 \frac{D_1}{u_{sh}^2}$$

### MAXIMUM ENERGY

## Maximum energy can increase only during the ejecta dominated phase of the SNRs because $u_{\rm sh} \sim const$



**Shock radius:** 
$$\begin{cases} R_{sh}(t) \propto t^{5/7} & \text{Ejecta-dominated} \\ R_{sh}(t) \propto t^{2/5} & \text{Sedov-Taylor} \end{cases}$$

But particles diffuse ahead of the shock:  $d \propto \sqrt{Dt}$ 

→ during the ST phase the highest energy particles cannot be catched by the shock and escape towards upsteam

Estimate of the beginning of the Sedov-Taylor phase:

$$\frac{1}{2} M_{ej} u_{sh}^{2} = E_{SN} 
\frac{1}{2} M_{ej} u_{sh}^{2} = E_{SN} 
\frac{4\pi}{3} \rho_{ISM} R_{ST}^{3} = M_{ej}$$

$$t_{ST} \approx 50 \left(\frac{M_{ej}}{M_{\odot}}\right)^{\frac{5}{6}} \left(\frac{E_{SN}}{10^{51} \text{erg}}\right)^{-\frac{1}{2}} \left(\frac{n_{ISM}}{\text{cm}^{-3}}\right)^{-\frac{1}{3}} \text{yr,}$$

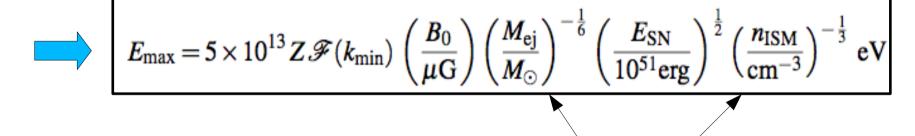


### MAXIMUM ENERGY

We use the diffusion coefficient from quasilinear theory:

$$D = \frac{1}{3} \frac{r_L v}{F(k_{res})}; \quad F(k) = \frac{\delta B_k^2}{B_0^2}$$

Equating the acceleration time with the end of the ejecta dominated phase  $t_{acc} = t_{ST}$ :



Emax is weakly dependent on the ejecta mass and ISM density

High energies, up to PeV, can be achieved only if  $\mathcal{F}(k) >> 1$ . This condition requires amplification of the magnetic field

**BUT WHAT PRODUCES THE TURBULENCE?** 



### TURBULENCE IN THE GALAXY

### The main origin of turbulence are thought to be SN explotion.

Turbulence is injected at a scale comparable with the size of SNR (or super-bubbles) and than cascades at smaller scales

Power injected at:

$$k_{min} = 1/L_0 \approx 50 \ pc$$

Kolmogorov cascade: 
$$P(k) = \frac{\delta B(k)^2}{B_0^2} \propto k^{-5/3}$$

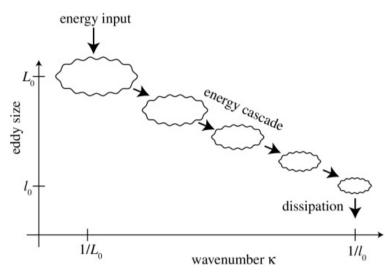
$$k_{res}(E_{max}) = \frac{1}{r_L(E_{max})} = 1 \times \left(\frac{E}{10^{15} eV}\right)^{-1} \left(\frac{B_0}{1 \mu G}\right) pc^{-1}$$

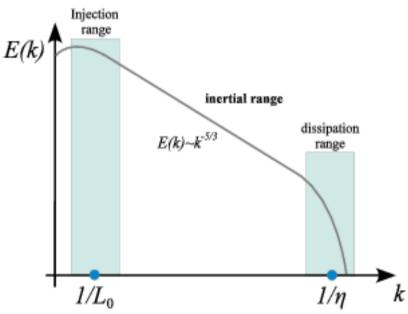


$$\frac{P(k_{res})}{P(k_{min})} = \left(\frac{k_{res}}{k_{min}}\right)^{-5/3} \approx 10^{-3} \left(\frac{E}{10^{15} eV}\right)^{5/3}$$



 $E_{max} < 10 \, GeV$ 





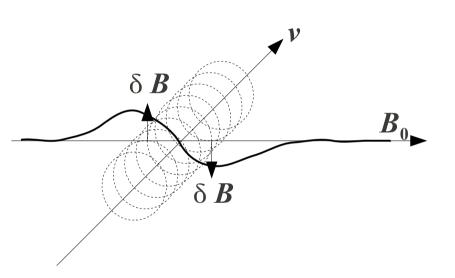
The Kolmogorow turbulence is not enough!

### SELF-GENERATION OF WAVES



### WHO GENERATES WAVES?

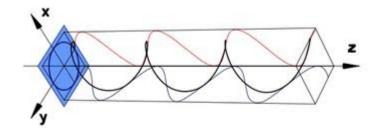
# WAVES MAY BE GENERATED BY DIFFERENT SOURCES (e. g. SN EXPLOSION) BUT THERE IS A MORE INTERESTING AND PHYSICALLY IMPORTANT PHENOMENON: SELF GENERATION



Charged particles moving transverse to the magnetic field line produce a variable magnetic field  $\delta B$  which perturb  $B_a$  producing an Alfvén wave.

→ Alfvén wave in turn scatter particles

The effect of scatter is to isotropize CRs.



Generated Alfvén waves are circularly polarized

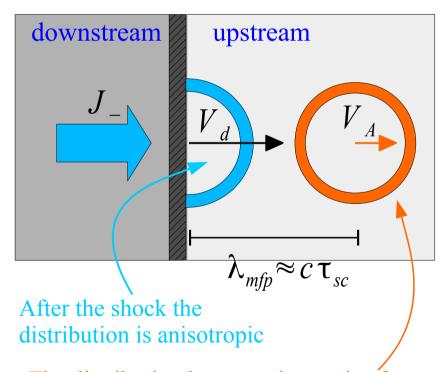


### SELF GENERATION OF WAVES: RESONANT INSTABILITY

WAVES MAY BE GENERATED BY DIFFERENT SOURCES (e. g. SN EXPLOSION) BUT THERE IS A MORE INTERESTING AND PHYSICALLY IMPORTANT PHENOMENON:

**SELF - GENERATION VIA RESONAT INSTABILITY** 

[e.g. Skilling (1975), Bell & Lucek (2001), Amato & Blasi (2006)]



The distribution becomes isotropic after one mean free path and moves at the same speed of the waves

Assume particles are drifting with  $v_d > v_A$  and are isotropyzed on a time-scale  $\tau_s$ :

$$\tau_{sc} \approx \frac{1}{v_{sc}} = \frac{\pi}{4} F(k) \Omega$$

**Initial momentum** 

final momentum

$$n_{CR} m \gamma_{CR} v_d \longrightarrow n_{CR} m \gamma_{CR} v_A$$

The momentum lost by particles is:

$$\frac{dP_{CR}}{dt} = \frac{P_2 - P_1}{\tau_{sc}} = \frac{n_{CR} m \gamma_{CR} (v_d - v_A)}{\tau_{sc}}$$



### SELF GENERATION OF WAVES: RESONANT INSTABILITY

The momentum lost is transferred to waves

Transport equation for waves:

$$\frac{dP_{CR}}{dt} = \frac{n_{CR} m \gamma_{CR} (v_d - v_A)}{\tau_{sc}}$$

$$v_A \frac{dP_W}{dt} = \Gamma_W \frac{\delta B^2}{8\pi}$$

Equating momentum lost by CR and momentum gain by waves

$$\frac{dP_{W}}{dt} = \frac{dP_{CR}}{dt} \longrightarrow \Gamma_{W} = \frac{n_{CR}}{n_{gas}} \Omega_{cyc} \left( \frac{v_{D} - v_{A}}{v_{A}} \right)$$

For  $n_{\rm CR} = 10^{-10}$  cm<sup>-3</sup>,  $n_{\rm gas} = 10^{-1}$  cm<sup>-3</sup> and  $B_0 = 1 \mu G$ , and assuming  $v_{\rm d} = 2 v_{\rm A}$ , one finds:

$$V_{A} = 7 \ 10^{5} \text{ cm/s}$$
 $\Omega_{cyc} = 10^{-2} \text{ s}^{-1}$ 
 $\Gamma_{W} = \frac{n_{CR}}{n_{gas}} \Omega_{cyc} \left( \frac{v_{D} - v_{A}}{v_{A}} \right) \approx 10^{-3} \text{ yr}^{-1}$ 
VERY RAPID GROWTH



# HOW MUCH THE SELF-GENERATED TURBULENCE CAN GROW?

Turbulence can grow for at most one advection time

$$t_{adv} = D_1/u_{sh}^2$$

Equating the grow time with the advection time we get the maximum level of turbulence at the shock:

$$t_{adv} = t_{grow} = 1/\Gamma_W$$

$$F_0(k) = \frac{\pi}{2} \frac{\xi_{CR}}{\ln(p_{max}/m_p c)} \frac{u_{sh}}{v_A} \approx 10$$

$$\begin{cases} \xi_{CR} = P_{CR} / (\rho u_{sh}^2) \sim 0.1 \\ u_{sh} \sim 5000 \, km/s \\ v_A \sim 10 \, km/s \\ p_{max} \sim 10^5 \, GeV \end{cases}$$

The condition F(k) >> 1 violates the quasi-linear theory used to derive the growth time.

A more realistic estimate including the modification to the dispertion relation induced by CRs gives:

Self-amplification can produce  $\delta B \sim B_0$ 

$$F_0(k) = \left(\frac{\pi}{6} \frac{\xi_{CR}}{\ln(p_{max}/m_p c)} \frac{c}{u_{sh}}\right)^{1/2} \le 1$$



$$E_{max} \approx 10^{13} - 10^{14} eV$$



### **NON-RESONANT AMPLIFICATION**

There are other possibilty to amplify the magnetic field.

The most invoked one is the non-resonant Bell instability [Bell, A.R. (2004)]

This instability is excited by the force

$$\vec{j}_{CR} \times \delta \vec{B}$$

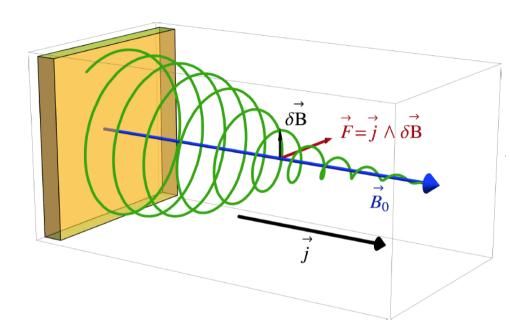
where the current is due to escaping particles upstream.

It amplifies almost purely growing waves with wavenumbers much greater

than the inverse particle gyroradius.

**→** works for very high shock velocity (initial phase of SNR expansion)

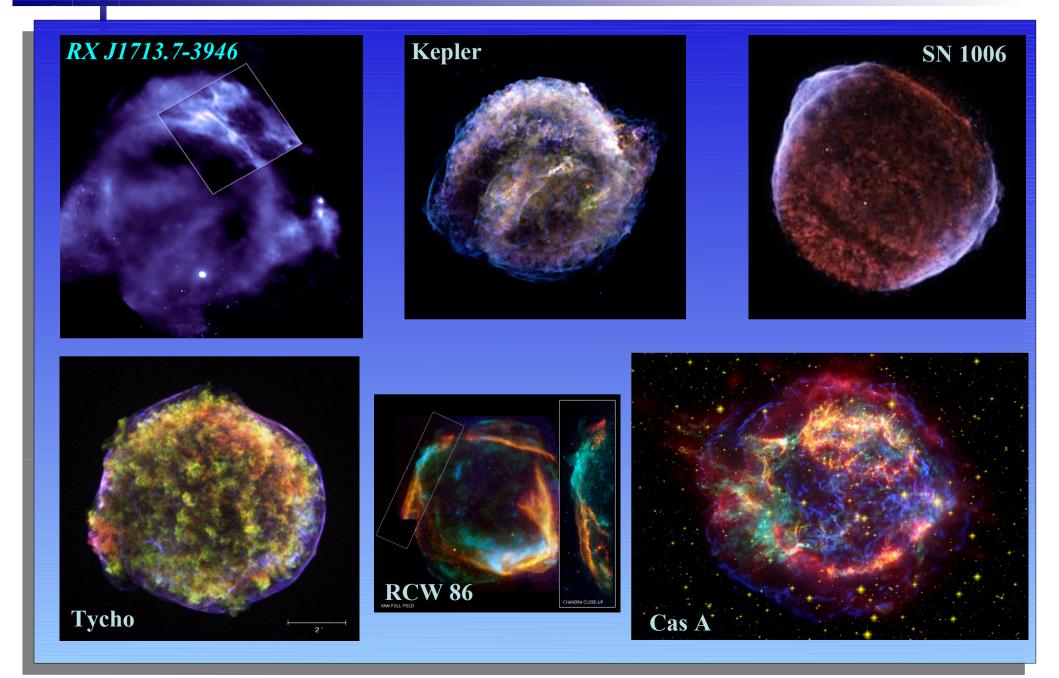
We can have 
$$\frac{\delta B}{B_0} > 10$$
 if  $\xi_{CR} = \frac{P_{CR}}{\rho u_{sh}^2} > 0.1$ 



Simulation from Revill & Bell (2013)

### DO WE SEE MAGNETIC FIELD AMPLIFICATION?

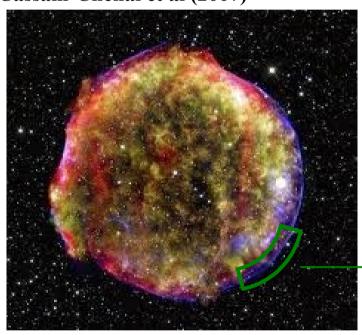
### Galactic SNRs in X-rays





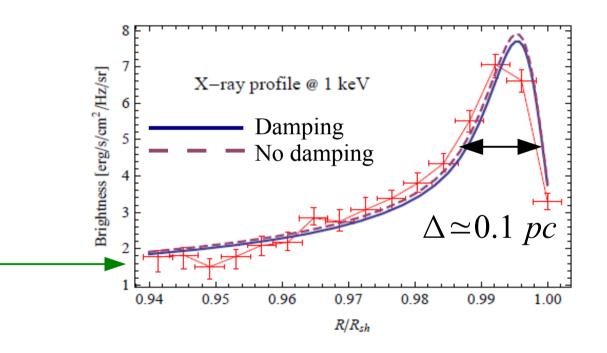
### Evidences for magnetic field amplification

Chandra X-ray map.
Data for the green sector are from Cassam-Chenaï et al (2007)

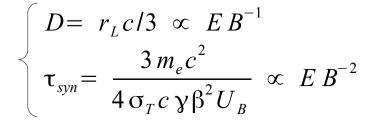


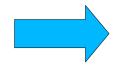
Thin non-thermal X-ray filaments provide evidence for magnetic field amplification

[Hwang el al(2002); Bamba et al (2005)]



$$\Delta \simeq \sqrt{D \tau_{syn}} \propto B^{-3/2}$$

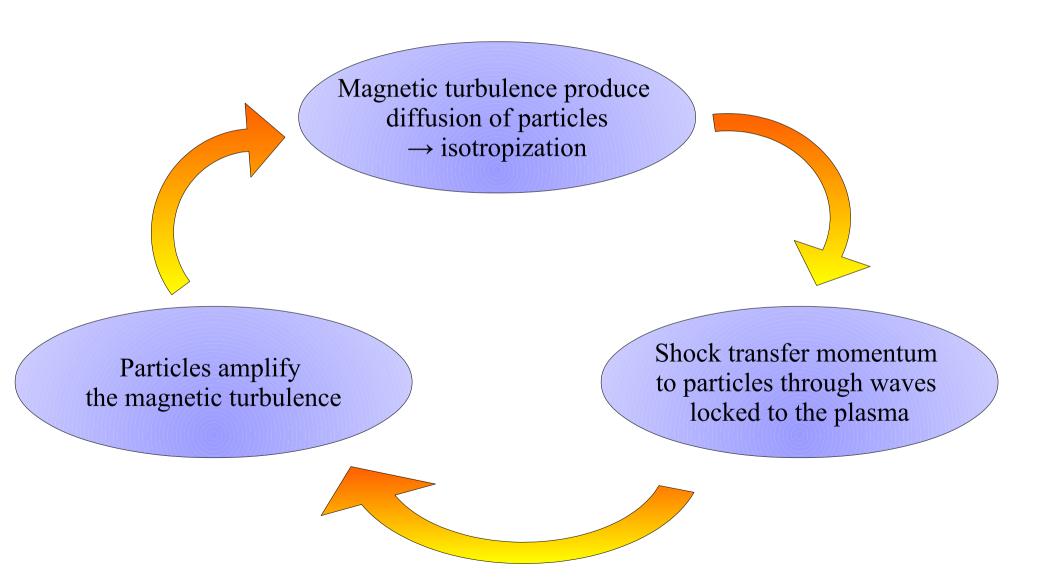




*B*~200-300 μG



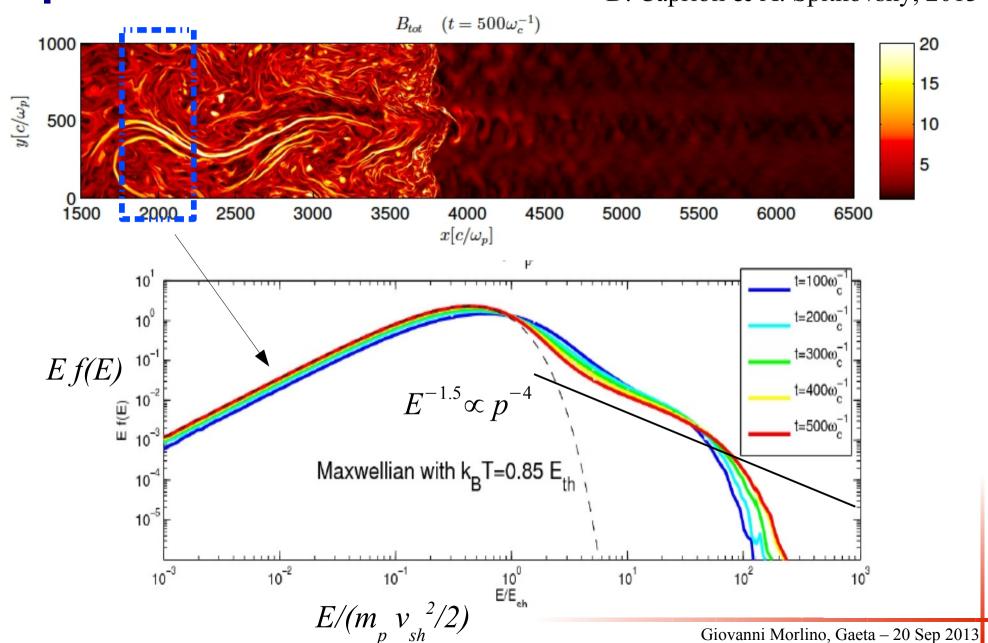
### THE ESSENCE OF NON-LINEARITY





### SIMULATIONS: results for the spectrum

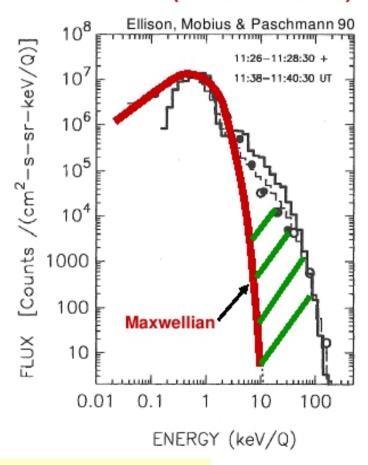
D. Caprioli & A. Spitkovsky, 2013

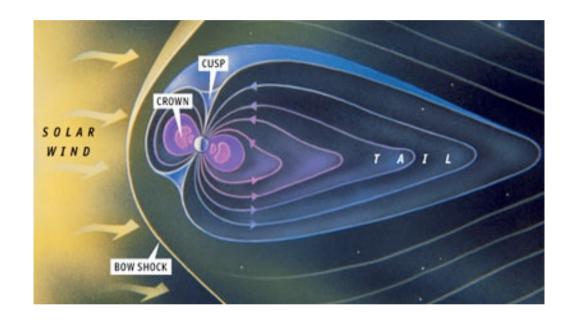




# **Evidence for efficient shock acceleration** in Earth bow shock

### Earth Bow Shock (direct evidence)





>25% of energy flux in superthermal ions



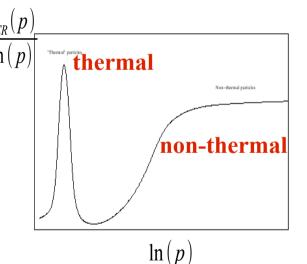
### **Problems with linear theory**

### 1 - Observation: CRs power

**Lower Limit!! (Average value)** Instantaneous power can be greater

### 2 – Theory: CRs pressure

$$P_{CR} \propto \int d \ln(p) \ v(p) p^4 f_{CR}(p) \quad \Rightarrow \quad \frac{P_{CR}}{P_{gas}} \approx 2.3 \ \xi \left(\frac{\eta}{10^{-5}}\right) \ln\left(\frac{p_{max}}{10^5 GeV/c}\right) \left(\frac{T}{10^5 K}\right)^{-1/2}$$



### 3 – Theory: Maximum CR energy

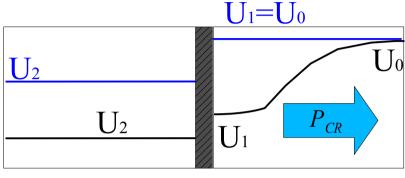
Linear theory (with self generated magnetic turbulence) predict for protons

$$\delta B < B_{Gal} \Rightarrow E_{max} \le 10^4 GeV$$

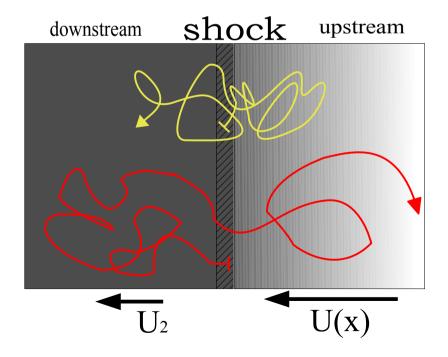
**BUT** 
$$E_{knee} \simeq 3 \cdot 10^5 \, GeV$$



### **Including the CR Back-Reaction**



velocity profile u(x)



What happen when non-thermal particles exert non negligible pressure?

1 – CRs pressure compresses the gas upstream

**→** The subshock compression factor decreases

$$r_{sub} = \frac{U_1}{U_2} < 4$$

2 – CRs subtract energy from the downstream plasma which becomes more compressible

**→** The total compression factor increases

$$r_{tot} = \frac{U_0}{U_2} > 4$$

Particles feel a different compression factor depending on their momentum

$$r(p) = \frac{\bar{U}(p)}{U_2}$$

$$\downarrow$$

$$n(E) = E^{-s(p)}$$

We expect a momentum dependent slope



### **Basic equations**

### **Transport equation for CRs**

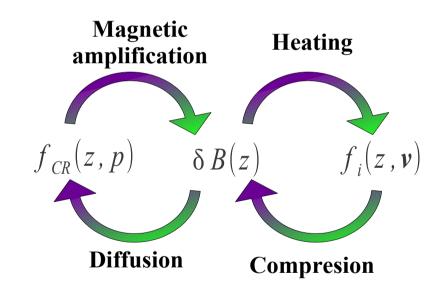
$$\frac{\partial}{\partial z} \left[ D(z, p) \frac{\partial f_{CR}}{\partial z} \right] - u \frac{\partial f_{CR}}{\partial z} + \frac{1}{3} \frac{du}{dz} p \frac{\partial f_{CR}}{\partial p} = 0$$

### Fluid equations couple CRs + ions + waves

$$\frac{\partial}{\partial z} \left[ \rho_i u_i \right] = 0$$

$$\frac{\partial}{\partial z} \left[ \rho_i u_i^2 + P_i + P_{CR} + P_W \right] = 0$$

$$\frac{\partial}{\partial z} \left[ \frac{1}{2} \rho_i u_i^3 + \frac{\gamma}{\gamma - 1} P_i u_i + F_W \right] = -u \frac{\partial P_{CR}}{\partial z} + \Gamma_W$$

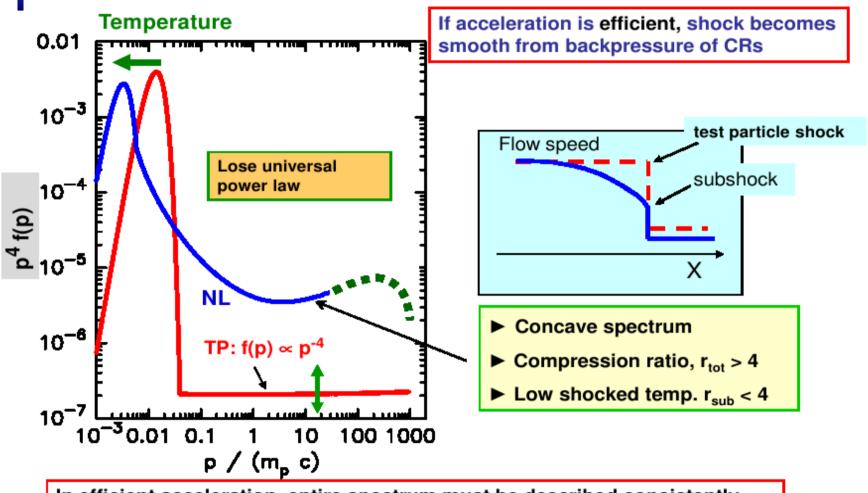


### Transport equation for magnetic field

$$\frac{\partial F_{w}}{\partial z} = u \frac{\partial P_{w}}{\partial z} + P_{w} \left[ \sigma_{CR}(k, z) - \Gamma(k, z) \right]$$



### **Including the CR Back-Reaction**



In efficient acceleration, entire spectrum must be described consistently, including escaping particles

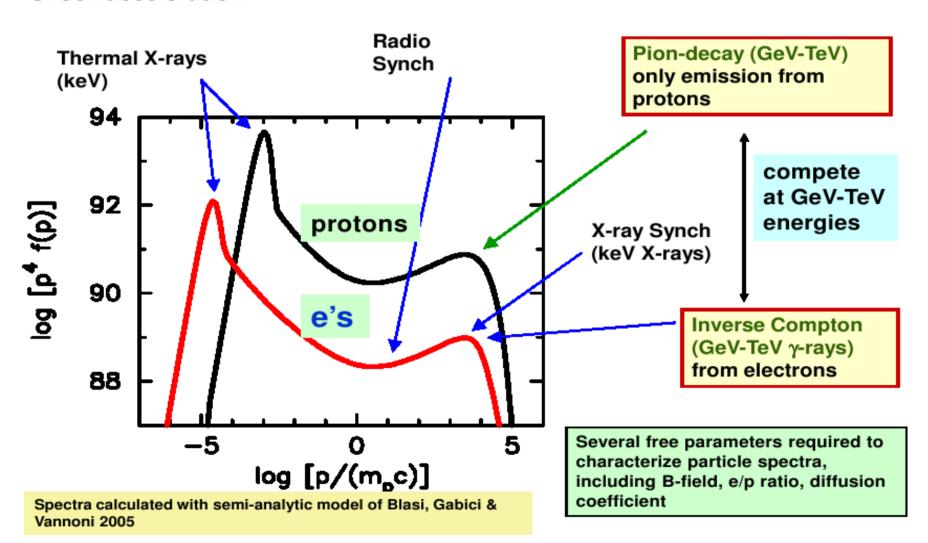
much harder mathematically

BUT, connects photon emission across spectrum from radio to  $\gamma$ -rays



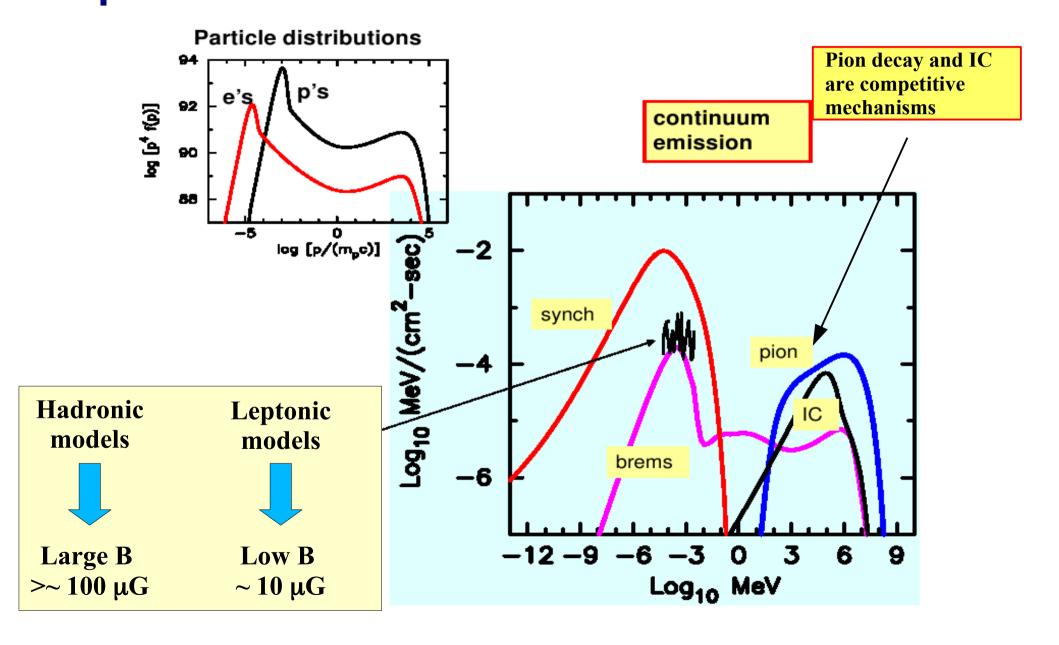
### EM radiation from accelerated particles

Electron and Proton distributions from efficient (nonlinear) diffusive shock acceleration



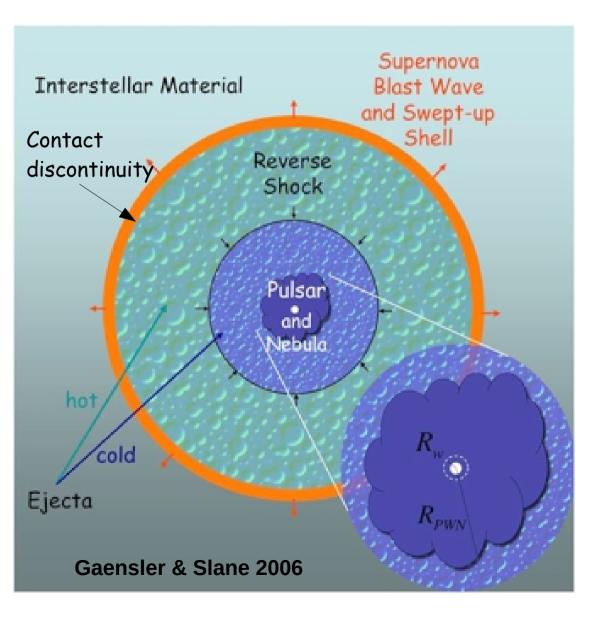


### EM radiation from accelerated particles



### APPLICATION TO ISOLATED SNRs

### **SNR** structure



### **SNR structure**

- ◆ ISM
- Forward shock
- Shocked ISM
- Contact discontinuity
- Shocked ejecta
- Reverse shock
- Unshocked ejecta

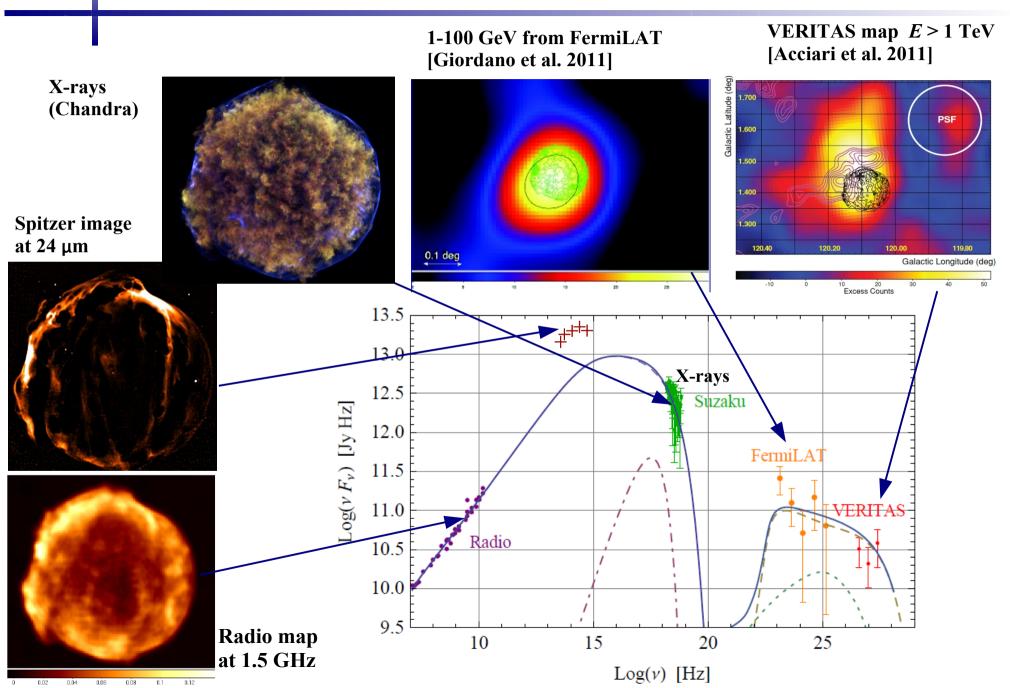
### For core-collapse SNR

- → PWN
- Termination shock
- Pulsar wind
- Pulsar

WHERE NON-THERMAL PARTICLE ARE PRODUCED?



### Tycho's SNR (Type Ia SNR)





### **Look for PeVatrons in known SNRs**

### Summary of shell SNRs emitting TeV gamma rays

NAME	Age [yr]	Distance [kpc]	Flux(>1TeV) [10 <sup>-12</sup> cm <sup>-2</sup> s <sup>-1</sup> ]	T <sub>TeV</sub> Spectral index	Evidence of cutoff	E <sub>γ,max</sub> [TeV]
Cas A North.	em. 330	3.4	0.77±0.11	2.61±0.24	(?)	5
Tycho	440	3.3	0.19±0.05	1.95±0.6 $\Gamma_{\text{GeV-TeV}}$ =2.2	(?)	10
SN 1006 (NE)	1000	2.2	0.23±0.05	2.36±0.2	(?)	20
SN 1006 (SW)	п	II .	0.15±0.05	2.43±0.2	(?)	6
RX J1713.7- 3946	~1600	1	15.9±0.6	2.32±0.01	YES @10TeV	80
RX J0852 (Vela Jr.)	420-1400 (best ~700)	200 pc - 1 kpc	15.2±3.2	2.24±0.15	YES	10
RCW 86	1600	~2.5	2.34	2.54	(?)	20
G353.6-0.7	~14000(?)	3.2(?)	6.91±0.75	2.32±0.06 (	NO	30

Maximum detected energy in  $\gamma$ -rays. In case of hadronic model  $E_{\rm p,max} \sim 10 E_{\rm y,max}$ 



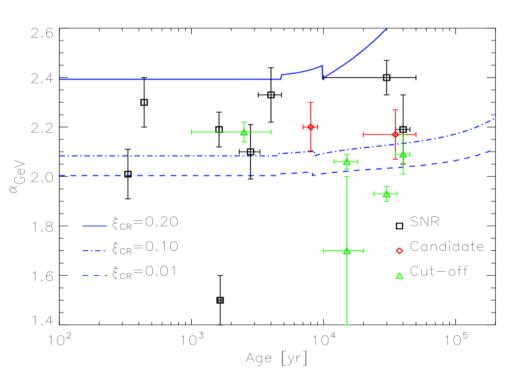
### Slope of gamma-ray emission of SNRs

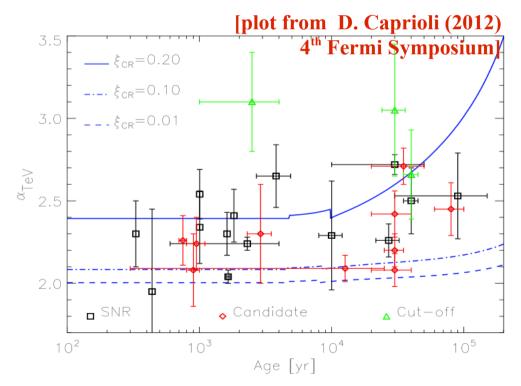
# In many observed SNRs the slope is steeper than E<sup>-2</sup> difficult to explain theoretically

If the y-ray spectrum is hadronic  $(\pi^0 \to \gamma \gamma)$  the slope is the same as the proton spectrum

If the  $\gamma$ -ray spectrum is leptonic (IC) the spectrum is harder

$$f_e(E) \propto E^{-s} \rightarrow \phi_{\gamma} \propto E^{-(s-1)/2}$$

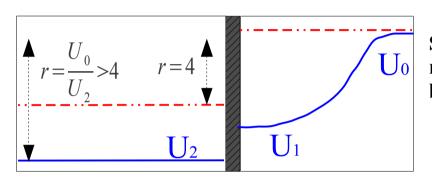






# The role of scattering centers in presence of strong magnetic amplification

In the standard NLDSA the CR pressure modifies the shock structure in such a way to produce concave particle spectra with spectral slope < 2 at higher energies



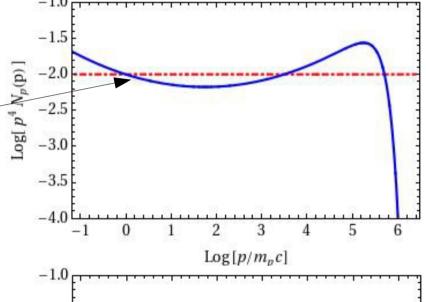
Shock modified by CRs

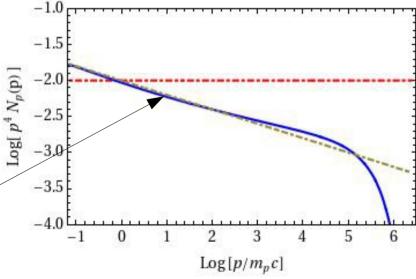
When the magnetic field is strongly amplified the Alfvén speed upstream can become a non negligible fraction of the shock speed. In this case the effective compression ratio is:

$$r = \frac{u_1 - v_{A,1}}{u_2 \pm v_{A,2}} \simeq \frac{u_1 - v_{A,1}}{u_2}$$

Downstream  $v_{A,2} \approx 0$  because of helicity mixing. In the case of Tycho:

$$v_{A,1} = \frac{B_1}{\sqrt{4\pi\rho_1}} \approx 0.15 V_{sh} \rightarrow s = \frac{r+2}{r-1} \approx 4.2$$
 (2.2 in energy)

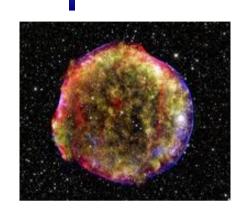






### Modelling the multi-wavelength spectrum of Tycho

[G.M. & D. Caprioli, 2012]



Simultaneous fit of multi-wavelength spectrum with non-linear DSA model

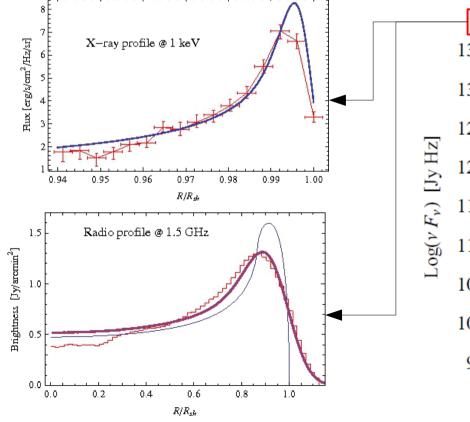
- 1) Maximum energy of ions
- 2) Non-thermal spectrum
- 3) Amplified magnetic field
- 4) TOTAL CRs ENERGY

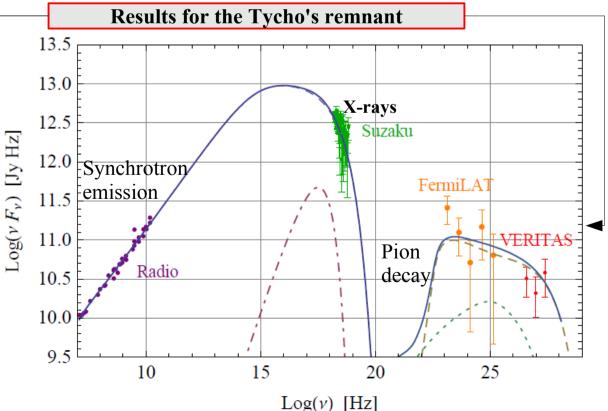
$$E_{max} = 470 \, TeV$$
$$N(E) \propto E^{-2.3}$$

$$N(E) \propto E^{-2\pi}$$

$$\delta B_2 \approx 300 \,\mu G$$

$$\epsilon_{\rm CR} = 12\% E_{\rm SN}$$







### Application to the Kepler's SNR

[D. Caprioli & G.M., preliminary results]

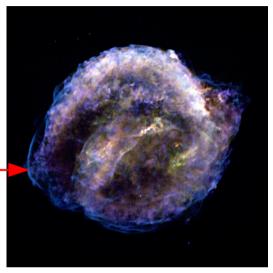
The Kepler's Remnant shows remarkable similarities with Tycho:

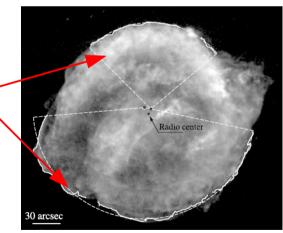
- → both originate from Type Ia SN
- $\rightarrow$  similar age (408 vs 440 yrs)
- $\rightarrow$  similar radio spectral index (0.64 vs 0.65)
- → presence of non-thermal X-ray emission in thin filaments

### But also differences:

- → Kepler is not detected in gamma rays (larger distance?)
- → Several north-south asymmetry has been detected
  - Radio and X-ray emission more pronounced in the North
  - different shock speed
  - different expansion rate

Due to expansion in a non-uniform CSM (probably progenitor's wind?)





Chandra X-ray map. From Katsuda et al (2008)

We apply a model similar to the one used for Tycho: results must be taken with care because we use uniform CSM density



### Multi-wavelength spectrum of Kepler

[D. Caprioli & G.M., preliminary results]

### **Assumed**

$$E_{SN} = 10^{51} erg$$

$$M_{eje} = 1 M_{sol}$$

$$T_{SNR} = 400 yr$$

$$f(v) \propto (v/v_{eje})^{-7}$$

### **Fitted**

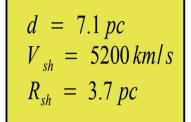
$$n_0 = 0.3 p/cm^3$$
  

$$\xi_{inj} = 3.7$$
  

$$\chi_{esc} = 0.1 R_{sh}$$
  

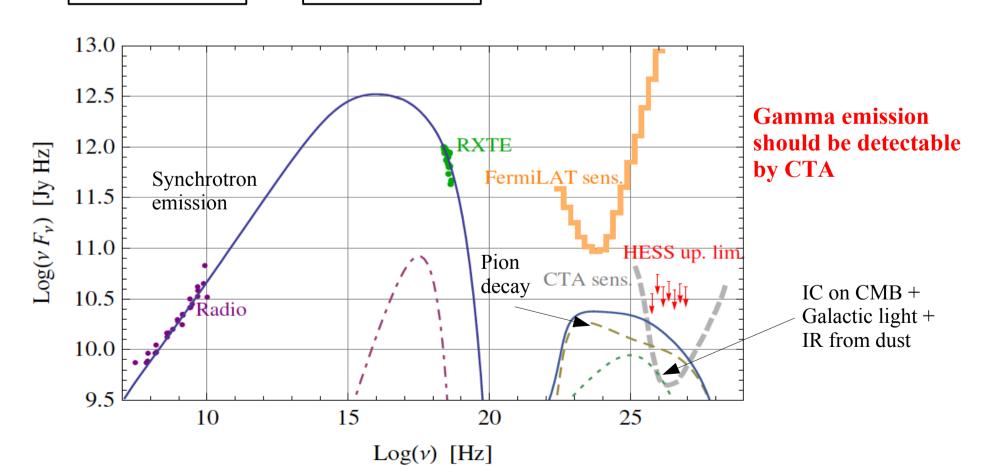
$$K_{ep} = 2.8 \times 10^{-3}$$

### **Inferred**



**CR** efficiency

 $\epsilon_{+} \simeq 12\%$ 





0.002

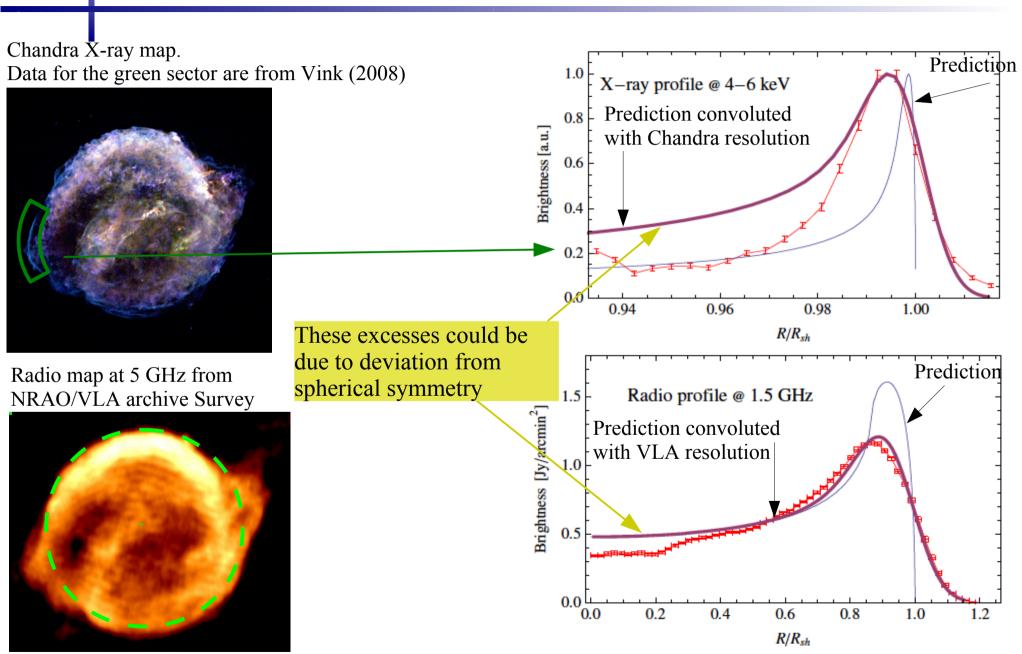
0.006

0.014

0.01

### Radial profile of X and radio emission for Kepler

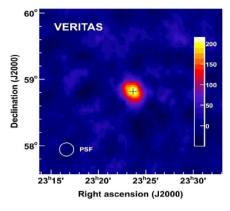
[D. Caprioli & G.M., preliminary results]





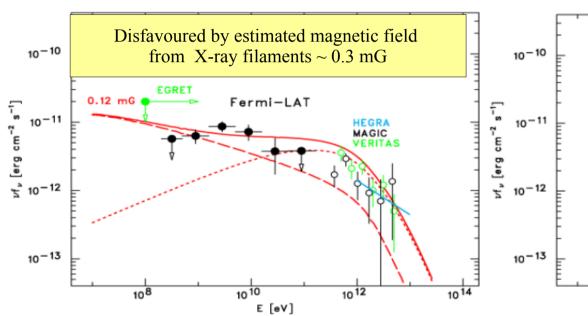
Cta
Cherenkov telescope array

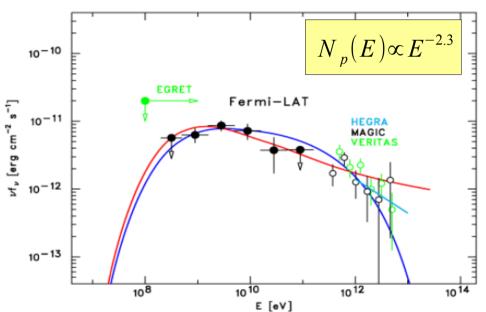
Cas A in TeV (VERITAS)



Cas A in X-rays (Chandra)







**Leptonic Model** 

B=120μG, PL (-2.34) + cutoff @ 40 TeV Dashed Line – Bremsstrahlung Dotted Line – IC (dominated by FIR)

Hadronic Models

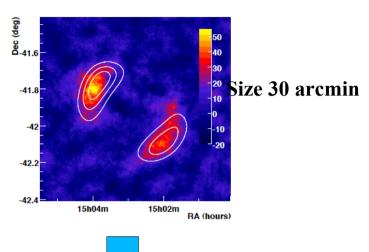
Blue: PL (-2.1) + cutoff @ 10 TeV Red: PL (-2.3)

Hadronic model is favored, but leptons not ruled out

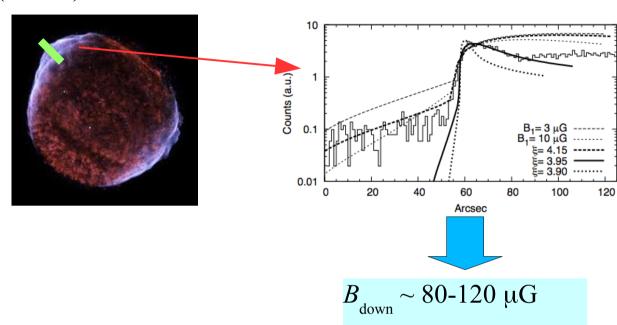
Abdo et al. ApJL 710 (2010)



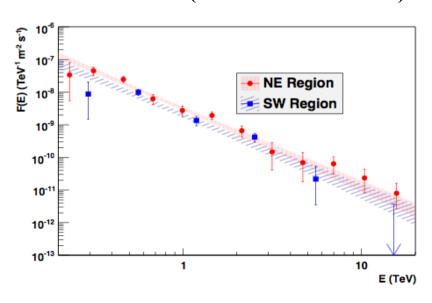
SN 1006 in TeV (HESS)



SN 1006 in X-rays (Chandra)



HESS data (130 hrs of observation)

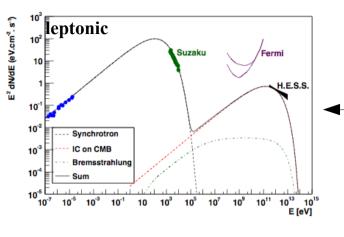


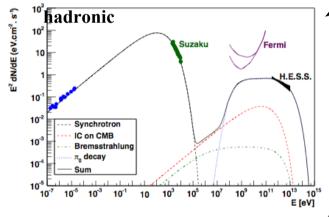
The magnetic field amplification is occurring upstream!!

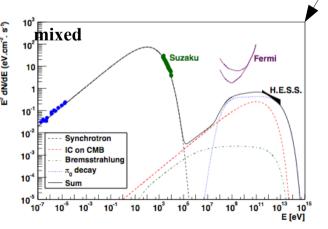
### Total gamma-ray flux <~ 1% Crab

Region	photon index Γ	Φ(> 1TeV)		
	_	$(10^{-12} \text{cm}^{-2} \text{s}^{-1})$		
NE	$2.35 \pm 0.14_{stat} \pm 0.2_{syst}$	$0.233 \pm 0.043_{stat} \pm 0.047_{syst}$		
SW	$2.29 \pm 0.18_{stat} \pm 0.2_{syst}$	$0.155 \pm 0.037_{stat} \pm 0.031_{syst}$		









### Model fit parameters from Aharonian et al.(2014), arXiv:1004.2124

Model	$E_{cut,e}$	$E_{cut,p}$	$W_e$	$W_p$	В
	[TeV]	[TeV]	[10 <sup>47</sup> erg]	[10 <sup>50</sup> erg]	[μ <b>G</b> ]
Leptonic	10	-	3.3	-	30
Hadronic	5	80	0.3	3.0	120
Mixed	8	100	1.4	2.0	45

### Leptonic model (1 zone):

- Explain the integrated gamma-ray flux
- Fails to explain the steep spectrum
- ♣ Requires low B, contrary to what inferred from observed thin X-ray rim (B~120 μG)

### Hadronic model (1 zone):

- ♣ Requires efficiency ~ 30%
- $\downarrow$  1) Steep spectrum  $E^{-2.3}$  with  $E_{\text{cut}} >> 100 \text{ TeV}$
- 2) hard spectrum E<sup>-2</sup> with E<sub>cut</sub>~80 TeV

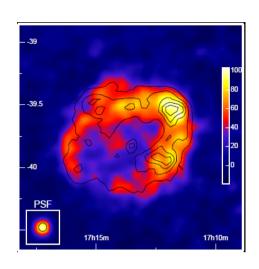
### How to distinguish between the two scenarios?

- At high energies X-rays come from downstream while IC photons come from upstream → 1' resolution will be able to detect a displacement between X-rays and γ-rays

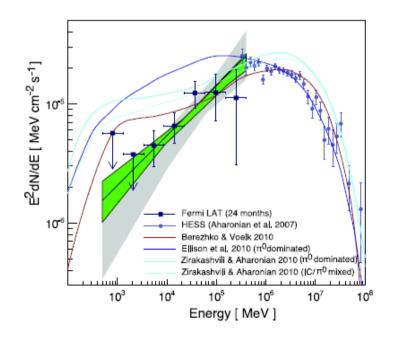


The remnant **RX J1713.7-3946** has been considered the most promising candidate to prove the existence of accelerated hadrons FermiLAT data seem to favor a probable leptonic origin

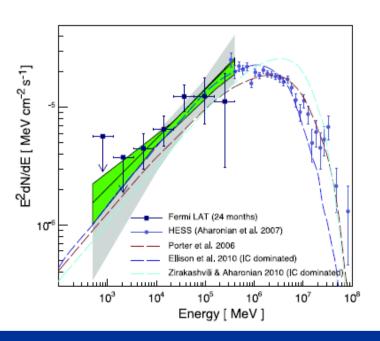
BUT...



### Hadronic model(s): $\pi^{\cdot} \rightarrow \gamma \gamma$

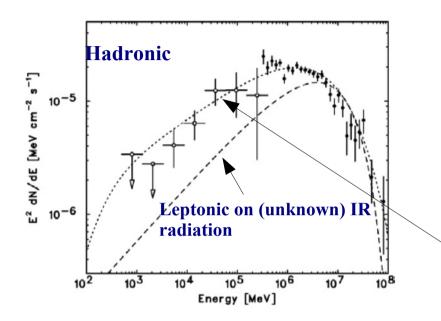


### **Leptonic model(s):** inverse Compton scattering





### Curves from T. Tanaka et al., ApJ 685 (2008)



# Clumpy CSM shock

### Both leptonic and hadronic models have problems in fitting Ge-TeV emission.

### Leptonic model (1 zone):

- Problems in fitting the highest energy points
- ♣ Need a IR background 30 > Gal. average

### Hadronic model in clumpy medium:

Reasonable fit with hard spectrum  $E^{-1.72}$  and with  $E_{p,cut}$ ~250 TeV

### How to produce hard spectrum?

Expansion in circumstellar medium with low average density but with high density clumps:

Nj High en. particles penetrate inside the clumps

Nj Low en. particles do not penetrate

Nj we get a hard spectrum



### •y-ray emission well correlate with Radio and X-ray emission

- •Main uncertainty due to distance 200pc < d < 1kpc
- •Both hadronic and leptonic model can fit the data
- •Lept. model favored for spectral shape but need  $B \sim 6 \ \mu G$ 
  - X-ray filaments require B~100 μG
  - Issue in fitting the shell in γrays
- $\rightarrow$  A better morphological study in  $\gamma$ -rays will help in distinguish between L. and H.

### Remnant size ~ 120'

